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GPU Implementation of DPSO-RE Algorithm for Parameters Identification of Surface PMSM Considering VSI Nonlinearity

Zhao-Hua Liu, Member, IEEE, Hua-Liang Wei, Qing-Chang Zhong, Fellow, IEEE, Kan Liu, Member, IEEE, and Xiao-Hua Li

Abstract: In this study, an accurate parameter estimation model of surface permanent magnet synchronous machines (SPMSM) is established by taking into account voltage-source-inverter (VSI) nonlinearity. A fast dynamic particle swarm optimization (DPSO) algorithm combined with a receptor editing (RE) strategy is proposed to explore the optimal values of parameter estimations. This combination provides an accelerated implementation on graphics processing unit (GPU), and the proposed method is therefore referred to as G-DPSO-RE. In G-DPSO-RE, a dynamic labor division strategy is incorporated into the swarms according to the designed evolutionary factor during the evolution process. Two novel modifications of the movement equation are designed to update the velocity of particles. Moreover, a chaotic-logic based immune receptor editing operator is developed to global best individual (gBest particle) to explore a potentially better region. Furthermore, a GPU parallel acceleration technique is utilized to speed up parameter estimation procedure. It has been demonstrated that the proposed method is effective for simultaneous estimation of the PMSM parameters and the disturbance voltage ($V_{\text{dead}}$) due to VSI nonlinearity from experimental data for currents and rotor speed measured with inexpensive equipment. The influence of the VSI nonlinearity on the accuracy of parameter estimation is analyzed.

Index Terms: particle swarm optimization (PSO), artificial immune system (AIS), Graphics Processing Unit (GPU), parallel computing, parameter estimation, permanent magnet synchronous machines (PMSMs), voltage-source-inverter (VSI), nonlinearity.

I. INTRODUCTION

RECENTLY, permanent magnet synchronous machines (PMSMs) are widely used in high-performance applications such as industrial robots, servo drive, wind power generation, and machine tools due to their overall good performance [1]-[2]. The design of the control system of such a machines crucially involves the choice of many key machine parameters such as winding resistance, dq-axis inductances, and rotor PM flux linkage [3][4]. Any change of these parameters could affect the system behavior and therefore the change in these parameters can be used to evaluate the health conditions of PMSM. For example, the inter-turn short circuit can result in an abrupt change in winding resistance and inductance [5]; the demagnetization can result in a sudden decrease in the amplitude of fundamental back electromotive force (EMF) [6]. A controller with inappropriately designed parameters cannot work well, and can lead to a dysfunction of the machine especially for high power machines and large scale equipment or systems [4]. A PMSM is time-varying system, whose parameters are sensitive to the change of environmental conditions such as temperature, noise, load torque, and the aging of the motor, etc. [7].

Recently, many parameter estimation approaches have been introduced in the literatures. Some measurement instruments such as thermal couplers, search coils and load test bench [8] were applied to observe the machine parameters. However, they are usually not preferred in practice for the potential increase of cost. In practical engineering, parameter optimization using numerical methods is an ideal technology for directly estimating the needed parameters based on regular measurable data [7]. Existing research mainly focused on online estimation algorithms including self-commissioning technique [2] , extended Kalman filter (EKF) [9], model reference adaptive system (MRAS) [10], recursive least-squares (RLS) [3] [11], adaptive observer [12], and artificial neural networks (ANN) [10] [11]. However, with the increasing complexity of operation conditions, these methods may not always work well. For example, in [9], an EKF algorithm was proposed to estimate the rotor speed and position of PMSM, but it may be difficult for real applications as the algorithm is sensitive to noise. The MRAS estimators proposed in [10] cannot simultaneously estimate winding resistance, inductance and rotor flux linkage accurately. In this method, in order to estimate a group of parameters, some are fixed to their nominal values for the estimation of other parameters given in the motor manual. For example, the winding resistance parameter needs to be set to its nominal value in order to estimate the rotor flux linkage afterward, the accuracy of estimation results depend on the accuracy of the nominal values of machine. However, the nominal value is usually not consistent with the actual operating value, thus these
estimators cannot ensure to converge to the actual parameter value. In comparison with other algorithms, RLS possesses a good property of rapid convergence rate, but the algorithm may suffer from high computational burden and poor tracking ability in non-stationary environments [3]. An adaptive observer was introduced in [12] to obtain the estimated values of PMSM systems. It can estimate the PMSM parameters accurately, but has poor robustness when dealing with the uncertainties in machine parameters estimation. Usually, the existing parameter estimation models are based on the conventional dq-axis equation, the dq-axis equations will be rank deficient for estimating three or four parameters when the motor is operating at a steady state, thus the estimation results may converge to suboptimal. To solve the rank deficient problem, the d-axis current injection method can be used to increase the number of state equations due to the variation of d-axis current [11]. PMSM is usually fed by a voltage source inverter (VSI), and the reference voltages for the parameter estimator are measured from the PI regulator in a PMSM vector control system. This may introduce an error between the reference voltage of the controller and the actual output voltage of the VSI. Commonly, the researcher uses the relevant parameters of the switching devices to calculated the VSI disturbance voltage, and then to compensate the reference voltage of the controller [13]. However, some device parameters (e.g., the dead-time period, switching times and voltage drops of switching device) vary with the operating conditions and they difficult to be measured by instruments. Thus, the parameter estimates could be biased due to the effect of nonlinearity of VSI such as switch voltage drop, switching delay and dead zone response [14]. To achieve accurate estimation, the influence of VSI nonlinearity has to be considered; in other words, it is necessary to take into consideration of both the VSI and machine. Additionally, the parameters of the PMSM system are inherently dependent on each other, and this is a big challenge for most conventional parameter estimation methods.

More recently, a particle swarm optimization (PSO) algorithm was introduced for the estimation of parameter electrical machines including induction machine and PMSM machine [15]-[20]. The PSO algorithm is a nature-inspired algorithm with several advantages such as its self-tuning decoupling and fast convergence speed in dealing with multivariate coupling system parameter optimization problems [15]. A PSO combing least mean squares (LMS) method was proposed to identify the parameters of an induction motor in [16]. In [18], a co-evolution based parameter estimator was developed to estimate the multi-parameters of PMSM by combining multiple PSO and artificial immune system (AIS). However, the computational load of this method is heavy. A parallel implementation of co-evolutionary immune PSO on GPU is proposed to accelerate the computation of parameter estimation and temperature monitoring in PMSM [19], for which the estimation accuracy and time consuming of the parameter estimates were greatly improved by combining PSO with a parallel computing technology. Nevertheless, the existing PSO-based parameter estimators of PMSM are based on the basic dq-axis equation and do not consider the VSI nonlinearity. A dynamic PSO embed with variable exploration vector and Gaussian-distribution based dynamic opposition-based learning operator is proposed for the estimation of machine parameters and voltage-source-inverter (VSI) nonlinearities in PMSM [20]. The development of a high performance PSO for the estimation of PMSM multi-parameters, together with the VSI nonlinearity is still highly demanded.

In order to achieve better estimates for PMSM parameters, two important issues need to be solved when applying PSO algorithms. Firstly, the dynamic performance of the PSO need to be improved as the swarms are easily clustering together and losing their diversity in the later stage of evolution. Secondly, PSO would be time demanding if a large population size involves in the evolution and therefore some massively parallel devices may be required to accelerate the calculating speed. To overcome these problems, the labor division and cooperation mechanism ubiquitously existing in the biological world, together with the immune receptor editing mechanism in AIS, can be used to improve the dynamic performance of PSO during the search process. The time consuming problem can be solved by using Graphic processing units (GPUs), due to its massively parallel computing ability with hundreds of threads and low hardware cost [21].

This study aims to achieve better performance in PMSM parameters estimation using an accurate parameter estimation model where the effect of VSI nonlinearity is considered. A fast dynamic particles swarm optimization algorithm using immune receptor editing combined GPU acceleration technology for PMSM parameter optimization (called G-DPSO-RE) is proposed. The main contributions and main advantages can be summarized as follows:
1) An accurate parameter estimation model of surface permanent magnet synchronous machines (SPMSM) is established by taking into account voltage-source-inverter (VSI) nonlinearity. A labor division based dynamic particle swarm optimization (DPSO) algorithm combined with a receptor editing (RE) strategy is designed to explore the optimal values of parameter estimator.
2) High-performance computing ability of GPU is fully utilized to speed up parameter estimation procedure. It can promote the practical application and real-time response of PSO as it takes full advantage of the inherent parallelism of population-based intelligent computing techniques.

The remainder of this paper is organized as follows. In section II, an accurate parameter estimation model is established. In section III, the G-DPSO-RE algorithm for PMSM parameter estimation is proposed, where the principle, mathematical model and implementation procedure of the algorithm are addressed in details. Experimental results and analysis are given in section IV. Finally, conclusions are summarized in section V.

II. PMSM MODEL AND DESIGN OF PARAMETER ESTIMATION MODEL

A. PMSM Model

The mathematical model of the PMSM in dq-axis voltage
The equation is given as

\[
\begin{align*}
\dot{u}_d &= R_i d + L_d \frac{di_d}{dt} - L_q \omega i_q \\
\dot{u}_q &= R_i q + L_q \frac{di_q}{dt} + L_d \omega i_d + \psi_m \omega
\end{align*}
\]  

(1)

where \(\omega\) is the electrical angular velocity, \(u_d, u_q, i_d\) and \(i_q\) are \(d\) \& \(q\) axis stator voltage and current. The elements of the parameter set \(\{R, L_d, L_q, \psi_m\}\) are the motor winding resistance, magnet flux, \(d\)-axis and \(q\)-axis inductances, respectively, which are usually unknown to the users. Note that the estimated resistance \(R\), as a lumped circuit resistance, includes two parts, namely, the ON-state slope resistances of the active switch and freewheeling diode in inverter and terminal wire resistance. At steady state the equation (1) can be discretized as follow.

\[
\begin{align*}
\dot{u}_d(k) &= R_i d(k) - L_q \omega(k) i_q(k) \\
\dot{u}_q(k) &= R_i q(k) + L_q \omega(k) i_d(k) + \psi_m \omega(k)
\end{align*}
\]  

(2)

In a PMSM vector control system, the voltages used for the PMSM parameter estimation are usually measured from the output voltage of the current controllers, and the terminal voltages of PMSM are PWM pulses from VSI which are difficult to measure directly [22]-[24]. The two output voltages, denoted by \(u_d^*, u_q^*\), are shown in Fig.1. Note that there exists an error between the reference voltage of the controller and the actual output voltage of the VSI due to the nonlinearity of VSI, so it is essential to estimate VSI nonlinearity.

Taking into account the influence of VSI nonlinearity, the model of PMSM and VSI as a whole, for surface-mounted PMSM, \(d\)-axis inductance is regarded as equal to \(q\)-axis inductance, that is \(L_d = L_q = L\) (2) can be rewritten as

\[
\begin{align*}
\dot{u}_d^*(k) + D_d(k)V_{\text{dead}} &= R_i d(k) - L_o o(k) i_q(k) \\
\dot{u}_q^*(k) + D_q(k)V_{\text{dead}} &= R_i q(k) + L_o o(k) i_d(k) + \psi_m \omega(k)
\end{align*}
\]  

(3a)

\[
\begin{align*}
\dot{u}_d^*(k) + D_d(k)V_{\text{dead}} &= R_i d(k) - L_o o(k) i_q(k) \\
\dot{u}_q^*(k) + D_q(k)V_{\text{dead}} &= R_i q(k) + L_o o(k) i_d(k) + \psi_m \omega(k)
\end{align*}
\]  

(3b)

where \(D_d\) and \(D_q\) are the function of rotor position [13]. In (3) \(L, R, \psi_m\) and \(V_{\text{dead}}\) are the parameters to be estimated. The variable \(V_{\text{dead}}\) is the distorted voltage due to VSI nonlinearity, and can be represented as

\[
V_{\text{dead}} = \frac{T_{\text{dead}} + T_{\text{on}} - T_{\text{off}}}{Ts} (V_{dc} - V_{sat} + V_d) + \frac{V_{sat} + V_d}{2}
\]  

(4)

where \(T_{\text{dead}}\) is the dead-time period of the switching device, \(T_{\text{on}}\) and \(T_{\text{off}}\) are turn-on and turn-off times of the switching device, \(V_{dc}\) is measured real-time DC bus voltage, \(V_{sat}\) and \(V_d\) are the saturation voltage drop of the active switch and the forward voltage drop of the freewheeling diode, \(T_s\) is the switching period. It can be seen that if variable \(V_{\text{dead}}\) is ignored, the estimation results may also be influenced by the nonzero VSI nonlinearity terms (\(D_d V_{\text{dead}}\) and \(D_q V_{\text{dead}}\)), and this may introduce an error into the estimation of the PMSM parameters.

B. The Design of Estimation Model based on Parameter Optimization

![Fig.2. Schematic diagrams of estimation and mathematical model.](image)

Apparently, the rank of equation (3) \(<3\), while the number of unknown parameters is four, thus the equation (3) is rank deficient, the four parameters in (3) are not be identifiable and an estimate to converge to suboptimal. To solve this problem, a full rank reference model should be constructed if all these parameters need to be estimated simultaneously at steady state. Generally, \(d\)-axis current injection method is employed to obtain more state equations due to the variation of \(d\)-axis current. The parameters of machine can be assumed to be constant as the duration of injected pulse current is very short due to mechanical inertia and fast response of current loop PI controller. In this case, the influence of injecting a short pulse of \(i_d\) on output torque and speed can be negligible. Thus, the two sets of steady state data (Data0 and Data1) can be used together for the estimation machine parameters and VSI nonlinearity simultaneously modeling. An illustration is given in Fig.2, where \(i_d\) = 0(A) during normal operation for the decoupling the flux and torque control of SPMSM, and a very short time of \(i_d\) \(\neq\) 0(A) is injected to obtain another \(dq\)-axis voltage equation model. Two groups of equations at \(i_d = i_{d0}\) and \(i_d = i_{d1}\) are obtained as

\[
\begin{align*}
\dot{u}_d(k) &= -L_o o(k) i_q(k) - D_d o(k) V_{\text{dead}} \\
\dot{u}_q(k) &= R_i q(k) + \psi_m \omega(k) - D_q o(k) V_{\text{dead}} \\
\dot{u}_d(k) &= R_i d(k) - L_o o(k) i_q(k) - D_d o(k) V_{\text{dead}} \\
\dot{u}_q(k) &= R_i q(k) + L_o o(k) i_d(k) + \psi_m \omega(k) - D_q o(k) V_{\text{dead}}
\end{align*}
\]  

(5)
The parameter identification can be addressed as an optimization problem where the system response to a known input is used to find the unknown parameter values of a model. Based on (5), the cost function for the estimating parameter set \((R, L, \theta, V_{\text{dead}})\) is as
\[
f(p) = \frac{1}{n} \sum_{k=1}^{n} \left[ w_1 \left[ \mu_{\theta_0}^k(k) - \hat{\mu}_{\theta_0}(k) \right] + w_2 \left[ \mu_{\theta_0}^k(k) - \hat{\mu}_{\theta_0}(k) \right] \right] + w_3 \left[ \mu_{\theta_0}^k(k) - \hat{\mu}_{\theta_0}(k) \right] \tag{6}
\]
where \(w_1, w_2, w_3, w_4\) are weight coefficients, satisfying \(w_1 = w_2 = w_3 = w_4 = 1\). \(\hat{\mu}_\theta\) and \(\mu_\theta\) indicate the estimated voltages in \(dq\)-axis computed by the measured currents and the estimated parameters.

### III. GPU-accelerated Parallel Dynamic PSO with Receptor Editing

#### A. Principle of Basic PSO Algorithm

PSO [15] is a swarm-based intelligent optimization algorithm inspired by the ideas of simulating behaviors of birds flocking foraging. Assuming that each particle \(i\) in a \(d\)-dimensional solution space is composed of two vectors, which are the velocity vector \(V_i = \{V_{i1}, V_{i2}, ..., V_{id}\}\) and the position vector \(X_i = \{X_{i1}, X_{i2}, ..., X_{id}\}\), the search procedure can be formulated as
\[
V_{id}(t+1) = \phi V_{id} + c_1 \cdot \text{rand}_1([\text{Pbest}_{id}(t) - X_{id}(t)]) + c_2 \cdot \text{rand}_2([\text{gBest}_{id}(t) - X_{id}(t)]) \tag{7}
\]
\[
X_{id}(t+1) = X_{id}(t) + V_{id}(t+1) \tag{8}
\]
where \(c_1\) and \(c_2\) are the acceleration coefficients, \(\phi\) is the inertia weight factor decreasing linearly, \(\text{rand}_1\) and \(\text{rand}_2\) are random numbers in the interval \([0,1]\), respectively. \(\text{Pbest}_{id}\) represents the best position with the best fitness found by \(i\)-th particle up to now and \(\text{gBest}_{id}\) is the best position found among the entire population.

#### B. The proposed G-DPSO-RE Algorithm for PMSM parameter estimation

As mentioned in Section II, the objective function is multimodal and therefore requires that the optimization method should have a good global search capability. The existing static optimization methods may easily get trapped in some local minima. To effectively solve the multimodal optimization problem (6), a fast dynamic parameter tracking approach is indeed developed to explore the optimal search ability for parameters estimator of the PMSM. Biological inspired PSO, combined with parallel computing technology, can meet such a requirement, since PSO has the intrinsic ability to automatically track the dynamic objective and the GPU acceleration technology can reduce the computation time with significantly low cost. The proposed G-DPSO-RE method involves three key strategies.

1) Firstly, three novel schemes are developed to enhance the dynamic performance of PSO based on a division of labor concept in colony society. One of the designs is to divide the group into two parts dynamically according to evolution factor during the evolution process and two novel velocity updating equations are investigated for two different state particles respectively.
2) Secondly, a novel strategy is to utilize RE using chaotic logistic to overcome the blindness in action of \(g\text{Best} \) stochastic evolution and make it drift from the local minima.
3) Thirdly, GPU parallel computing technique is used to speed up the search process and then an optimized parallel accelerated G-DPSO-RE algorithm using CUDA (Compute Unified Device Architecture, is a GPU programming hardware and software architecture developed by NVIDIA Corporation).

The general steps of G-DPSO-RE for PMSM parameter estimation are stated as follows.

Algorithm: G-DPSO-RE algorithm for parameter estimation

- **Step1:** Initialize population, parameters and GPU device environment, signal sampling and recording as in Fig 1.
- **Step2:** Load data \((u_n,u_{\text{in}},i_d,i_q,\omega)\) are used to drive the estimator model.
- **Step3:** Launch parallel functions kernels in CUDA, transfer data from CPU to GPU.
- **Step4:** For \(i=1\) to \(N\) \((1 \leq i \leq N, N\) is the number of particles
  - Calculating an “evolutionary factor” \(E(i)\)
    - IF \(E(i) \geq \eta\): The particle, goto State (1) - exploitation
      - update particle, velocity \((V_i)\) utilizing equation (10)
      - update position \((X_i)\) utilizing equation (11)
    - IF \(E(i) < \eta\): The particle, goto State (2) - exploration
      - update particle, velocity utilizing equation (12)
      - update position utilizing equation (13)
  - Computing the parameter estimator model
  - Evaluate the fitness value \((\text{Fit}(X_i))\) of particle, using equation (6);
    - IF \(\text{Fit}(X_i) < \text{Fit}(\text{Pbest})\) then Update Pbest, \(\text{Pbest} \leftarrow X_i\)
    - IF \(\text{Fit}(\text{Pbest}) < \text{Fit}(g\text{Best})\) Then Update gBest \((g\text{Best} \leftarrow \text{Pbest})\)
  - end for
- **Step5:** Immune receptor editing operator for \(g\text{Best} \) particle
  - by utilizing the equations (16)-(18) and the Fig. 4.
- **Step6:** If a termination condition is met, or else, go to step3.
- **Step7:** Transfer result back to CPU and output.
- **Step8:** Record the optimal machine parameters \((R, L, \theta, V_{\text{dead}})\).
In order to achieve the automatic control of population dynamic division, a real-time evolutionary state estimation procedure is performed to identify the two evolutionary states via computing an “evolutionary factor” of each individual. Therefore, in this mechanism the population evolutionary information in every generation has been taken into account, and details are given below.

1) Denote the best fitness of the i-th particle at the t-th generation by $Fit_{i, best}^t$, compute an “evolutionary factor” $E(i)$.

$$E(i) = \frac{Fit_{i, best}^t (t+1) - Fit_{i, best}^t (t)}{Fit_{i, best}^t (t) - Fit_{i, best}^t (t-1)} + \alpha$$

where $t$ is current generation, $T$ is the total generation, $\alpha$ is a smooth coefficient. Let $\eta = e^{-t/T}$ be a function measuring the convergence rate of the evolutionary factor $E(i)$. If $E(i) \geq \eta$, then the particle $i$ should converge to the exploitation state and carry out a fine search. Otherwise, if $E(i) < \eta$, then the particle $i$ should shift to the exploration state and make a broader exploration of the solution space. Therefore, the designed dynamic evolution model makes particles more flexible in exploration and exploitation and is suitable to solve dynamic problems. Thus, the size of each subpopulation can be dynamically adjusted based on individual’s evolutionary status.

2) State (i) - exploitation: In this exploitation state, we use the following velocity updating equation

$$V_{id} (t+1) = c_1 * rand_1() (P_{best, id}(t) - X_{id}(t))$$

$$+ c_2 * rand_2() (gBest_{2d}(t) - X_{id}(t))$$

$$X_{id}(t+1) = X_{id}(t) + V_{id}(t+1)$$

where $gBest_{2d}$ is the best position discovered in the entire particles under exploration state. The symbol $\phi$ is the randomly selected the exploitation population and $\phi = \left\lceil rand * K \right\rceil$, $k$ is total exploitation population size. The velocity updating equation of exploitation state indicates that all of exploitation particles' historical best information is used to update a particle’s velocity. So, the elite particles in exploitation state can focus on the best-known solution region and search the optimal goal via the cooperative behavior of the entire sub-swarms.

3) State (ii) - exploration: In this exploitation state, we use the following velocity updating equation:

$$V_{jd} (t+1) = c_1 * rand_1() (P_{best, jd}(t) - X_{jd}(t))$$

$$+ c_2 * rand_2() (gBest_{2d}(t) - X_{jd}(t))$$

$$+(X_{max} - X_{min}) \cdot Gauss$$

$$X_{jd}(t+1) = X_{jd}(t) + V_{jd}(t+1)$$

where $gBest_{2d}$ is the best position discovered in the entire particles under exploitation state. In this velocity updating equation, the old velocity $\phi V_{id}$ component is omitted, that means the potential local information is forgotten. And also, the term $(X_{max} - X_{min}) \cdot Gauss$ is added to provide a broader exploration of the solution space for the j-th particle. The symbol Gauss is the density function with a zero mean $u$ and a standard deviation (SD)$\sigma$, which can be expressed as:

$$Gauss(x) = \frac{1}{\sqrt{2\pi}} \exp(-\frac{(x-u)^2}{2\sigma^2})$$

$$\sigma = \sigma_{max} - (\sigma_{max} - \sigma_{min}) \cdot \frac{t}{T}$$

where $\sigma_{max}$ and $\sigma_{min}$ are the upper and lower bounds of $\sigma$. As fixed $\sigma_{max} = 1, \sigma_{min} = 0.01$. From the above discussion, it can be expected that the dynamic PSO scheme can make equilibrium between extensive searching and accurate searching.

D. Chaotic Logistic-Based Receptor Editing for gBest

The gBest particles usually used as the exemplars to lead the flying direction of other particles among the swarms. It needs a reinforcement learning mechanism to improve the gBest search performance. It was discovered that B-lymphocytes in natural immune system with low quality will undergo a molecular selection and develop completely new ones by gene recombination or shift, which called immune receptor editing theory[27].The receptor editing mechanism can provide wider exploration of the solution space and help gBest push itself out to a potentially better region in unknown environment. If there another better region is found, then the rest of the swarm will follow the leader to jump out and converge to the better region. Nonlinear chaotic logistic series possesses the characteristics of randomness, ergodicity and so on, which can simulate the operations of gene drift or recombination in immune receptor editing. The receptor editing operator is defined as:

$$gBest_{d} = gBest_{d} + [(rd > P_m)] * (X_{d \max} - X_{d \min}) * x(t+1)$$

$$- [(rd \leq P_m)] * (X_{d \max} - X_{d \min}) * x(t+1)$$

(16)
where \( r_d \) is a randomly generated number, and \( P_m \) is set to be 0.5, the search range \([x_{\text{max}}, x_{\text{min}}]\) is the upper bound and lower bound respective. The term \( x(t+1) \) is chaotic logistic sequence function:

\[
x(t + 1) = u x(t) (1 - x(t))
\]

where control parameters \( u \in N \). The sequence (18) can exhibit chaotic behaviors when its initial values on \([0, 1]\) except 0, 0.25, 0.50, 0.75, and 1.0 [28]. Thus, chaotic-logistic-based receptor editing can be viewed as a refinement mechanism, which can provides a broader exploration of the solution space for the \( gBest \) particle and can lead it to the global optimum.

### E. Parallelization Implementation on GPU

Graphic processing unit (GPU) possesses an obvious advantage over CPU in terms of numerical processing ability, multithread instruction unit, and memory bandwidth, whereas it has a low cost and small power consumption, which can greatly reduce the required computing times. In order to speed up parameter estimation procedure, the proposed G-DPSO-RE algorithm is implemented in the GPU devices through the CUDA program. Both CPU and GPU are conducting heterogeneous collaborative computation where the GPU is carry out numeric parallel processing while CPU is in charge of serial computing such as logic and transaction processing.

Note that in the work the entire swarm is run at one block of GPU structure and each particle is run at one thread, as illustrated in Fig.4. The populations and related parameters are generated on CPU and allocated to a grid with one dimension of blocks at GPU. So, the proposed parameters estimation method can be speeded up significantly by GPU.

### IV. EXPERIMENTAL RESULTS AND ANALYSIS

#### A. Hardware Control System and Software Platform

![Fig. 5. Schematic diagram of identification system and waveforms of sampled operation data. (a) The schematic diagram hardware and software platform framework (b) Sampled of \( dq \)-axis current. (c) sampled of voltage and electrical angular speed.](image)

![Fig. 4. The G-DPSO-RE is parallel implementation on GPU](image)

### TABLE I

<table>
<thead>
<tr>
<th>DESIGN PARAMETERS AND SPECIFICATION OF PMSM</th>
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<tbody>
<tr>
<td>Rated speed</td>
</tr>
<tr>
<td>DC link voltage</td>
</tr>
<tr>
<td>Nominal terminal wire resistance</td>
</tr>
<tr>
<td>Nominal self inductance</td>
</tr>
<tr>
<td>Nominal mutual inductance</td>
</tr>
<tr>
<td>Nominal ( d )-axis inductance</td>
</tr>
<tr>
<td>Nominal ( q )-axis inductance</td>
</tr>
<tr>
<td>Nominal amplitude of flux induced by magnets</td>
</tr>
<tr>
<td>Number of pole pairs</td>
</tr>
<tr>
<td>Nominal phase resistance ((T=25^\circ C))</td>
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<tr>
<td>Inertia</td>
</tr>
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</table>
To perform our experiment, the schematic of the parameter estimation system is depicted in Fig. 5(a), whose design parameters are shown in Table 1, where a permanent magnet synchronous motor prototype and DSP vector control hardware platform are used as the experimental facility. The waveforms of measured dq-axis currents/voltages and electrical angular speeds of PMSM such as normal temperature condition are shown in Fig. 5 (b)-(c). The current signals are obtained from the Hall transducers and then sampled by the DSP. The DC link is connected with the DC power source whose output is fixed to 36V. The sampling period is set to 83.3 µs. The data used for parameters estimation data modeling come from the DSP via serial protocol communication network and recorded in memory. After this, the parameter estimator is computed iteratively in host computer by the proposed G-DPSO-RE using visual studio 2012 software. For a large-scale engineering application, there is a need to process a large amount of operating condition data and control signals, so it needs large computing and mass storage, for such a case the processing of parameter estimation can still be done in a PC, equipped with graphic processing units (GPUs), which has massively parallel computing ability with hundreds of threads and low hardware cost. The work can be done by collaborative PC with inverter controller: the high computational task and massive storage can be done by PC and the results can be sent to inverter controller for controller design.

A number of hybrid PSOs are used for a comparison purpose with the proposed G-DPSO-RE, including HGAPSO (hybrid PSO with genetic algorithm) [29], HPSOWM (hybrid PSO with Wavelet Mutation) [30], CLPSO (comprehensive learning PSO) [31], A-CLPSO (An improved comprehensive learning PSO) [32] and APSO (adaptive Particle Swarm Optimization) [33]. To assess the performance of parameter estimation, a statistical analysis is performed in terms of the mean results, standard deviation and the t-test value. The basic settings of these PSOs are as follows: the maximum iteration is 300 and the number of runs is 15. All hybrid PSOs are operated on the same platform with the same objective function and PMSM hardware. All experiments are carried out on the same computer with AMD Athlon(tm) II X4 555, four-core processors, RAM 4.0GB and GPU of NVIDIA GeForce GTX560TI equipped with 512 cores.

B. Parameter Estimation under Normal Temperature Condition

Table II presents the set of the parameters which are applied in the HGAPSO, HPSOWM, CLPSO, A-CLPSO, APSO, G-DPSO-RE algorithms for PMSM parameter estimation using data measured from normal temperature environment, and the convergence of different PSOs are shown in Fig. 6 from which it is clear that the proposed G-DPSO-RE shows the best performance in terms of mean, standard deviations and t-values among those seven methods. Furthermore, all the t-values are higher than 9, which imply that the G-DPSO-RE has significantly better solution performance than other hybrid PSOs (the confidence level is 98%). As can be seen from Fig. 6, DPSO-RE converges to the optimum after about 60 generations of evolution whereas other hybrid PSOs shows poor convergence performance. Moreover, as shown in Table II, the execution time of G-DPSO-RE is shorter than the other seven methods.

As demonstrated in Table II and Fig. 8 (a)-(c), the estimated winding resistance (0.371Ω) by G-DPSO-RE is quite close to its measured value (0.373Ω (0.33Ω+0.043Ω)) under normal temperature condition. In addition, the estimated flux linkage ψ_m (78.36mWb) by G-DPSO-RE is quite close to its nominal value (77.6mWb), the estimated dq-axis inductance (3.474mH) is also consistent well with the nominal value on manual (3.24mH). As shown in Fig. 7, the value of VSI disturbance voltage V_{dead} can be estimated along with other machine parameters based on the proposed estimator model. Although the accurate value of V_{dead} cannot be acquired, it can be seen from Table II and III that the estimation results of the machine parameters (i.e. resistance (R), rotor flux linkage (ψ_m)) are of the highest estimation accuracy, and thus it can be expected that the estimated value of V_{dead} should be close to true value.

Fig. 6. The fitness convergence curve of six PSOs on PMSM parameter identification under normal temperature condition.

Fig. 7. The estimated VSI distorted voltage under normal temperature condition

In all, the proposed G-DPSO-RE is of high accuracy in parameter estimation under normal temperature condition though there is a slight difference between the estimated and nominal values of (R, L, ψ_m) due to nonlinearity on load condition. It can also be observed from Table I and Fig. 8(a)-(c) that the proposed G-DPSO-RE produced more precise parameter estimates for motor resistance, dq-axis inductances and the rotor flux, and the estimates converge to their desired values rapidly. The proposed estimator has a global convergence performance by combining the labor division cooperation mechanism inspired by the biological world and immune receptor editing mechanism in AIS. The
results confirm that the cost function previously defined is related to the reality problems with local minima, and the poor performance of the identification method will progress from convergence to localization.

Moreover, as is shown in Table II, in terms of time-consuming, it requires 23.85s, 36.24s, 18.30s, 18.17s, and 12.47s for HGAPSO, HPSOWM, CLPSO, A-CLPSO and APSO, respectively. However, the computation time of G-DPSO-RE is only 6.97 s, which is smaller than all the comparative PSO methods. This demonstrates that the potential of the high-performance computing ability of GPU is well exploited to speed up the parameter estimation procedure. It can promote the real-time response of the proposed G-DPSO-RE as it takes advantage of the inherent parallelism of population-based intelligent computing techniques.

As mentioned above, the proposed G-DPSO-RE for the estimation of PMSM parameters can converge to the global optimal solution when solving dynamically nonlinear PMSM parameters estimation problem.

### TABLE II.
RESULT COMPARISONS AMONG SIX PSOS ON PMSM PARAMETER IDENTIFICATION WITH NORMAL TEMPERATURE

<table>
<thead>
<tr>
<th>Estimated Parameters</th>
<th>HGAPSO</th>
<th>HPSOWM</th>
<th>CLPSO</th>
<th>A-CLPSO</th>
<th>APSO</th>
<th>G-DPSO-RE</th>
</tr>
</thead>
<tbody>
<tr>
<td>$R (\Omega)$</td>
<td>0.359</td>
<td>0.367</td>
<td>0.333</td>
<td>0.321</td>
<td>0.369</td>
<td>0.371</td>
</tr>
<tr>
<td>$\psi_m (mWb)$</td>
<td>78.23</td>
<td>77.69</td>
<td>78.62</td>
<td>78.51</td>
<td>79.62</td>
<td>78.36</td>
</tr>
<tr>
<td>$L (mH)$</td>
<td>3.528</td>
<td>3.589</td>
<td>3.278</td>
<td>3.133</td>
<td>3.755</td>
<td>3.474</td>
</tr>
<tr>
<td>$V_{dead}(V)$</td>
<td>-0.286</td>
<td>-0.211</td>
<td>-0.116</td>
<td>-0.139</td>
<td>-0.109</td>
<td>-0.078</td>
</tr>
<tr>
<td>Fitness</td>
<td>Mean</td>
<td>1.23</td>
<td>1.90</td>
<td>2.072</td>
<td>1.74</td>
<td>2.12</td>
</tr>
<tr>
<td></td>
<td>Std.dev</td>
<td>0.259</td>
<td>0.123</td>
<td>0.553</td>
<td>0.608</td>
<td>0.588</td>
</tr>
<tr>
<td></td>
<td>Time(s)</td>
<td>23.85</td>
<td>36.24</td>
<td>18.30</td>
<td>18.17</td>
<td>12.47</td>
</tr>
<tr>
<td></td>
<td>t-value</td>
<td>10.04</td>
<td>12.11</td>
<td>15.51</td>
<td>10.29</td>
<td>15.17</td>
</tr>
</tbody>
</table>

Fig. 8. Identified parameters (a) winding resistance. (b) rotor flux linkage (c) $d$-axis inductance.

C. Parameter Estimation under Temperature Variation Condition

Temperature is the main indicator for the reliable operation of PMSM, the variation of temperature can change the machine physical parameters. In order to evaluate the dynamic performance of the proposed method for tracking the change of parameters under temperature variation conditions, a heater is used to heat the prototype PMSM, and experiments are carried out. Firstly, continuously heating the PMSM for 20 minutes and then recording experimental data for the estimation of the machine parameters ($t=20$ minutes).

The comparisons of the performance for different PSOs are shown in Table III, Fig.9, Fig.10,and Fig.11. The convergence curves of different PSOs are shown in Fig.9. From Table III, it is obvious that G-DPSO-RE produces the best performance in terms of mean, standard deviations and t-values. Fig.9 further shows that the G-DPSO-RE has a fast convergence speed compared to other hybrid PSOs.

Additionally, the stability of the G-DPSO-RE is better than other hybrid PSOs. Meanwhile, as can be seen from Table III and Fig.11, the estimated winding resistance $R$, $dq$-axis inductance $L$ and rotor flux linkage $\psi_m$ vary with the changing temperatures. For example, the estimated winding resistance value varies from 0.371 (\(\Omega\)) to 0.446 (\(\Omega\)) after 20 minutes heating due to the effects of the thermal metal, the estimated

Fig. 9. The fitness convergence curve of six PSOs on PMSM parameter identification under variation temperature condition.
rotor flux linkage decreased from 78.36 (mWb) to 76.81 (mWb) after 20 minutes heating, the abrupt drop in the estimated rotor flux linkage after 20 minute heating can be explained by the fact that the residual flux density of the PM heating can be explained by the fact that the VSI distorted voltage after 20 minute heating. This phenomenon can be explained by the fact that the VSI nonlinearity is also influenced by the temperature variation.

From above results and analysis, it indicates that G-DPSO-RE has a good dynamic tracking performance. Hence, the G-DPSO-RE is significantly better and statistically more robust than other listed hybrid PSOs in terms of global search capacity and local search precision in our experiments.

D. Speedup Achieved by GPU Parallel Implementation
The speed-up ratio is defined as $SUR = \frac{T_s}{T_p}$, where $T_s$ and $T_p$ are the execution runs of the serial and parallel algorithms respectively. In this work speedup ratio is used to evaluate the efficiency of our proposed method implemented on different multi-core architecture. A GTX560TI GPU and multi-core CPU systems (range from one core to four cores) are compared in terms of computation speedup when applied to the estimation of PMSM parameters. The results are shown in Table IV and Fig.12, where the symbol CPU-1, CPU-2, CPU-3, and CPU-4 are means CPU with one core, two cores, three cores, and four cores respectively.

The results show that the execution time of the G-DPSO-RE reduces greatly when it runs on increasing multi-core CPU. For example, it requires 64.01s, 52.34s, 38.93s and 24.19s for running with one core, two cores, three cores and four cores CPU under the normal temperature condition, respectively. Whereas, the average time required for GPU is only 6.97s. The computation of
optimal solution is accelerated by 9.18× in comparison of a sequential execution on CPU through exploiting the massively parallel architecture of GPUs. This fact shows that the speed and efficiency of the proposed parameter estimation method has been remarkably improved by GPU parallel execution. There are two main reasons behind this. Firstly, the computing speed of GPU with hundreds of threads is much faster than that of CPUs. Secondly, the proposed estimator involves mass intensive computing including data and program because of the G-DPSO-RE with intrinsic parallel character.

![Fig 12](image)

**Fig. 12.** The comparison for SUR of G-DPSO-RE in PMSM parameter estimation parameter using different multi-core architecture using different multi-core architecture.

**E Comparison Between With and Without Considering the VSI Nonlinearity**

In this section, an experimental is conducted to provide a comparison between the results with and without including the effect of VSI nonlinearity. Fig. 13(a)-(c) show the estimated machine parameters (winding resistance, rotor flux linkage and dq-axis inductance) with and without considering the VSI nonlinearity under normal temperature condition using the proposed G-DPSO-RE. The estimated machine parameters without considering the VSI nonlinearity are as follows: the estimated winding resistance \( R \) is 0.453 (\( \Omega \)), the estimated rotor flux linkage \( \psi_m \) is 75.9 (mWb) and the estimated dq-axis inductance \( L \) is 3.433 (mH), while the estimates with considering the VSI nonlinearity are: 0.371 (\( \Omega \)), 78.36 (mWb) and 3.474 (mH), respectively. It is obvious that the estimated values with considering the VSI nonlinearity are different from that without considering the VSI nonlinearity, especially for the estimated winding resistance value and the estimated flux linkage. For example, the estimated winding resistance value (0.453\( \Omega \)) without considering VSI nonlinearity is much larger than that (0.371\( \Omega \)) with considering VSI nonlinearity (with an error of 0.453-0.371)/0.371≈22\%. The estimated rotor flux linkage value (75.95 mWb), without considering VSI nonlinearity, is obviously smaller than 78.36 (mWb) which was estimated with considering VSI nonlinearity, with an error of 78.36-75.95)/78.36≈3\%.

The differences between the parameter estimates are are mainly accounted for by effect of the VSI nonlinear disturbance voltage (i.e., \( V_{\text{dead}}-D_d \) and \( V_{\text{dead}}-D_q \) in (3a) and (3b)) which results in an increase in the estimated winding resistance. From the experiment, the distort voltage \( V_{\text{dead}} \) is about 0.1 V, the two terms \( D_q V_{\text{dead}} \) (about 0.4 V) and \( D_d V_{\text{dead}} \) (about 0.2 V) could introduce an error into the estimation of the PMSM parameters. This can be analyzed by using the typical electrical parameters in Table I and equation (3b). Note that \( R_{iq} \) is about 1.3 V, \( \omega_\psi \) is about 12 V, and \( D_q V_{\text{dead}}/R_{iq} \approx 30\% \), \( D_q V_{\text{dead}}/\omega_\psi \approx 3\% \), so, after Clarke and Park transforms, the dq-axis voltage will change because \( D_q V_{\text{dead}} \) can significantly affect the winding resistance and flux linkage estimation significantly.

The results show that the proposed parameter estimation model with considering the effect of VSI nonlinearity can improve the accuracy for machine parameter estimation.

![Fig 13](image)

**Fig 13.** The comparison of the identified parameters between with considering VSI nonlinearity and without considering VSI nonlinearity under normal temperature condition using the proposed G-DPSO-RE (a) winding resistance. (b) rotor flux linkage (c) dq-axis inductance.

**V. CONCLUSION**

In this study, an accurate estimation model of combining the SPMSM parameters with VSI nonlinearity is established. A labor-division based dynamic PSO combined immune receptor editing strategy is designed for dynamic optimization and parallel implementation on GPU to accelerate the convergence process for parameter estimation. The computational efficiency of the parameter estimation procedure is greatly improved by the GPU parallel computing technique. The proposed parameter optimization method can be used to collectively estimate several parameters including...
the resistance, inductance, rotor flux along with VSI disturbance voltage with no expensive equipment. The influence of the VSI nonlinearity on the accuracy of the parameter estimation is also analyzed. In comparison with other PSO algorithms, the proposed estimation algorithm is relatively more complicated and the implementation of GPU techniques needs some special knowledge and programming skills, and this may be a major challenge for most of control or electrical engineers. But with the development of computer technology, it can be expected that this estimation algorithm can become easier for commercial PMSM drives. The proposed parameter estimation model focuses on steady state operation of machines and may not be suitable for other complex cases, for example for machine operating under time-varying operating conditions. This is a limitation of the proposed method. In our future work, we will investigate a new dynamic parameter estimation model for machine parameter estimation under dynamic operating state including the consideration of variation in the load disturbance and speed.

References


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