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Patch size reduction of rectangular microstrip antennas by means of a cuboid ridge

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Abstract: An effective approach to reduce the patch size in rectangular patch microstrip antennas is presented. The proposed approach is based on inductively loading the patch using a cuboid ridge. A theoretical background of the approach using the transmission line model has been provided. A prototype of the proposed antenna is fabricated and measured. The results, advantages and limitations of the proposed approach are presented and discussed.

1 Introduction

The widespread use of portable RF communication devices has increased the demands for low profile antennas. One of the most promising candidates for radiating element in modern wireless communication systems has been microstrip antennas. This is due to their well-known attractive characteristics such as low weight, low cost, possible conformity, ease of fabrication and simple design principle [1]. Microstrip antennas have been intensively developed during the past few decades and many of their shortcomings have been overcome.

In a conventional rectangular patch microstrip antenna, the length of the conducting patch is required to be of the order of a half wavelength to achieve a reasonable radiation performance. Such a patch size may be too large for some practical applications. The high demands for compact size antennas have made the patch miniaturisation one of the key challenges in microstrip antennas. A variety of techniques have been proposed for patch size miniaturisation in microstrip antennas. High dielectric constant material [2, 3], shorting walls [4, 5], shorting pin [6], folded patch [7], loading the patch with an inductive notch [8, 9] and irregular ground planes [10] have been some of those techniques.

In this paper, we present a new approach to reduce the patch size in rectangular patch microstrip antennas. This provides an uncomplicated, easily manufacturable low cost technique for patch miniaturisation. In this approach a flange cuboid ridge is placed in the middle of the patch to create a non-uniform height substrate in the radiating face of the antenna. In [11], numerical results indicate a downward shift in the resonance frequency of a rectangular patch microstrip antenna with a ridge in the middle. The present paper is a continuation of the study in [11], by a systematic investigation on the effect of a flange cuboid ridge on rectangular patch microstrip antennas. Furthermore, the present paper gives a complete physical understanding of the miniaturisation phenomena achieved by a flange discontinuity using the transmission line theory together with a parametric investigation of the approach.

In this paper the ridge is included in the transmission line model of the patch antenna using two different electromagnetic perspectives, as a series short-circuited stub or as a piece of transmission line with higher characteristic impedance. A prototype of the patch antenna with ridge is fabricated and measured. The measured and simulated results are presented and compared. The results indicate a significant reduction in physical dimension of the patch size. Many emerging applications have specific space requirements and therefore this work will disseminate new information and facilitate a new degree of freedom for antenna design engineers by providing at least three additional parameters characterising the antenna. These parameters are the height, width and location of the ridge. The proposed antenna provides a symmetric broadside radiation pattern. The simulation results show no substantial degradation in antenna gain as compared with a conventional patch antenna on a similar substrate and operating in the same frequency band.

Traditionally, microstrip patch antennas have been manufactured by etching a double sided printed circuit board. This paper demonstrates that the frequency can be reduced with a 3D substrate by manually combining separate substrates. However, this work has particular relevance to emerging manufacturing techniques and the consequent applications. For example, 3D substrates with curved or complex shapes can be easily created using 3D printing. Furthermore, wearable antennas are rapidly growing area of research [12]. In this case the patch antennas are generally assembled additively rather than by using destructive techniques and hence there are no fabrication disadvantages to altering the substrate height locally.

2 Configuration of the antenna

The configuration of a rectangular patch microstrip antenna with a cuboid ridge is illustrated in Fig. 1. The geometry consists of a grounded, square cross section dielectric substrate of dimension $W$ and thickness $h$ with a dielectric cuboid ridge of height $h_1$ and width of $g$ on the radiating face. The ridge is located between the two conducting sections of the patch with lengths of $l_1$ and $l_2$. These two sections are electrically connected through the conducting faces on top and sides of the ridge.

The substrate and the ridge are assumed to be homogeneous materials characterised by the permittivity $\varepsilon_{r1}$ and $\varepsilon_{r2}$, and the permeability $\mu_1$ and $\mu_2$, respectively. The antenna is fed by a coaxial line placed a distance $d$ from the edge of the patch and on the antenna symmetry plane.

3 Transmission line model

A conventional rectangular patch microstrip antenna can be approximately modelled by its basic transmission line circuit as shown in Fig. 2 [13, 14]. In this illustration, the resonant length of the patch is $L = L_1 + L_2$, where $L_1$ and $L_2$ are the distances of the feed point from each of the radiating slots at the edges and along the length of the patch. In this model each of the radiating slots is represented as a parallel RC circuit with a conductance $G$ and a
susceptance $j\omega C$. The patch connects the two $RC$ admittances as a transmission line. The value of the capacitance $C$ is proportional to the effective patch width divided by the thickness of the substrate ($C \propto a_w/h$ [1]). The effective width of the patch, $a_w$, is a function of the physical width of the patch, the thickness and dielectric constant of the substrate. It means for a wide patch on a thin substrate with a relatively high dielectric constant, the impedance of the radiating slots would be highly capacitive.

The length of the patch is usually about a half-wavelength at its resonance frequency. The location of the feed is such that $L_1 > \lambda/4$. Hence the highly capacitive admittance of the radiating slot is transformed to an inductive admittance $Y_1$ at the feed point. Similarly, since $L_2 < \lambda/4$, the transformed admittance $Y_2$ remains capacitive but with lower susceptance. If $L_1$ and $L_2$ have been carefully chosen, the susceptance seen from each side at the feed point cancel each other out [15] and the input admittance becomes purely real and the patch resonance. In other words, the length of the patch as a transmission line should be long enough to add sufficient value of inductance to the highly capacitive slot admittances to provide matching at the feed point.

By introducing a cuboid ridge in a rectangular patch microstrip antenna, the patch length required to obtain resonant matching at the feed point is reduced. This size reduction can be described based on the transmission line model of the patch antenna. Here, we investigate the ridge from two different perspectives, as a series flange stub and as a part of the transmission line with different characteristic impedance.

### 3.1 Ridge as a series stub

The flange discontinuity created by the ridge at one side of the feed point can be modelled as a short-circuited series stub in the transmission line model of the rectangular patch microstrip antenna.

The input impedance of a short-circuit terminated lossless transmission line seen looking toward and at a distance $d_s$ from the termination is given by [16]

$$Z_{in} = jZ_0 \tan \beta d_s,$$

where $\beta$ is the propagation constant and $Z_0$ is the characteristic impedance of the transmission line.

Since $\beta d_s$ can vary from $-\infty$ to $+\infty$, the input impedance of a short-circuited lossless line can be either purely inductive for $\tan \beta d_s > 0$ or purely capacitive, for $\tan \beta d_s < 0$. However, for a transmission line with a small electrical length, $\beta d_s \ll 1$, $\tan \beta d_s \approx \beta d_s$ and the input impedance is purely inductive and can be approximately determined by

$$Z_{in} \approx jZ_0 \beta d_s.$$  \hspace{1cm} (2)

This is a pure inductive impedance and hence, a short-circuited series stub in the patch transmission line model behaves as a series inductor $L$ as shown in Fig. 3. By adding this series inductive impedance to the transmission line model of the patch, the required inductance to provide matching at the feed point is partly achieved and the remaining part can be achieved by a shorter length of the patch.

When the patch width is much larger than the substrate thickness ($a \gg h$) the patch and ground plane can be approximately considered as a parallel plate waveguide. A brief formulation of a parallel plate waveguide is presented in the Appendix at the end of this paper. By assuming the ridge as a parallel plate waveguide, the impedance of this stub can be determined by substituting (9) and (10) into (2) as

$$Z_{ripp} \approx j\frac{\mu d_p}{\omega \varepsilon} \frac{d_s \sqrt{\mu \varepsilon}}{w_p}$$

$$= j\sqrt{\frac{\mu d_p}{\varepsilon}} \frac{d_s \sqrt{\mu \varepsilon}}{w_p} = j\omega \mu d_p d_s$$

Hence, for the ridge shown in Fig. 1, as a short stub, the contributed series inductive impedance can be approximately determined as

$$Z_{ridge} \approx j\omega \mu \frac{h_s}{a}.$$  \hspace{1cm} (4)

This equation shows that the impedance of a short ridge is a function of frequency, permeability of the material under the ridge, the patch width and the cross sectional area of the ridge. Hence for $h_s/\lambda \ll 1$, the dielectric constant of the medium under the ridge has no contribution in the ridge impedance.

The independence of the inductance provided by a short ridge from the dielectric constant of the medium under the ridge is also verified by our numerical simulations in CST Microwave Studio.

### 3.2 Ridge as a transmission line with different characteristic impedance

The ridge is a flange stub transformer in the transmission line model of the patch. Assuming the whole patch and the ground plane as a transmission line, the area under the ridge is part of this transmission line with different characteristic impedance than the
rest of the patch. This is due to the larger separation between the conductors in the area under the ridge. The discontinuities across the junctions at the edges of the ridge can be modelled as shunt capacitive susceptances at the junctions [17–19] as shown in Fig. 4.

A lossless transmission line is described by two circuit elements, a series inductance \( L \) and a shunt capacitance \( C \); where \( LC = \mu \epsilon \) [20]. For a parallel plate transmission line (see Fig. 12), \( C \propto 1/d_p \). Therefore, by increasing the separation between the plates in a parallel plate waveguide, the capacitance of the guide is reduced and consequently its inductance increases.

By adding the ridge to the patch, part of the transmission line which is located under the ridge has a greater separation distance between the plates as compared with other parts of the patch. Therefore, an increase in the inductance and a decrease in the capacitance associated to the transmission line model of the patch is expected. However, the reduced capacitance is compensated by the shunt conditional capacitive admittances due to the discontinuities at the junctions. Therefore, the overall capacitance of the antenna system remains unchanged, while the overall inductance has been increased.

The circuit model of a patch antenna filled with a hypothetical dispersion-free and lossless material is shown in Fig. 5. The resonance frequency of the antenna network can be determined by

\[
    f_0 = \frac{1}{2\pi\sqrt{L_C}},
\]

where \( L_0 \) and \( C_0 \) are the equivalent inductor and capacitor associated with the patch as a resonator.

According to (5), the resonance frequency of the antenna network can be lowered by inductively or capacitively loading the antenna. As explained, the ridge increases the overall inductance of the antenna network in (5). Such an increase, leads to a reduction in the resonance frequency. The size of the antenna can then be reduced to keep the operation frequency unchanged.

4 Results

To verify the proposed approach in miniaturisation of rectangular patch antennas, a prototype of the proposed antenna is designed, fabricated and measured. The fabricated prototype is depicted in Fig. 6. This is built on a square cross sectional, low loss Taconic laminate substrate of dielectric constant \( \epsilon_r = 2.2 \) with the lateral dimension of 70 mm. The substrate is 0.8 mm thick \((b)\) and is grounded on the bottom side. The two split parts of the patch of dimensions \((a, h_1) = (29, 15.5)\) mm and \((a, h_2) = (29, 9.5)\) mm are etched on the top side of the substrate. There is a gap of 7 mm width between these two parts. A cuboid laminate of dimensions \(29 \times 7 \times 1.6\) mm and dielectric constant of \(\epsilon_{r2} = 2.2\) is located in the gap area and affixed using two small drops of superglue. This cuboid laminate acts as a ridge of height \(h_1 = 1.6\) mm. The parameters of the antenna prototype are summarised in Table 1. It should be noted that according to our simulation results, the ridge is most effective if it is located at the centre of the patch \((l_1 = l_2)\). However, to provide a space for the feeding, a small offset from the centre has been considered.

The antenna is fed by a coaxial line at a point \(d = 12.5\) mm away from the edge of the larger part of the patch. The whole area of the two parts of the patch and the top and sides of the cuboid ridge are covered by a copper tape with conductive adhesive to provide a uniform electrically conductive area.

The simulated and measured \(|S_{11}|\) response of the antenna to a 50 \(\Omega\) port, as a function of frequency, are shown in Fig. 7. The antenna resonant at 2.35 GHz and the graphs indicate a good agreement between the simulated and measured results. The difference between measured and simulated bandwidth can be due to the fabrication of the prototype using lossy copper tape that is not considered in the simulated model.

To compare the proposed antenna with the conventional flat patch antennas, a rectangular patch antenna operating at the same frequency band is also designed using the same dielectric material substrate. The dimensions of the rectangular patch are 42 mm and

<table>
<thead>
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<th>Design parameters for the fabricated prototype. The dimensions are in millimetres</th>
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<tbody>
<tr>
<td>(W)</td>
</tr>
<tr>
<td>70</td>
</tr>
</tbody>
</table>

Fig. 5  Circuit network model of an ideal patch antenna

Fig. 4  Circuit representation of the patch antenna with ridge shown in Fig. 1. The ridge is modelled as a transmission line with different characteristic impedance

Fig. 6  Fabricated antenna prototype

Fig. 7  Simulation and measured results for reflection coefficient
38 mm for the resonant length and impedance length (patch width) respectively. The probe feed is located 15 mm away from the edge of the patch aligned the resonant length and at the centre of the impedance length. By comparing the dimensions of the two antennas, it is observed that by adding a 7 mm wide and 1.6 mm thick ridge, a 24% reduction in the resonant length of the antenna has been achieved. The comparison between this flat patch and the ridge patch antenna is summarised in Table 2. CST microwave studio [21] is the primary simulation tool in this paper, however, EMPIRE XCcel FDTD [22] is used to further corroborate the results in this paper. It should be noted that the resonant length can be reduced even further by using a wider or thicker ridge. Note the dimensions of the prototype are chosen due to material availability and just to verify the validity of the approach.

The measured and simulated realised gain of the proposed design are plotted in Fig. 8. The measured and simulated data are in agreement around the resonance frequency and illustrate the peak realised gain of 6 dBi in both cases. The difference between the broad side realised gain at frequencies upper and lower resonance can be due to spurious radiations from feeding network and fabrication uncertainties. As compared with the designed conventional patch antenna, no considerable difference is observed in the realised gain of the proposed antenna.

The measured and simulated radiation patterns of the proposed antenna at 2.35 GHz at E-plane and H-plane are plotted in Figs. 9a and b respectively. The measured and simulation radiation patterns are in agreement. It is observed that the antenna produces a fairly symmetric, broadside radiation pattern.

The presented miniaturisation approach using cuboid ridge may be looked similar to antennas reported in [23, 24], where a single step discontinuity is introduced in patch antenna to affect the resonant frequency and radiation efficiency. However, the phenomenon of variation in resonance frequency is completely different. The present paper provides a more general form of discontinuities, the flange ridge containing two step discontinuities, which reduces the resonant frequency by inductively loading the antenna equivalent circuit while in [24] by only one step, there will be no inductance loading. Furthermore, the present approach gives more free parameters for the antenna design, more effective for patch size reduction and also leads to a more compact design in terms of total volume of the antenna.

Table 2 Comparison of the conventional patch with the ridge patch prototype

<table>
<thead>
<tr>
<th></th>
<th>Flat patch</th>
<th>Ridge patch</th>
</tr>
</thead>
<tbody>
<tr>
<td>resonant length, mm</td>
<td>42</td>
<td>32</td>
</tr>
<tr>
<td>CST f, GHz</td>
<td>2.4</td>
<td>2.35</td>
</tr>
<tr>
<td>measured f, GHz</td>
<td>2.4</td>
<td>2.35</td>
</tr>
<tr>
<td>CST realized gain, dBi</td>
<td>6.5</td>
<td>6.0</td>
</tr>
<tr>
<td>measured realized gain, dBi</td>
<td>5.7</td>
<td>5.2</td>
</tr>
</tbody>
</table>

The presented miniaturisation using cuboid ridge may be looked similar to antennas reported in [23, 24], where a single step discontinuity is introduced in patch antenna to affect the resonant frequency and radiation efficiency. However, the phenomenon of variation in resonance frequency is completely different. The present paper provides a more general form of discontinuities, the flange ridge containing two step discontinuities, which reduces the resonant frequency by inductively loading the antenna equivalent circuit while in [24] by only one step, there will be no inductance loading. Furthermore, the present approach gives more free parameters for the antenna design, more effective for patch size reduction and also leads to a more compact design in terms of total volume of the antenna.

Fig. 9 Simulation and measured results for radiation pattern at 2.35 GHz

5 Design consideration

The proposed technique for size reduction of a rectangular patch microstrip antenna is based on inductively loading the antenna network. As explained in Section 3, a cuboid ridge in a rectangular patch microstrip antenna loads the antenna network with an inductance. The value of this loaded inductance can be approximately determined as

\[ L_{\text{ridge}} = \sqrt{\frac{\mu}{\varepsilon \omega}} \tan(\omega \sqrt{\mu \varepsilon h}). \]

The value of the inductance of the loaded antenna is then

\[ L \approx L_0 + L_{\text{ridge}}, \]

where \( L_0 \) is the inductance of the unloaded antenna.

Substituting (6) and (7) into (5) gives an approximate relation between the resonance frequency of an inductively loaded patch antenna with ridge and the resonance frequency of an unloaded conventional patch antenna with the same dimensions, \( f_{0\text{a}} \)

\[ f = \frac{f_{0\text{a}}}{\sqrt{1 + \frac{\mu \varepsilon h}{(g/a)\omega L_0} \tan(\omega \sqrt{\mu \varepsilon h})}}. \]

In (8), the ridge height \( h \) contributes as a term in the tangent argument. This implies that the rate of resonant frequency reduction by means of a cuboid ridge is faster for smaller values of the ridge height. As the ridge height increases the rate of resonant frequency reduction decreases.

The tangent term in (8) has \( 1/L_0 \) as a factor. Since \( L_0 \propto h \), it is implied that a ridge with a specific height is more efficient to reduce the resonant frequency of a patch antenna on a thinner substrate.

These characteristics are verified by simulation results shown in Fig. 10. In this figure the variation of resonance frequency of the patch antenna is presented as a function of ridge height, for two
different values of substrate thickness, \( h = 0.8 \) and \( h = 1.6 \) mm. For this numerical investigation, regardless of the substrate thickness and ridge height, all other parameters are the same as presented in Table 1. It is observed in the figure that the curves are steeper for smaller values of the ridge height. In other words, although the effect of ridge increase with its height growth, further increase in the ridge height is less effective but increases the volume of the antenna. It is also shown in Fig. 10 that a ridge with certain height is more effective in resonance frequency reduction for the patch antenna with a thinner dielectric substrate.

Another parameter that contributes to the ridge effect is its width, \( g \). An investigation has been carried out on the variation of resonance frequency with respect to the ridge width. In this investigation, a rectangular patch microstrip antenna with patch size of \( a = 146 \) mm and \( l_1 + l_2 + g = 116 \) mm, where \( l_1 = l_2 \), has been considered. The substrate is a 250 × 250 mm square cross section dielectric slab with \( \varepsilon_r = 2.2 \) and thickness of \( h = 1 \) mm. Three different values of ridge height are considered. The variation of resonance frequency as a function of ridge width, \( g \), is plotted in Fig. 11 for the three values of ridge height. It is observed that for all the three cases the resonance frequency is reduced as the width of the ridge starts to grow. This reduction in resonance frequency continues up to the limit \( g \approx l_1 + l_2 \). However, further increase in the length of the patch leads to an increase in resonance frequency. Hence, the maximum reduction in resonance frequency achieved by a ridge with specific height occurred when the length of the ridge is roughly equal to the half of the total resonance length of the patch. As the width of the ridge approaches the total patch length, the resonant frequency approaches the value for the unloaded regular patch, as expected.

One of the advantages of the presented approach for patch antenna miniaturisation is the simple design procedure and a high degree of flexibility for the designer. In contrast to other miniaturisation approach such as shorting pin which is very sensitive to the location of the pin and requires an optimisation process to design, the proposed approach provides a very simple design procedure

and is relatively robust to the distortion of design parameters.

The proposed technique can be used for the patch size reduction in microstrip antennas. Nevertheless, in most of the applications a smaller ground plane is also desired. In other words, the miniaturisation of the patch and keeping the ground plane size the same can be insufficient for some applications. In the comparison between the conventional patch antenna and the proposed antenna carried out in Section 4, the ground plane size was chosen the same for both of the antennas. This provides a fair gain comparison between two antennas. However, for an ordinary case, the minimum ground plane size for the proposed antenna with cuboid ridge can be much smaller than the smallest ground plane size required for the conventional patch on a similar substrate and operating in the same frequency. A simulation based investigation indicates that reducing the ground plane size up to \( \sim 1.1 \) times of the maximum patch dimension keeps the antenna performance for the both conventional patch and the cuboid ridge patch antennas. In both of the cases to reduce the ground plane size leads to reducing the broadside gain of the antenna and increasing the side-lobe level. A very small variation in resonant frequency is also observed.

### 6 Conclusion

An effective approach to reduce the patch size in rectangular patch microstrip antennas has been proposed. The approach is based on inductively loading the patch using a cuboid ridge. The cuboid ridge is included in the transmission line model of the patch antenna and a theoretical background of the approach has been explained. The concept was numerically and experimentally verified. The results, advantages and limitations of the proposed approach were presented and discussed. Design considerations and limitations have been investigated for the proposed antenna.

### 7 Acknowledgment

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### 8 References

medium of permittivity $\varepsilon$ and permeability $\mu$. Ideally, the plates are infinitely wide. However, the solution can well approximate the characteristics of plates of finite width provided that $w \gg d_p$.

The fundamental mode in a parallel plate waveguide is the TEM mode. The characteristic impedance for the TEM mode \(^{[20]}\) is

$$Z_0 = \frac{\eta d_p}{w_p}, \quad (9)$$

where $d_p$ is the separation distance between two strips, $w_p$ is the strip width and $\eta = \sqrt{\mu/\varepsilon}$ is the intrinsic impedance of the medium between the parallel plates.

The propagation constant of the TEM wave is

$$k = \omega \sqrt{\mu\varepsilon}, \quad (10)$$

where $\omega$ is the angular frequency.

Higher order modes in a parallel plate waveguide are $TM_n$ modes and $TE_n$ modes. The propagation constant for these modes is given by

$$\beta = \sqrt{k^2 - k_c^2}, \quad (11)$$

where $k_c$ is the cutoff wave-number given by \(^{[20]}\):

$$k_c = \frac{n \pi}{d_p}, \quad n = 0, 1, 2, 3 \ldots \quad (12)$$

The cutoff frequency of the $TM_n$ and $TE_n$ mode is the frequency that makes $\beta = 0$, and can be expressed as

$$f_c = \frac{k_c}{2 \pi \sqrt{\mu\varepsilon}} = \frac{n}{2 d_p \sqrt{\mu\varepsilon}}. \quad (13)$$

Waves with $f > f_c$ propagate with phase constant $\beta$, and waves with $f \leq f_c$ are evanescent.

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**9 Appendix**

**9.1 Parallel plate waveguide**

The geometry of a parallel plate waveguide is shown in Fig. 12. It contains two parallel conducting plates separated by a dielectric

![Fig. 12 Geometry of a parallel plate waveguide](image_url)