Transportable high-energy high-current inductive storage GW generator

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Citation: NOVAC, B.M. ...et al., 2014. Transportable high-energy high-current inductive storage GW generator. IEEE Transactions on Plasma Science, 42(10), pp. 2919-2933.

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Metadata Record: [https://dspace.lboro.ac.uk/2134/20453](https://dspace.lboro.ac.uk/2134/20453)

Version: Accepted for publication

Publisher: © IEEE

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Transportable High-Energy High-Current Inductive Storage GW Generator

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Abstract—A number of high-power applications require a transportable high-energy, high-current GW generator to drive a pulsed power system at the output. A first prototype, based on exploding wire technology and using an H-bridge circuit configuration, was developed at Loughborough University a few years ago and reported previously. The present stage of the work has necessitated the development of a more powerful and energetic source, and this is now based on inductive storage technology. A 400 kJ capacitor bank is connected by a high-Coulomb explosively-driven closing switch with an air-cored 0.6 MV transformer, an exploding wire array and a high-power diode based on a polarity-dependent spark-gap completing the arrangement. The GW generator, including the command and control module, is accommodated in two ISO containers.

The various components of the generator are described in the paper, together with results obtained from full-scale tests.

Index Terms—Closing switches, exploding wires, high-voltage technology, inductive storage, opening switches, pulse transformers

I. INTRODUCTION

During a large scale experimental program, it was necessary to supply a powerful impulse of many GWs to a system having a resistance of at least ten ohms and a self-inductance of many tens of micro-henrys. Such a load is uncommon in conventional high-energy, high-power applications and the design of the source that was required necessitated very careful consideration. Initially, a generator based on a capacitor bank storing only a few tens of kJs of energy was developed [1]. The arrangement, using an H-configuration circuit with a high-voltage ballast inductor and an exploding wire array contained in each pair of the diagonally opposite arms, successfully generated a peak output voltage of 300 kV and a load current of about 6 kA. Scaling-up the low-energy generator proved however difficult and led to the successful development of a novel high-energy generator, based on inductive energy storage technology.

The inductive energy storage technique was considered in the early 1960s in relation to high-energy plasma fusion projects. There are two great advantages of using inductive storage systems rather than capacitive storage based power sources: the magnetic energy density can be several thousand times greater than the electrostatic energy density and at a much lower cost [2]. The difficulty is that while a capacitive storage system naturally requires a closing switch an inductive storage system also needs an efficient opening switch and, as pulsed power practice has demonstrated many times, an opening switch is always more difficult to develop than a closing switch. An inductive storage system can also contain a transformer, used to match the system with a high-impedance load that requires a high-voltage pulse at a relatively low current. Such type of circuit, which is used in the present work, has been described previously [3-5]. As detailed below, the three novelties contained in the present paper are: an air-core transformer capable of withstanding very large magnetic forces, an inter-winding connection enabling (after the action of the opening switch) the generation of a very long current pulse in the load and the use of a high-voltage diode to attach the load.

The paper details the components of the novel inductive energy storage generator and shows that, a two-step development was required for two critical items, before they could reliably be incorporated in the overall arrangement. Data obtained during generator testing is presented and compared with predictions based on theoretical modelling.

II. GENERATOR OVERVIEW

Fig. 1 shows that the electrical equivalent circuit of the generator contains a capacitor bank \((C)\), a high-voltage transformer \((HVT)\), two closing switches \((S_1\) and \(S_2)\) and an ‘opening switch’ in the form of an exploding wire array \((EWA)\). The primary winding circuit of the HVT includes the high-Coulomb closing switch \(S_1\) that triggers the discharge of the capacitor bank, generating a current that charges the primary winding self-inductance \(L_P\) with magnetic energy and at the same time deposits Joule energy in the EWA. At the time the discharge begins, the time rate-of-change of this
current has a relatively high (positive) value, inducing a negative polarity precursor voltage pulse in the secondary winding. As the deposited Joule energy increases the wires explode, with the solid copper transformed firstly into liquid and finally into an ionised gas while the EWA resistance increases hundreds of times and a high-voltage is generated across the array (i.e., the circuit ‘opens’). Another consequence of the high resistance excursion of the EWA is the generation of a large (negative) time-rate-of-charge of the current, which in turn produces by induction a very high-voltage positive polarity impulse across the secondary winding of the HVT. The circuit is closed by the electrical self-breakdown of the high-voltage spark gap $S_2$ with part of the magnetic energy stored in $L_P$ being transferred into the self-inductance of the secondary winding circuit. The switch $S_2$ acts as a diode, removing the unwanted negative voltage precursor and connecting the load only as the voltage becomes positive. This action conditions the load current by reducing its rise time in comparison with the rise time should the load be connected at the beginning of the capacitor bank discharge (i.e., $S_2$ is closed at all times).

An interesting and novel feature of the present generator is the interconnection provided between the two transformer windings, which enables the load to be powered with a long duration slowly decaying current. The operation is as follows: once the EWA ‘opens’ the current $I_{EWA}$ in the EWA becomes negligible and the load current $I_L$ is practically equal to the primary current $I_P$, allowing the load to remain energized for a long period of time determined by the characteristic time constant of the circuit: $(R+R_L)C$. The differential equations governing the generator circuits together with a detailed analysis are presented later.

The components of the primary winding circuit are:
- a capacitor bank containing eight capacitors type General Atomic Energy Products (GAEP) 32349 [6], with a combined capacitance $C = 1715 \mu F$. When charged to its rated voltage $V_o = 22 \text{ kV}$, by a $8 \text{ kJ/s}$ charger type GAEP CCS0802P1D [6], the bank stores 415 kJ;
- a high-Coulomb closing switch $S_1$, similar to that described in [1], operated using up to five detonators. In the tests described later it was always driven by only three detonators, when the switch self-inductance was only 0.5 nH and its effective resistance less than 0.5 mΩ;
- an opening switch $EWA$ made from 99.99%, temper annealed, oxygen free, high conductivity (OFHC C110) copper wires, each 500 µm in diameter and up to 500 mm long. Each wire is housed in an acrylic cylindrical cartridge filled with 40 µm glass beads (sand) and sealed with hot melt glue. The $EWA$ arrangement allows a total of up to 20 cartridges to be mounted.

The total self-inductance and resistance of the primary winding circuit at the beginning of a discharge are $L = 60 \text{ nH}$ and $R = 3.1 \text{ mΩ}$. These values exclude the contribution from the HVT primary winding but include those from the capacitor bank (10 nH, 1 mΩ), transmission lines (12 nH, negligible resistance), detonator-activated closing switch $S_1$ (0.5 nH, 0.5 mΩ) and an $EWA$ using 16 wires, each 300 mm long (38 nH, 1.6 mΩ).

Fig. 2 shows a block-diagram of the overall generator assembly which was installed in a 20ft ISO container with Figs. 3 and 4 showing some of the important constituent parts. As presented in Fig. 2, the pulsed power generator requires two capacitor banks: a high-energy high-voltage unit (415 kJ/22 kV) to drive the generator and a low-energy low-voltage unit (10 J/4.5 kV) to trigger the detonators used to operate the switch $S_1$. Both banks have dedicated high-voltage chargers which are each monitored using a DC high-voltage probe coupled to a laptop via a picoscope and a fiber-optic interface. For both banks, ancillary ‘isolate and dump’ systems are used to disconnect the chargers during a shot or to release the bank energy into high-value resistors if the test needs to be aborted. All capacitor bank instrumentation is controlled via pneumatics and fiber-optics from a command and control module installed in a separate 10ft ISO container (Fig. 4(d)), with both containers powered by dedicated diesel generators. Details of the diagnostic instrumentation shown in Fig. 2 are presented later.

III. DEVELOPMENT OF CRITICAL COMPONENTS

A. Development of the air-core HVTs

1) The development of the helical HVT

HVTs for use in high-power systems are normally constructed in either a spiral-strip configuration [5], with the primary and secondary windings both of copper sheet, or a helical arrangement [7] in which the secondary winding is made using a relatively thin round copper conductor. More recently, a further design has appeared [8], with a coaxial primary and a toroidal secondary winding made from insulated cable. The merits and drawbacks of all three designs are summarized in Table I.

After discarding the spiral-strip design for reasons mainly related to simplicity, a first version of the HVT was constructed using the technique employed in many Tesla-type air-core transformers previously developed at Loughborough (Fig. 5). The primary winding is a single-turn copper strip.
100 mm wide by 5 mm thick, rolled into a 490 mm inner diameter loop and secured on the outside of a polyethylene oil-filled drum. The secondary winding has 14 turns, with a constant pitch of 8.47 mm, wound on a polyethylene mandrel grooved to locate the wire, as shown in Fig 5(a) and mounted inside the polyethylene drum. The first 9 turns are coaxial-helical with a (constant) inner diameter of 457 mm and the last 5 are conical-helical, with the taper linearly reducing the diameter for additional high-voltage insulation to 444 mm. In reference to Fig. 1, the inductances of the helical HVT were calculated by filamentary modelling [9] as $L_p = 767 \, \text{nH}$, $L_S = 128 \, \mu\text{H}$ and $M_{PS} = 8 \, \mu\text{H}$, which give a magnetic coupling coefficient $k = 0.807$. Preliminary low voltage experiments confirmed these values.
Fig. 4. Components of the pulsed power generator a) the high-voltage side of the stripline connected between capacitor bank and switch \( S_1 \); b) Detonator-activated high-Coulomb closing switch \( S_1 \); c) Opening switch: exploding wire array (EWA) with 16 cartridges connected in parallel; for EWA details see text d) Details showing a EWA cartridge mounted at the end of the transmission line; the direction of current flow is also indicated e) Command and control module installed inside a 10ft ISO container

<table>
<thead>
<tr>
<th>TABLE I</th>
<th>RELATIVE MERITS AND DRAWBACKS OF THREE HVT DESIGNS WHEN USED IN HIGH-POWER SYSTEMS</th>
</tr>
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<tbody>
<tr>
<td>Type</td>
<td>Advantages</td>
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</table>
| Spiral-strip | • high coupling coefficient possible (>0.9)  
• can carry high currents (>1MA) in both winding circuits  
• coaxial output as required by most loads  
• can be scaled to multi-MV operation (but only when immersed in a liquid such as oil or solution of CuSO4) | • primary input easily coupled to a parallel transmission line but requires an adaptor ('fish-tail') to couple to coaxial configurations  
• elaborate manufacturing due to voltage grading and other techniques required to handle the high electric fields generated by strip edges  
• high secondary capacitance |
| Helical | • relatively easy to manufacture  
• -can be easily adapted to coaxial geometry  
• -low secondary winding capacitance  
• -can have extremely high secondary/primary ratios | • low coupling coefficient (<0.8)  
• difficult to scale up above 1MV  
• cannot drive high currents in the secondary winding |
| Coaxial | • high coupling coefficient possible (>0.9)  
• does not require oil or pressurised gas  
• can be scaled to multi-MV operation  
• can carry a high current (>1MA) in the primary circuit  
• relatively easy to manufacture  
• extremely robust, able to handle very large forces  
• coaxial input  
• very low secondary winding capacitance | • the output is not coaxial  
• cannot drive large currents in the secondary winding |
In an effort to increase the mechanical inertia, the secondary was wound with 4 mm diameter, but the forces generated of about 2 tons per turn still pulled the wire out of the mandrel groove. This occurred even when the additional restraining technique shown in Fig. 5(b) and various other approaches were adopted. The final elegant and simple solution was to fill the mandrel grooves above the wire by polyethylene welding, thus completely encapsulating the winding as seen in Fig. 5(c). The resulting helical HVT (Fig. 5(d)), still requires oil to insulate its output, but has so far successfully survived a number of high-energy shots in which the load current was of the order of 10 kA. The helical HVT allows a voltage probe to be mounted at the secondary output which was extremely useful in facilitating the detailed analysis presented later, related to the extreme peak voltage induced when S2 opens, and helped in highlighting an important design issue. However, because it was decided to abandon the use of oil in the generator when mounted inside a container together with the need to produce much greater load currents in subsequent work attention turned to the alternative of a coaxial design.

2) The development of the helical HVT

The artistic view of a coaxial HVT of Fig. 6 shows the outer conductor of the coaxial single-turn primary winding, in which
the current flow is axial (Fig. 6(a) and 6(c)) and the multi-turn
 toroidal secondary winding located within the primary
 winding (Fig. 6(a) and 6(b)).

The primary winding coaxial is open at one end (Fig. 6c) and
short-circuited at the other. The inner conductor located at
the center is a thick aluminum tube covered with a thick
insulating tube and connected to a plate. The outer coaxial
conductor is a relatively thin copper layer mounted on a thick
plastic support, the ‘top-hat’ insulator, and connected to a
second plate. Fig. 6(c) shows the two plates, which are
inserted in the upper high-voltage part of the capacitor bank
transmission line (Fig. 4a), between the switch \( S_1 \) (Fig. 4b) and
the EWA (Fig. 4c).

The toroidal secondary winding is made from insulated
cable and mounted on a very thick cylindrical plastic former
inside the primary winding. The input to the secondary
winding is attached to the central aluminum tube to provide
the necessary inter-winding interconnection and, as Fig. 6b
shows, the high-voltage output exits via a well-insulated hole
made in the outer copper layer. Design of the \( HVT \) requires
accurate calculation of all the three transformer inductances,
together with their dynamic resistances (taking both into skin
and proximity effects into account) and finally the
electromagnetic forces acting on the \( HVT \) structure during a
shot. The specific methods used to calculate these details are
explained below.

3) Calculation of self and mutual inductance

The self-inductances of both the primary and secondary
windings can be obtained from standard textbook formulae
[10]:

\[
L_p = \frac{\mu_0 Z_{\text{max}}}{2\pi} \ln \left( \frac{R_p}{r_p} \right) \tag{1}
\]

\[
L_S = \frac{\mu_0 N^2 (Z_{\text{max}} - Z_c)}{2\pi} \ln \left( \frac{R_S}{r_S} \right) \tag{2}
\]

where \( Z_{\text{max}} \) is the axial length of the \( HVT \) and \( Z_c \) is twice the
bending radius of the secondary winding cables. \( R \) and \( r \) are
outer and inner radii and subscripts \( P \) and \( S \) indicate
respectively the primary and secondary windings. Both
equations are valid only for \( Z_{\text{max}} \gg R \) (with \( R > r \)).

When cylindrical coordinates \( (r, \theta, z) \) are used it is well-
known that in a coaxial structure, with a current flowing along
the \( z \)-axis, the magnetic flux-density generated is circular \( (B_\theta) \). It
then follows that the mutual inductance can be obtained from
an equation similar to Eq. 1 to determine the magnetic flux
linking one turn of the secondary winding. For \( N \) turns the
result is:
\[ M_{ps} = \mu_0 N (Z_{max} - Z_C) \ln \left( \frac{R_s}{r_s} \right) \]
which provides a conservative figure due to neglect of the (small) magnetic flux linked to the two regions where the cables are bent.

The errors involved in Eq. 2 cannot be readily estimated, and an analysis was therefore undertaken using a more precise method of calculation. Each turn was regarded as a plane rectangle made from four very thin straight metallic wires, with the Biot-Savart formula used to calculate the magnetic flux density distribution produced by a current flowing round the rectangle. The result is used in determining the mutual inductance between the various pairs of turns \( M_{ij} \) circularly positioned with an angle \( 2\pi/N \) between any adjacent pair. With the self-inductance of each turn \( L_s \) obtained using a standard textbook formula [10], the calculated overall secondary winding self-inductance is given by:
\[ L_s^2 = \sum_{i=1}^{N} L_i + \frac{1}{2} \sum_{i=1}^{N} \sum_{j=1}^{N} M_{ij} \]

In most cases studied so far, the difference between the estimate provided by Eq. 2 and the more precise result obtained using Eq. 4 turns out to be very small, with the estimate typically being about 1.5% larger than the more precise figure.

4) Calculation of dynamic resistance

Although the calculation of the dynamic resistances of all the HVT components, using both skin and proximity effects, can readily be performed this was unnecessary in the present study, as the resistance introduced by the EWA in the primary winding circuit and the load system in the secondary winding circuit are some two-orders of magnitude greater.

5) Calculation of forces

Between the primary coaxial conductors, the magnetic flux density generated by a primary current \( I_p \) flowing through the aluminum tube can be obtained using the **Ampère's Circuital Law** [10] as \( B(r) = \frac{\mu_0 I_p}{2\pi r} \), assuming \( r_P < r < R_P \). This magnetic field interacts with a secondary current \( I_s \) flowing through the inner \((i)\) and outer \((o)\) straight axial section of length \( Z_{max} - Z_C \) of each secondary winding rectangle, with the resulting radial **Ampère's forces** [10] being:
\[ F_r^i = \frac{\mu_0 I_p I_s}{2\pi r} (Z_{max} - Z_C) \]
\[ F_r^o = \frac{\mu_0 I_p I_s}{2\pi R} (Z_{max} - Z_C) \]

6) Final design characteristics

After considering all aspects related to implementing the HVT into the pulsed power circuit of Fig. 1, the following design parameters were established:

- **Toroidal secondary winding:** \( N = 15 \) turns made from a high voltage (HV) cable, each with \( r_S = 91 \) mm and \( R_S = 778 \) mm. The minimum bending radius specified by the cable manufacturer is 150 mm, resulting in \( Z_C = 300 \) mm.

Although the resulting electrical parameters are: \( L_P = 886.52 \) nH, \( L_S = 127.69 \) µH and \( M_{PS} = 8.51 \) µH, with the magnetic coupling coefficient estimated as \( k_{theory} \approx 0.8 \). This value was later confirmed during preliminary testing as \( k_{opt} = 0.806 \).

It will be noted that coaxial transformers can easily be produced with coupling coefficients in excess of 0.9. However, as the most stringent requirement for the present transformer is to withstand a large number of shots whilst extremely heavy loaded due to electromagnetically generated forces, all the insulation employed has a thickness much greater than that necessary to prevent electrical breakdown. For example, the thickness of the cylindrical insulator covering the central metallic tube is 20 mm, well above that dictated by electric breakdown requirements. This inevitably reduced the values of the mutual inductance.

7) Preliminary testing of the secondary winding high-voltage cable

The high-voltage cable used in the manufacture of the present coaxial HVT is type C2236, from series 2400 of the X-ray cables produced by Essex X-ray [11]. The cable is coaxial with an overall outer diameter of 38 mm, it can withstand 250 kV DC and has a core made from a collection of three stranded wires covered with rubber (ethylene propylene diene monomer). After removing the outer protective PVC jacket and the metallic braid, the overall outer diameter of the remaining cable is 32.5 mm and it was used as such in the construction of the transformer i.e., no effort was made to remove the semiconductor layer, resulting a cable weighing less than 1.7 kg/m.

The calculated peak values for the HVT currents of \( I_P = 400 \) kA and \( I_S = 20 \) kA result in large radial forces: \( F_{r^i} = 2.2 \) tons (18.3 kg/cm) and \( F_{r^o} = 0.25 \) tons (2.1 kg/cm).

However, the generator is required on occasions to produce a bipolar current \( (S_o \text{ permanently closed}) \), resulting in radial forces that change in direction. In time this effect may lead to internal damage to the cable, in ways that are particularly difficult to estimate. Instead of a long and tedious investigation, it was decided to test the cable against a force considerable higher than the ‘normal’ peak force calculated above. A section of the high-voltage cable was used as part of a parallel transmission line and, by discharging the Quattro bank [5], the sinusoidal current shown in Fig. 7, with a 280 kA peak, was passed through the cable. The corresponding force acting on the inner stranded wires was calculated as 262 kg/cm i.e., 16 times larger than the peak force experienced under normal operation, and the experiment was repeated twice. ‘Post-mortem’ investigation, performed by cutting the cable into two along its length, revealed no damage to the insulating rubber but the very thin insulation of the three strands was completely destroyed. This result was considered, perhaps slightly optimistically, as an indication that under normal circumstances the degradation of the cable, when mounted inside the HVT, will be a long and slow process.
8) Manufacture and mounting of the coaxial HVT

Both the manufacture of the coaxial HVT and its mounting inside the 20ft container were challenging and Figs 8-11 show various stages of this process. Following this, an intensive test program was performed without raising any issues.

B. Development of the high-voltage diode

1) The role of the HV diode

With no switch in the secondary winding circuit (i.e., \( S_2 \) closed from the beginning of the bank discharge) an \( emf = -M_{ps}dI_p/dt \) is generated (where \( dI_p/dt > 0 \) represents the time rate-of-change of the primary winding circuit current), driving the load system with a negative voltage. When the EWA opens, the current falls rapidly (i.e., \( dI_p/dt << 0 \)) generating a corresponding \( emf > 0 \) and the system load voltage eventually becomes positive resulting in a bi-polar output. If however a closing switch is used as a HV diode, it must firstly withstand the negative voltage impulse and close at a relatively low positive voltage to optimize the rise time of the load system current after EWA opens.

It is interesting to note that, if \( S_2 \) does not close during a shot, the open circuit \( emf \) may attain values well in excess of 1 MV, and the HVT would almost certainly suffer an internal electrical breakdown!

With the helical HVT based generator, an existing HV closing switch [5] was firstly used as a diode, but this was later abandoned because it requires pressurized \( SF_6 \) and operation under oil. Once the use of oil was abandoned, a novel HV diode capable of operating in ambient air was required, with the principal aim during its design and preliminary testing being to ensure that it could withstand a high negative voltage of up to -300 kV and at the same time close easily at about +140 kV. Preliminary tests were undertaken at Pau University (France) to determine the optimum geometrical configuration of the novel HV diode, using similar temporal characteristics of the loading voltage that were similar to those generated when the unit forms part of the high-energy high-power generator.

2) Preliminary test arrangement

The HV diode of Fig. 12(a) is essentially a rod/plate configuration, operated in ambient air with the metallic plate
During the high-energy generator tests described later, the gap was fixed at between 180 mm and 200 mm. 

5) **3-D electrostatic simulations**

The CST EM Studio 3-D electrostatic solver [14] includes solver modules ideally suited to the analysis of static and low frequency devices and was therefore used to gain an improved understanding of the functioning of the HV diode. Both experimental conditions outlined above were simulated, with Fig. 14 presenting 2-D and 3-D views of the electric field distribution for negative polarity. Figs. 15 and 16 show the voltage evolution and the electric field distribution along the vertical central axis of the arrangement. The tip of the rod corresponds to the origin \( z = 0 \) mm with the plate situated at \( z = d_p = 200 \) mm for the negative polarity test and \( z = d_p = 130 \) mm for the positive polarity test. The results show that the electric field generated in the immediate vicinity of the rod is very strong i.e., 280 kV/cm for the negative polarity and 80 kV/cm for positive polarity. Thereafter it decreases exponentially towards the metal plate, where it becomes only 9 kV/cm for the negative polarity and 5.7 kV/cm for the positive polarity. It is important to note that the static electric field magnitude, as considered by the software, is not polarity dependent and but only changes due to the geometry of the two electrodes.

6) **Analysis**

To initiate the electrical discharge, the first condition is related to the electrical field intensity in the immediate vicinity of the rod. In air, the homogeneous DC breakdown field is estimated at 30 kV/cm/bar [15, 16] although it is much greater under pulsed conditions when a spark-gap can withstand 2-3 times the voltage under DC conditions [17]. The value of the overvoltage is a function of the gas composition, the gap spacing, the polarity and rise-time of the voltage impulse and is attributed to the delay introduced (i.e., statistical time-lag) while waiting for a seed electron to appear [18, 19]. In the present test conditions, the breakdown is required during the positive rise of the transformer voltage, when the time allowed for the seed electrons to appear is short (a few \( \mu s \)) and therefore the stability and the reproducibility of the load output pulse is very much improved. Since the level of the overvoltage will increase as the pulse rise-time reduces [18] it should be possible, by applying a fast pulse, to achieve significant overvoltage and subsequent ionisation of a spark-gap, leading to the rapid collapse of the channel.

Additionally, in air, propagation of a breakdown is attributed to the discharge propagation with the positive streamers described by a model that considers the head of the streamer as a sphere with a concentrated positive charge [20, 21]. The energy balance at the head determines the propagation of the streamer, and there is a propagated electric field in which the streamer can continue to grow without losing or gaining charges. The values of this field are 5 kV/cm/bar for positive polarity and 18 kV/cm/bar for negative polarity, which explains the polarity dependence of the breakdown of the present HV diode. The molecular binding forces in air are sufficiently low for the negative space charge behind the streamer to be sufficiently far away for the assumption of a unipolar space charge to be justified and the contribution of the space charge to be decisive. The space charge field could be taken into account by a microscopic...
Fig. 12. a) Arrangement for testing the HV diode (a) schematic (b) during testing.

Fig. 13. Results from testing the HV diode (a) closure at -310 kV (b) closure at +140 kV

Fig. 14. Electric field distribution in negative polarity obtained with CST software a) 3-D view for an applied voltage of -310 kV and b) 2-D representation.
model, but this is beyond the scope of the present study. The spatial distributions of the electric field in Figs. 15(b) and 16(b) confirm the validity of the above argument. For positive polarity, the electric field in the immediate vicinity of the rod reaches 80 kV/cm, greater than the critical field in air of 30 kV/cm because of the pulse conditions, and the discharge can be initiated. After this, the electric field remains above the propagation field of the streamers in air of about 5 kV/cm for this polarity, and a breakdown can occur. For negative polarity at -310 kV, the electric field in the vicinity of the rod is sufficiently strong and allows the electric field along the axis to be maintained sufficiently high to initiate a breakdown.

IV. TESTING THE HIGH-ENERGY HIGH-CURRENT GW GENERATOR

The diagnostic equipment used in testing included:
- a magnetic pick-up probe mounted in a transmission line tunnel, calibrated in situ and used to measure $dI/dt$. Following a test, the current waveform $I_p(t)$ is obtained by numerical integration;
- a Pearson current monitor [22] model 3025 for the direct measurement of the load current;
- three North-Star high-voltage probes [12]: type PVM-6 for the EWA, type VD-300 for the load and type MEGA-1.2 for the HVT output.

The sensors were attached to 300 MHz (or 500 MHz) Tektronix [13] oscilloscopes, powered either by internal batteries or UPS units.

A. High-power bipolar-mode operation

In this mode switch $S_2$ is closed from the beginning of the capacitor bank discharge i.e., the load system is at all times attached to the generator. In the example considered here both the load self-inductance $L_L = 25 \mu H$ and its resistance $R_L = 36 \Omega$ remain constant during the shot. The load current is shown in Fig. 17 and the energy balance in Fig. 18. The generator provides the system with a peak power close to 3 GW, maintains the power in excess of 1 GW for almost 4 µs and deposits a load Joule energy in excess of 23 kJ.

B. Detailed analysis of single-mode operation

In this mode the switch $S_2$ acts like a HV diode, attaching the load system only when the voltage in the secondary winding becomes positive.
The first-order differential equations used to simulate the operation of the inductive-storage system of Fig. 1 are:

a) when \( S_1 \) is closed and \( S_2 \) is open, \( I_{EWA} = I_P \) and \( I_S = 0 \):
\[
V_o - \frac{Q}{C} = (L + L_p) \frac{dI_P}{dt} + (R + R_{EWA}) I_P
\]
\[
\frac{dQ}{dt} = I_P
\]
\[
\frac{dW}{dt} = \frac{I_P^2 R_{EWA}}{m_{EWA}}
\] (6a)

b) when \( S_1 \) is closed and \( S_2 \) is closed; \( I_{EWA} = I_P - I_S \)
\[
V_o - \frac{Q}{C} = (L + L_p) \frac{dI_P}{dt} + R I_P + R_{EWA} (I_P - I_S) + M_{PS} \frac{dI_S}{dt}
\]
\[
0 = (L + L_s) \frac{dI_S}{dt} + R I_S - R_{EWA} (I_P - I_S) + M_{PS} \frac{dI_P}{dt}
\] (6b)

In the equations above \( Q \) is the charge injected into the circuit by the capacitor bank and \( W \) is the specific Joule energy i.e., the energy deposited in the EWA mass \( m_{EWA} \). The EWA resistance \( R_{EWA} \), which depends only on \( W \), is obtained from a phenomenological model for exploding wires similar to that presented in [3]. However, in [3] the wires were relatively thin and operated in air while the present model, presented in Fig. 19, is for thicker exploding wires operated in sand. During computation, a number is obtained for each value of \( W \), representing the dynamic resistance i.e., the ratio between the required ‘hot’ resistance and the initial ‘cold’ resistance of the wires measured immediately before the shot.

Figs. 20-24 compare detailed experimental data that enables the dynamic characteristics to be obtained for a load system with a constant self-inductance \( L_L = 25 \mu H \) and a time-varying resistance \( R_L(t) \) decreasing linearly in 250 ns from 100 \( \Omega \) to 20 \( \Omega \). The rise time of the load current is less than 2 \( \mu s \). It is important to note that when the load system is coupled at \( V_S = 323 \) kV (see Fig. 23), inductive effects generate in the secondary winding of the HVT a peak voltage reaching \( -M_{PS} \frac{dI_P}{dt} + L_s \frac{dI_S}{dt} = 553 \) kV. This unwanted phenomenon is the reason why the design of a HVT to produce a peak load voltage in excess of 400 kV, must take into account that the peak voltage in the secondary winding exceeds 600 kV!

C. Powering extremely large self-inductance systems

In the final example, similar to that presented above, the load system has an extremely large constant self-inductance \( L_L = 50 \mu H \) and a dynamic resistance \( R_L(t) \) falling from 30 \( \Omega \) to 10 \( \Omega \) in 4 \( \mu s \). The principal results shown in Figs. 25 and 26 confirm that the generator is capable of maintaining an...
Fig. 20. a) Time dependence of primary winding circuit current and b) its time rate-of-change. Continuous lines: experimental data; dotted lines: theoretical predictions.

Fig. 21. Voltage across EWA (16 wires mounted in parallel, each 500 µm thick and 300 mm long, fired in quartz sand). Continuous line: experimental data; dotted line: theoretical prediction using the model shown in Fig. 19.

Fig. 22. Current delivered to the load system during single-mode operation; the load has a constant self-inductance $L_L = 25$ µH and a time-varying resistance $R_L(t)$ decreasing linearly in 250 ns from 100 Ω to 20 Ω.

Fig. 23. Voltage across HVT output compared with that across the load for the experiment of Fig. 22. a) complete time history b) zoomed view around the time when the switch $S_2$ closes (indicated by an arrow) attaching the load system. The switch removes the long negative precursor seen in a) and at the same time conditions the load current and voltage.
electrical power output in excess of 1 GW for more than 5 µs, while depositing more than 15 kJ of Joule energy and Fig. 27 presents stills from a movie with 1000 frames/s, showing the diode plasma dynamics during the shot.

V. CONCLUSIONS

A unique generator, capable of driving a system with a self-inductance of many tens of µHs and a resistance of tens of Ωs, has been successfully demonstrated at GW power levels. The transportable pulsed power source, mounted in a container, includes a novel design of a coaxial 0.6 MV transformer and a high-power diode, both operating in ambient air. To date the generator has been operated at about 50% of its maximum initial energy and theoretical predictions, very accurate for the existing data, show that peak powers in excess of 3 GW and Joule energies above 40 kJ can be produced on high-inductance, high-resistive load systems.
REFERENCES


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