A basic probability assignment methodology for unsupervised wireless intrusion detection

This item was submitted to Loughborough University's Institutional Repository by the/an author.

Citation: GHAFIR, I. ...et al., 2018. A basic probability assignment methodology for unsupervised wireless intrusion detection. IEEE Access, 6, pp.40008-40023.

Additional Information:

- This is an Open Access Article. It is published by IEEE under the Creative Commons Attribution 3.0 Unported Licence (CC BY). Full details of this licence are available at: http://creativecommons.org/licenses/by/3.0/

Metadata Record: https://dspace.lboro.ac.uk/2134/34208

Version: Published

Publisher: Institute of Electrical and Electronics Engineers (IEEE)

Rights: This work is made available according to the conditions of the Creative Commons Attribution 3.0 Unported (CC BY 3.0) licence. Full details of this licence are available at: http://creativecommons.org/licenses/by/3.0/

Please cite the published version.
A Basic Probability Assignment Methodology for Unsupervised Wireless Intrusion Detection

IBRAHIM GHAFIR, KONSTANTINOS G. KYRIAKOPOULOS, FRANCISCO J. APARICIO-NAVARRO, SANGARAPILLAI LAMBOTHARAN, BASIL ASSADHAN, AND HAMAD BINSALLEEH

1Wolfson School of Mechanical, Electrical and Manufacturing Engineering, Loughborough University, Loughborough LE11 3TU, U.K.
3Faculty of Technology, De Montfort University, Leicester LE1 9BH, U.K.
4Department of Electrical Engineering, King Saud University, Riyadh 11421, Saudi Arabia
5Department of Computer Science, Al-Imam Muhammad Ibn Saud Islamic University, Riyadh 11432, Saudi Arabia

Corresponding author: Ibrahim Ghafir (i.ghafir@lboro.ac.uk)

This work was supported in part by the Gulf Science, Innovation and Knowledge Economy Programme of the U.K. Government under UK-Gulf Institutional Link Grant IL 279339985 and in part by the Engineering and Physical Sciences Research Council (EPSRC), U.K., under Grant EP/R006385/1.

ABSTRACT  The broadcast nature of wireless local area networks has made them prone to several types of wireless injection attacks, such as Man-in-the-Middle (MitM) at the physical layer, deauthentication, and rogue access point attacks. The implementation of novel intrusion detection systems (IDSs) is fundamental to provide stronger protection against these wireless injection attacks. Since most attacks manifest themselves through different metrics, current IDSs should leverage a cross-layer approach to help toward improving the detection accuracy. The data fusion technique based on the Dempster–Shafer (D-S) theory has been proven to be an efficient technique to implement the cross-layer metric approach. However, the dynamic generation of the basic probability assignment (BPA) values used by D-S is still an open research problem. In this paper, we propose a novel unsupervised methodology to dynamically generate the BPA values, based on both the Gaussian and exponential probability density functions, the categorical probability mass function, and the local reachability density. Then, D-S is used to fuse the BPA values to classify whether the Wi-Fi frame is normal (i.e., non-malicious) or malicious. The proposed methodology provides 100% true positive rate (TPR) and 4.23% false positive rate (FPR) for the MitM attack and 100% TPR and 2.44% FPR for the deauthentication attack, which confirm the efficiency of the dynamic BPA generation methodology.

INDEX TERMS  Basic probability assignment, data fusion, Dempster-Shafer theory, intrusion detection system, local reachability density, network security, probability density function, wireless injection attacks.

I. INTRODUCTION

Over the last two decades, wireless local area networks, based on the IEEE 802.11 standard protocols (Wi-Fi), have become prevalent. Nowadays, most of the personal devices, laptops and smart phones are equipped with wireless connection capability. Furthermore, since the Internet of Things (IoT) has emerged, the number of devices connected to wireless networks is increasing rapidly [1]. Currently, there are more than 20 billion IoT devices connected to the Internet, and that number is expected to reach 75 billions by 2025 [2]. Due to the ease of deployment, maintenance and low cost, these devices have become ubiquitous. Consequently, securing this type of networks has become a priority.

The broadcast nature of Wi-Fi has made the wireless access open to new forms of cyber-attacks against the IEEE 802.11 standard protocol [3]. Any wireless device within the coverage area of the transmitter is able to intercept the communication channel. This provides an opportunity for attackers to eavesdrop and analyze the network communication. Moreover, the capability to inject malicious information into the wireless communication, and the capacity to impersonate the identity of legitimate network devices, allow an attacker to launch several types of wireless injection attacks, such as Man-in-the-Middle (MitM) at the physical layer [4], de-authentication [5] and rogue access point [6].

Furthermore, Wi-Fi encryption systems, such as WPA2, may fail under specific circumstances in guaranteeing...
Confidentiality, Integrity and Availability (CIA). For instance, in [7], Agarwal et al. describe how the vulnerability Hole 196 can be used to inject a spoofed broadcast/multicast frame in a WPA2 encrypted network. Wi-Fi networks require encryption protocols, as well as intelligent and robust network traffic monitoring mechanisms to defend themselves against attacks targeting CIA.

An Intrusion Detection System (IDS) is a security system designed to detect malicious activities within the network by extracting and analyzing network traffic measurements. Because most cyber-attacks manifest themselves through different metrics, current IDSs should not be based on a single metric, but should leverage a cross-layer metric approach. Hence, the combined use of multiple metrics across various network stack layers can help towards improving the IDS accuracy.

Data fusion techniques aim to integrate information from multiple, usually heterogeneous, data sources to improve the decision making, while decreasing the uncertainty in a knowledge domain. As many researchers have previously demonstrated, IDSs that make use of multiple metrics from the same or different network stack layers, may improve their Detection Rate (DR) while producing lower number of false alarms [8], [9].

The Dempster-Shafer (D-S) Theory of Evidence [10] is a prime data fusion approach that inherently handles knowledge representation and uncertainty reasoning [11]. D-S has been proven to be a powerful and efficient data fusion technique in various network security related fields [12], [13]. However, there are still a number of issues associated with D-S that need to be addressed. In particular, the generation of the Basic Probability Assignment (BPA) values is of fundamental importance.

Although D-S depends directly on the BPA, it does not dictate a specific methodology to derive the belief values. Due to this reason, few of the previously proposed methodologies can dynamically and robustly generate the BPA values to be used during the data fusion process of IDS. Therefore, this issue is still a challenge to be addressed.

In this work, we propose a novel unsupervised methodology to dynamically generate the BPA values, based on a robust and rigorous mathematical framework. The proposed methodology employs both the Gaussian and exponential probability density functions (pdf), the categorical probability mass function (pmf) [14], and the local reachability density (lrd) [15]. It dynamically assigns BPA values for each feature (i.e. metric) extracted from Wi-Fi frames, which appropriately represent the real nature of the data. Then, the D-S fusion is used to fuse the beliefs of each metric in order to classify whether the Wi-Fi frame is normal (i.e. non-malicious) or malicious. The combination of these techniques dynamically assigns belief values depending on the current characteristics of the network traffic, without intervention from an IDS administrator. More importantly, the proposed methodology operates in an unsupervised manner and, therefore, does not require labeled training data.

Secondly, the efficiency of the proposed BPA methodology in an IDS is evaluated for two types of wireless injection attacks using a real network testbed: MitM attack at the physical layer and deauthentication attack. In total, five metrics have been empirically selected from the network traffic to be analyzed by our system in order to identify injection attacks. The various metrics are extracted from different layers of the protocol stack.

Thirdly, our network traffic datasets have been made publicly available in [16], including the ground truth. These datasets have been generated from a real Wi-Fi network deployed at Loughborough University, UK. Given the scarcity of publicly available labeled network traffic datasets, making the data available would benefit the IDS research community.

The main aims of the experiments that we present in this work are summarized as follows:

- To evaluate the efficiency of the proposed methodology in terms of detecting attacks and reducing false alarms.
- To compare the results generated by the proposed methodology using the single-metric and multi-metric configurations.
- To determine best possible combination of metrics for the detection performance.

The remainder of this paper is organized as follows. In Section II, the most relevant previous works are reviewed. Section III provides an overview of the methods and algorithms used in this work. The proposed BPA generation methodology is described in Section IV. Section V presents the network testbed, implementation of attacks, and the datasets for the evaluation of performance. In Section VI, the results are discussed and a performance comparison between single and multi-metric approaches is provided. Finally, conclusions are drawn in Section VII.

II. RELATED WORK

Chen and Venkataramanan [17] present a comparative study between D-S and Bayesian inference as data fusion algorithms, and highlight the benefits of D-S theory. The application of D-S for improving the performance of IDSs is an active research topic. In [18], Chen and Ackelín present an IDS based on D-S. The beliefs, computed from multiple features, are combined to obtain an overall belief on whether the analyzed data corresponds to a malicious event. For each feature, a threshold is defined to generate the BPA related to the feature. However, this approach requires a training phase to determine various thresholds and to compute BPAs. Hence, this system cannot dynamically adjust to the current dynamics of the network traffic.
Xu et al. [11] use Gaussian distribution to construct a reference model for each dataset attribute and each hypothesis of the D-S framework, based on training datasets. The intersection of attributes from each test sample with the normal distribution of each class is used to define a nested BPA structure. However, with this nested approach, several singleton hypotheses may be assigned a null belief value. According to [18], the presence of null beliefs in the D-S fusion process can be a detrimental factor on the fused beliefs, as described by the conflicting belief phenomenon. In our proposed work, the problem of generating null beliefs is avoided by always assigning a non-zero belief value to each hypothesis, and ensuring that the mass functions are positive.

In [13] Fragkiadakis et al. present and evaluate an IDS for detecting Denial-of-Service (DoS) attacks by seeking changes in the signal-to-noise ratio. The value of this single metric is calculated from distinct nodes running two different local algorithms, single threshold and cumulative sum. Based on the collected information, their system generates the BPAs using a linear function. The BPAs are fused with D-S theory. In our work, we fuse multiple metrics across the layer stack.

In [4], we previously proposed a novel BPA methodology tailored to detect wireless injection attacks by adapting to the current characteristics of the network traffic, without intervention from an IDS administrator. The BPA methodology uses two independent statistical approaches based on the Euclidean distance from a defined point of reference, and the density distribution of the analyzed data. Although, it was proven to be an efficient BPA methodology, it can benefit from a new set of methodologies that provide a more rigorous and well-defined mathematical framework.

Other IDSs designed to secure Wi-Fi networks, which do not exploit data fusion techniques, have also been proposed in the literature. A framework that aims to detect DoS attacks at the MAC layer is described in [19]. This framework, which is based on thresholds, is composed of three main algorithms; the first one detects and prevents the masquerading of DoS attacks, the second algorithm mitigates the effect of the DoS attack in the secured resource, the third algorithm detects deauthentication, disassociation and MAC spoofing as part of the DoS attacks. The authors indicate that this framework is efficient in terms of throughput, recovery time and packet resend rates. However, it was evaluated using simulated network traffic only, and no evaluation has been performed using real network traffic.

The work proposed in [20] introduces an open source IDS for IEEE 802.11 networks operating in infrastructure mode. The authors indicate that the system is appropriate for the wireless environment since it does not need to be deployed on all the network nodes. Furthermore, two types of attack can be detected; deauthentication attack and evil twin attack. The detection of both attacks is based on the use of multiple metrics from the network traffic. Although this system achieves a detection accuracy of 90% on average for both deauthentication and evil twin attacks, the False Positive Rate (FPR) is relatively high and can be improved by modifying some characteristics of the detection logic, for instance, by using more indicators.

III. PRELIMINARIES

This section provides an overview of the relevant algorithms used by the proposed methodology, and describes the mathematical framework associated with each algorithm. These are the D-S theory, both Gaussian and exponential pdf, categorical pmf, lrd, k-means clustering, and k-Nearest Neighbors (k-NN).

A. DEMPSTER-SHAFER THEORY

D-S is a mathematical technique used to combine the evidence of information from multiple and heterogeneous sources in order to calculate the overall belief of occurrence of an event. D-S theory starts by defining a frame of discernment \( \Theta = \{\theta_1, \theta_2, \ldots, \theta_n\} \), where \( \theta_i \) are all possible mutually exclusive outcomes of a particular problem domain. Let us consider a problem with a frame of discernment presenting two possible outcomes \( \Theta = \{A, B\} \), then the possible hypotheses for this problem are defined as the power set \( \{A, B, \{A\}, \emptyset\} \subseteq 2^\Theta \). In the case of \( \{A\} \), this subset corresponds to Uncertainty (either A or B). In addition, \( \emptyset \) denotes an empty set. With regards to this work, we want to identify whether the analyzed network traffic is malicious or non-malicious. Therefore, the frame of discernment is comprised of \( A = \text{Attack} \) and \( N = \text{Normal} \).

Each hypothesis is assigned a belief value within the range \([0, 1]\), also known as BPA, through a mass probability function \( m \), which expresses the evidence attributed directly to the hypothesis. This is notated as:

\[
m : 2^\Theta \to [0, 1] \text{ if } \begin{cases} m(\emptyset) = 0 \\ m(H) \geq 0, \quad \forall H \subseteq \Theta \\ \sum_{H \subseteq \Theta} m(H) = 1 \end{cases}
\] (1)

Then, Dempster’s rule of combination is used to calculate the orthogonal sum of the belief values from two different observers, and fuses this information into a single belief. This rule is defined in (2), where \( m_1(H) \) and \( m_2(H) \) are the beliefs in the hypothesis \( H \), from observers 1 and 2, respectively. Similarly, \( X \cap Y = H \) refers to all combinations of evidence which yield \( H \); whereas \( X \cap Y = \emptyset \) refers to the mutually exclusive subsets of the hypothesis \( H \), thus their intersection is an empty set.

\[
m(H) = \frac{\sum_{X \cap Y = H} m_1(X) \cdot m_2(Y)}{1 - \sum_{X \cap Y = \emptyset} m_1(X) \cdot m_2(Y)} \quad \forall H \neq \emptyset
\] (2)

Dempster’s rule allows the combination of evidence from two observers at a time. In order to combine evidence from more observers, Dempster’s rule can be used iteratively. The output of the initial combination process is used as input evidence in the next iteration, along with the evidence of information from a third observer. Dempster’s rule satisfies the associative property, thus the order in which the belief...
values are fused does not affect the final combined belief values. To practically understand how Dempster’s rule of combination is implemented, the reader is referred to a practical example presented in our previous work [4].

B. GAUSSIAN AND EXPONENTIAL PROBABILITY DENSITY FUNCTION

The Gaussian, or normal distribution $N(\mu, \sigma^2)$, is most widely used to represent random variables in many applications. This is because, according to the Central Limit Theorem (CLT), in most cases, when adding new independent variables to a sample space, the added values tend to follow the normal distribution, even if the sample space values are not normally distributed [21]. The pdf of a Gaussian random variable $x$ is given as:

$$f(x | \mu, \sigma^2) = \frac{1}{\sqrt{2\pi}\sigma^2} e^{-\frac{(x-\mu)^2}{2\sigma^2}}$$

(3)

where $\mu$ and $\sigma^2$ are the mean and variance of the distribution, respectively.

A continuous random variable $x$ is said to be exponential distributed if it has the following probability density function:

$$f(x | \lambda) = \begin{cases} \lambda e^{-\lambda x} & \text{for } x \geq 0 \\ 0 & \text{for } x < 0 \end{cases}$$

(4)

where $\lambda > 0$ is the rate of the distribution [22].

C. CATEGORICAL PROBABILITY MASS FUNCTION

The pmf provides the probability that a discrete random variable $x_i$ is equal to a specific value [23]. The categorical distribution is a discrete probability distribution that defines probability of a random variable that can take one of $k$ possible values. For example, Bernoulli distribution has only two, i.e. $k = 2$, possible outcomes for the random variable. The pmf of a categorical random variable is given as:

$$f(x_i | p) = p_i$$

(5)

$$\sum_{i=1}^{k} p_i = 1$$

(6)

where $p = (p_1, \ldots, p_k), p_i$ is the probability of observing the outcome $i$.

D. LOCAL REACHABILITY DENSITY

The $Ird$ is an outlier detection technique based on the density of the data. The density between objects in an observation space is obtained by calculating their relative distances. The relative locality of an object is given by its $k$ nearest neighbors. For the purpose of clustering, objects that have similar density are considered to belong in the same group. However, objects that have lower local density than their neighbors are identified as outliers [15]. Let us assume a test sample $X$ and a set of $k$ nearest neighbors $N_k(X)$ of $X$, the $Ird$ of $X$ is calculated as follows:

$$Ird(X) = \frac{|N_k(X)|}{\sum_{Y \in N_k(X)} rd_k(X, Y)}$$

(7)

where $|N_k(X)|$ is the cardinality of $N_k(X)$, $rd_k(X, Y)$ is the reachability distance of an object $X$ from the $k$ nearest objects $Y \in N_k(X)$, as defined by (8):

$$rd_k(X, Y) = \max\{d(X, N_k(X)), d(Y, X)\}$$

(8)

where $d(X, N_k(X))$ is the distance of the $k$th nearest neighbor of the object $X$, $d(X, Y)$ is the distance between $X$ and each of the objects $Y \in N_k(X)$.

E. k-MEANS CLUSTERING

The $k$-means clustering is a technique used to group the observation space comprising of $n$ samples into $k$ different clusters. This unsupervised learning technique is used when the data is not labeled. Given a $k$ number of clusters, the aim of $k$-means is to cluster each object into one of the $k$ clusters. Let us consider a finite $d$-dimensional feature space $S = C_1 \cup C_2 \cup \ldots \cup C_k = x_n \in \mathbb{R}^d$, where $k$ is the number of clusters $C_i (i = 1, 2, \ldots, k)$, and $n$ is the number of data instances. The $k$-means optimization problem is defined in (9):

$$\min_{C_1 \cup C_2 \cup \ldots \cup C_k} \sum_{i=1}^{k} \sum_{x \in C_i} \left| x - \frac{1}{|C_i|} \sum_{j \in C_i} x_j \right|^2$$

(9)

Although the initial centroids can be chosen randomly, in this work we utilize the algorithm $k$-means++ to pick initial centroids, in order to improve the running time of the algorithm. $k$-means++ selects the first centroid randomly, then the next centroid is chosen based on a probability related to the distance to the first centroid [24]. A simple description of $k$-means clustering algorithm is provided below:

1) The initial $k$ centroids or seeds are randomly selected.
2) The Euclidean distance between each centroid and all data instances is calculated.
3) Each data instance is assigned to the closest centroid forming the clusters.
4) For each cluster, a new centroid is selected based on the average distance between data instances within the cluster.
5) Steps 2-4 are repeated until convergence of centroids.

F. k-NEAREST NEIGHBOURS

$k$-NN is a simple machine learning approach used for pattern recognition, either for classification or regression [25]. The $k$ closest samples to the test object in the feature space are selected as an input, where $k$ is a positive integer. In classification, the $k$-NN process returns a class to which the sample belongs. The decision is based on a voting among the $k$ closest samples to the object according to the Euclidean distance. In regression, the $k$-NN process returns a property value assigned to the sample. This value is based on the average value of the $k$ closest samples values.

In $k$-NN, a weight can be added to the participation of each neighbor. In doing so, the closer samples participate more to the final decision than the farther ones. Usually a weight
of \(1/d\) is assigned to each neighbor, where \(d\) is the distance between the object and the neighbor [26].

IV. PROPOSED BPA METHODOLOGY

This section describes the methodology that we propose to generate the BPA values. This methodology examines several metrics of the wireless network frames. Through manual forensics analysis, out of the all available metrics, five metrics have been empirically selected as the most appropriate for detecting the attacks. These are the Received Signal Strength Indication (RSSI), Injection Rate (Rate), Network Allocation Vector (NAV), MAC layer sequence number difference between two consecutive frames (Seq) and arrival time difference between two consecutive frames (IAT).

The proposed methodology comprises of two main stages. First, both Gaussian and exponential pdf, and categorical pmf are utilized to compute the belief in Normal. Additionally, lrd is utilized to compute the belief in Attack. Second, the different BPAs are fused using D-S, and the final detection decision is taken.

A. METHOD TO ASSIGN BELIEF IN NORMAL

The belief in the hypothesis Normal indicates how strong the belief is that the current analyzed data is non-malicious. In order to assign the belief in Normal, we make use of both Gaussian and exponential pdf, and categorical pmf.

The method to assign the BPA in Normal undergoes three main steps: 1) Outlier filtering, 2) Calculating the reference of normality, 3) Assigning the belief in Normal, based on a single-metric value of the current network frame. The first two steps utilize the metric values of the previous \(n\) frames to the current frame. A description of all three steps is given below.

1) OUTLIER FILTERING

The main purpose of this step is to build a baseline of normality. This step uses \(k\)-means clustering to filter significant outliers in the analyzed data (i.e. baseline data). Then, the remaining data resulting after discarding the outliers (i.e. clean data), is used to build more accurate baseline of normality. The \(k\)-means algorithm is applied on all five metrics of the frames in the baseline data. Assuming that the majority of the network traffic is non-malicious, the cluster with greater number of frames is considered to comprise non-malicious frames, and the smaller cluster is considered to comprise malicious frames.

Let us consider a finite \(d\)-dimensional feature space \(S = C_1 \cup C_2\), where \(S\) is the baseline data, \(k = 2\), \(C_1 = \{x_1, x_2, \ldots, x_m\}\) is the class for non-malicious data, \(C_2 = \{x_{m+1}, x_{m+2}, \ldots, x_{m+l}\}\) is the class for malicious data, \(n = m + l\) is the number of frames considered previous to the currently analyzed frame, \(x_i \in \mathbb{R}^d (i = 1, 2, \ldots, n)\), \(m\) is the number of non-malicious frames, \(l\) is the number of malicious frames. The outlier filtering step, applying (9), is expected to produce a \(d\)-dimensional feature space \(F = C_1 \cup C_2 = \{x_1, x_2, \ldots, x_m, x_{m+1}, \ldots, x_{m+l}\}\), where \(F\) is the clean data and \(g \ll l\), i.e. all or most data that comprise \(C_2\) should be discarded from the original dataset. The experiments conducted in this work considers the feature space of dimension \(d = 5\), where each network frame is a vector of five metrics. The clean data is used in the next step of this phase to calculate the reference of normality.

One condition that should be met, for statistical reliability, is that the baseline data should be \(n \geq 30\). This is the minimum number of frames required for estimating the parameters mean \(\mu\) and variance \(\sigma^2\) of the Gaussian distribution and rate parameter \(\lambda\) of the exponential distribution [27]. Algorithm 1 provides the implementation pseudo-code of the first step of the belief assignment method.

**Algorithm 1 Implementation Pseudo-Code of the First Step of the Belief Assignment on the Hypothesis Normal**

1: Get a single-metric value (\(x\)) from the current frame
2: Get baseline data (all metrics from previous \(n\) frames)
3: 
4: \textbf{Outlier Filtering}
5: Input: baseline data = \(C_1 \cup C_2\)
6: Select, initially, centroids \((c_1\) and \(c_2\)) using \(k\)-means++
7: \textbf{do}
8: Calculate distance from \(c_1\) and \(c_2\) to all the frames
9: \(d(c, x) = \sqrt{\sum_{i=1}^{n} (c - x_i)^2}\)
10: Assign all frames to the closest centroid \((c_1\) or \(c_2\))
11: Per cluster, identify a new centroid
12: \(d(c, x)/n\)
13: \textbf{while} \(c_1\) and \(c_2\) change
14: Remove outlier cluster
15: Output: clean data = \(C_1 \cup C_2 = (C_2' \ll C_2)\)

2) CALCULATING THE REFERENCE OF NORMALITY

The main purpose of this step is to define a reference of normality for calculating the BPA in Normal. This step utilizes Gaussian pdf for RSSI and Seq metrics, exponential pdf for IAT and categorical pdf for Rate and NAV.

For the metrics RSSI (measured in dBm) and Seq metrics, the underlying pdf of the metric values (i.e. the probability of occurrence of any metric sample) can be obtained as described in (3), based on the estimation of the \(\mu\) and \(\sigma^2\) for each metric from the clean data. The reference of normality is defined by the value with the maximum probability \(p_{\text{max}}\), which is the probability value, when \(x\) coincides with \(\mu\):

\[
p_{\text{max}} = f(\mu) = \frac{1}{\sqrt{2\pi\sigma^2}}
\]

For the metric IAT, based on the estimation of \(\lambda\) from the metric values in the clean data, the underlying pdf of the metric values can be obtained as in (4). The reference of normality is defined by the value with the maximum probability \(p_{\text{max}}\), which coincides with \(f(x_{\text{min}})\), where \(x_{\text{min}}\) is the minimum value of the metric IAT in the clean data. When \(x_{\text{min}} = 0\), then \(p_{\text{max}} = \lambda\) according to (4).
Finally, for each of the metrics, Rate and NAV, the empirical probability (relative frequency) of each unique value is computed. Based on (5) and (6), the empirical probability of a unique value \( x_i \) is the absolute frequency of the unique value \( n_i \), normalized by the total number of the metric values in the clean data, \( N \).

\[
f(x_i \mid p) = \frac{n_i}{N} \tag{11}
\]

The references of normality for RSSI, Seq, and IAT, and the empirical probabilities for Rate, and NAV are used when assigning the belief in Normal to the current frame, as explained in the next step. Algorithm 2 provides the implementation pseudo-code of the second step of the belief assignment method.

**Algorithm 2 Implementation Pseudo-Code of the Second Step of the Belief Assignment on the Hypothesis Normal**

1: Calculating the Reference of Normality
2: Input: Single-metric values \( x_i \) of the frames in clean data
3: For metrics RSSI and Seq:
4: Calculate \( \mu \) and \( \sigma \) of the single-metric values \( x_i \)
5: for each \( x_i; (i=1,2,...,m+g) \) do
6: \( f(x_i \mid \mu, \sigma^2) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{(x_i-\mu)^2}{2\sigma^2}} \)
7: end for
8: Find reference of normality \( (p_{max}) \)
9: \( p_{max} = f(\mu) = \frac{1}{\sqrt{2\pi\sigma^2}} \)

10: For metric IAT:
11: Calculate \( \mu \) of the single-metric values \( x_i \)
12: for each \( x_i; (i=1,2,...,m+g) \) do
13: \( f(x_i \mid \lambda) = \begin{cases} \lambda e^{-\lambda x} & \text{for } x_i \geq 0 \\ 0 & \text{for } x_i < 0 \end{cases} \)
14: end for
15: Find reference of normality \( (p_{max}) \)
16: \( p_{max} = f(x_{min} \mid \lambda) \)

17: For metrics Rate and NAV:
18: Find the set of unique values \( (X) \), frequency of each unique value \( n_i \) and the total number of values \( N \).
19: for each unique value \( x_i \in X \) do
20: \( f(x_i \mid p) = \frac{n_i}{N} \)
21: end for
22: Output: \( p_{max} \) or \( f(x_i \mid p) \)

3) BELIEF ASSIGNMENT IN NORMAL

This step provides the belief value in Normal. For the metrics RSSI and Seq, the probability of the currently analyzed metric value \( f(x_i) \), calculated using (3), is normalized by \( p_{max} \) given by (10), as illustrated in Fig. 1. Thus, the belief in Normal for these metrics is computed as:

\[
m(N) = \frac{f(x_i)}{f(\mu)} \tag{12}
\]

For the metric IAT, the probability of the currently analyzed IAT value \( f(x_i) \), given by (4), is normalized with the value \( p_{max} \). As explained in the previous step, for IAT, \( p_{max} = f(x_{min}) \). Thus, the belief in Normal, is computed as:

\[
m(N) = \frac{f(x_i)}{f(x_{min})} \tag{13}
\]

This step can update the reference of normality \( (p_{max}) \) for the metrics RSSI, Seq, and IAT. The value of \( p_{max} \) is updated when the computed \( f(x_i) \) of the currently analyzed value is greater than the current reference. In that case, the updated reference of normality would be \( p_{max} = f(x_i) \). Fig. 2 represents the assignment of the belief in Normal to the current frame, based on the exponential pdf.

Regarding the metrics Rate and NAV, the belief in Normal is assigned to the current frame based on the empirical probabilities computed by (11) in the previous step. When the analyzed value \( (x_i) \) is equal to one of the unique values in the clean data, the belief in Normal is assigned as:

\[
m(N) = p_i \tag{14}
\]

In contrast, when the analyzed value \( (x_i) \) is not equal to any of the unique values in the clean data, the belief in Normal is assigned to an arbitrarily small value. As previously explained in Section II, the presence of null beliefs in
the D-S fusion process can be a detrimental factor on the fused beliefs. Fig. 3 depicts the assignment of the belief in Normal to the current frame, based on categorical pmf. Algorithm 3 provides the implementation pseudo-code of the third step of the belief assignment method.

**Algorithm 3 Implementation Pseudo-Code of the Third Step of the Belief Assignment on the Hypothesis Normal**

1. **Belief Assignment in Normal**
2. Input: Single-metric value $x$ of the current frame
3. For metrics RSSI and Seq:
4. Compute $f(x)$ based on the Gaussian pdf
5. Calculate Belief in Normal, $m(N)$
6. $m(N) = f(x)/f(\mu) = f(x)/p_{\text{max}}$
7. For metric IAT:
8. Compute $f(x)$ based on the exponential pdf
9. Calculate Belief in Normal, $m(N)$
10. $m(N) = f(x)/f(x_{\text{min}}) = f(x)/p_{\text{max}}$
11. For metrics Rate and NAV:
12. if $x \in X$ then $m(N) = f(x | p) = \frac{p}{N}$
13. else $m(N) = 0$
14. end if
15. Output: $m(N)$

**B. METHOD TO ASSIGN BELIEF IN ATTACK**

The belief in the hypothesis Attack indicates how strong the belief is that the current analyzed data are malicious. In order to assign the belief in Attack, we propose using the $lrd$ technique. As previously explained in Section III-D, the $lrd$ is an ideal detection technique. Therefore, this technique is an ideal methodology to assign the belief in Attack.

The proposed methodology to assign the BPA depends on the comparison between the local density of a frame and its $k$-NNs among the previous $n$ frames within the baseline data. This methodology undergoes two main steps: 1) Calculating the reference of abnormal traffic, and 2) Assigning the belief in Attack, utilizing the $lrd$. A description of the two steps is given below. Algorithm 4 provides the implementation pseudo-code of the belief assignment for the hypothesis Attack.

1) **CALCULATING THE REFERENCE OF ABNORMAL TRAFFIC**

This step starts by removing duplicate features from the baseline data. This is because duplication would introduce instability caused by the distance value of zero, when calculating $lrd$ in the following steps. As a result, a new dataset called unique data is generated.

This step can be divided into the following five points:

1. Remove duplicate features from the baseline data, and generate unique data.
2. For each frame in the unique data, the $k$-NNs are found.
3. For each of the neighbors found in step 2), the $k$-NN are also found.
4. For each frame, the $lrd$ is calculated based on (7).
5. The maximum $lrd$ value (i.e. $lrd_{\text{max}}$) is selected as the reference of abnormal traffic.

Points 2-4 are repeated for each metric in the unique data. Fig. 4 shows a comparison between the local density of an object $A$ with its three nearest neighbors. As can be seen, the object $A$ has a much lower local density than its neighbors.

![FIGURE 4. A comparison between the local density of A with its three nearest neighbors. Given $k = 3$, A has a much lower local density than its 3 neighbors. This means that the belief in Attack assigned to the network frame based on A is higher than the beliefs assigned based on the 3 neighbors.](image)

Due to the computational cost that would entail to have a large number of nearest neighbors, we have experimentally chosen $k_{\text{max}} = 20$ for the $k$-NN algorithm. If the number of the unique values ($v$) is less than or equal to $k_{\text{max}}$, then the number of nearest neighbors is set as $k = v$. Otherwise, $k$ is set as $k = k_{\text{max}}$.

The $lrd$ for the currently analyzed frame $lrd(x_i)$ is calculated as described in (7). If $lrd(x_i)$ is larger than the reference of abnormal traffic $lrd_{\text{max}}$, then the reference of abnormal traffic is updated as $lrd_{\text{max}} = lrd(x_i)$.

2) **BELIEF ASSIGNMENT IN ATTACK**

This step provides the belief value in Attack. Once the $lrd$ for the currently analyzed frame, $lrd(x_i)$, and the reference of
abnormal traffic, $lrd_{\text{max}}$, have been calculated, the belief in $\text{Attack}$ assigned to the currently analyzed frame $x_i$ is calculated as follows:

$$m(A) = \left(1 - \frac{lrd(x_i)}{lrd_{\text{max}}}\right)$$  \hspace{1cm} (15)

Thus, the frame with the lowest $lrd(x_i)$ would receive the highest belief in $\text{Attack}$.

**Algorithm 4 Implementation Pseudo-Code of the Belief Assignment on the Hypothesis $\text{Attack}$**

1: Get a single-metric value ($x_i$) from the current frame
2: Get baseline data (all metrics from previous $n$ frames)
3: 
4: 1) Calculating the Reference of Abnormal Traffic
5: Input: baseline data
6: Remove duplicates in baseline data
7: 
8: if $m \leq k_{\text{max}}$, then
9: 
10: else
11: $k = k_{\text{max}}$
12: end if
13: 
14: for each unique single-metric value do
15: 
16: Find the $k$-NN
17: 
18: | for each previous $k$ nearest neighbour do
19: 
20: Find the $k$-NN
21: 
22: end for
23: 
24: Calculate $lrd$
25: 
26: end for
27: 
28: Output: $lrd_{\text{max}}$
29: 
30: Calculate the local reachability density $lrd(x_i)$
31: 
32: if $lrd(x_i) > lrd_{\text{max}}$ then
33: 
34: $lrd_{\text{max}} = lrd(x_i)$
35: 
36: end if
37: 
38: 2) Belief Assignment in $\text{Attack}$
39: 
40: Input: $lrd(x_i)$ and $lrd_{\text{max}}$
41: 
42: Calculate Belief in $\text{Attack}$, $m(A)$
43: 
44: $m(A) = \left(1 - \frac{lrd(x_i)}{lrd_{\text{max}}}\right)$
45: 
46: Output: $m(A)$

**D. FUSION OF BELIEFS AND DETECTION DECISION**

As described early on in this Section, the second stage of the proposed approach conducts the fusion of beliefs using D-S theory. This stage also aims to make the final decision on whether the network frame is actually malicious or not.

To meet the requirements of D-S theory, all the conditions listed in (1) have to be met. In particular, we need to ensure that the addition of all the belief values is equal to 1. In order to satisfy this condition, we compute the normalization of the three BPA values, as described in (17).

$$m(H') = \frac{m(H)}{\sum_{H \subseteq \Theta} m(H)} \hspace{1cm} \forall H \subseteq \Theta \hspace{1cm} (17)$$

Then, the BPA values assigned by all the observers are fused according to the Dempster’s rule of combination (2). The outcome of the D-S theory is a complete set of BPA values (i.e. one for each hypothesis initially considered). The analyzed information is classified according to the hypothesis with the highest BPA, which is considered to be the correct decision. Algorithm 5 depicts the implementation pseudo-code of the fusion of beliefs and the detection process.

**E. SINGLE METRIC ATTACK DETECTION**

As previously explained, IDSs that make use of multiple metrics in a cross-layers approach may improve their efficiency. Nonetheless, we also investigate whether using the BPA values assigned to single metrics could be used to produce more accurate detection results than multi-metric approaches.

By computing the BPAs as described in Section IV, the proposed approach could classify the network frames as normal or malicious, based on the belief values generated from a single metric only. If the belief in $\text{Normal}$ is greater than or equal to the belief in $\text{Attack}$, $m(N) \geq m(A)$, the currently analyzed frame would be classified as normal. Otherwise, if the belief in $\text{Normal}$ is smaller than the belief in $\text{Attack}$ the currently analyzed frame would be classified as malicious.

**V. TESTBED AND NETWORK TRAFFIC MEASUREMENTS**

**A. EXPERIMENTAL TESTBED WLAN**

The performance of the proposed BPA methodology has been evaluated on an experimental IEEE 802.11 network testbed, which was set up in our laboratory. As shown in Fig. 5, the experimental testbed consists of a wireless client machine connecting to the Internet through a legitimate Access Point (AP). Another machine is used as an attacker using the suite of hacking tools Aircrack [28]. The client machine and the attacker were running Linux and all the devices except from the Linksys WRT54GL AP used the Atheros chipset in their wireless cards.

**B. WIRELESS INJECTION ATTACKS**

The two different network traffic datasets, used in this work, have been made publicly available in [16], including the
Each of these dataset includes traces of one type of wireless injection attack. These types are MitM attack at the physical layer, and deauthentication attack. The relevant network traffic has been monitored and gathered from a real IEEE 802.11 network testbed shown in Fig. 5. The first dataset contains traces of the MitM attack at the physical layer, whereas the second dataset contains traces of the deauthentication attack. The MitM dataset comprises 14493 instances of which 93.1% (13498 frames) is normal and 6.9% (995 frames) is malicious. The Deauthentication dataset comprises 228 instances of which 71.93% (164 frames) is normal and 28.07% (64 frames) is malicious. It is worth noting that in our experimental evaluation, the ground truth was used only for evaluation purposes and was not used during the detection process.

**Algorithm 5 Implementation Pseudo-Code of the Belief Assignment on the Hypothesis Uncertainty and Beliefs Fusion**

1: 1) Calculating Uncertainty
2: Input: Belief in Normal and Attack assigned to ith frame;
3: \( m_i(N), m_i(A) \)
4: for metric = 1 \( \rightarrow \) r do
5: \( m_i(U) = \min(m_i(A), m_i(N))/\max(m_i(A), m_i(N)) \)
6: end for
7: Output: \( m_i(U) \)
8: 2) Beliefs Adjustment
9: Input: Beliefs set assigned to ith frame
10: \( m_i(N), m_i(A), m_i(U) \)
11: for metric = 1 \( \rightarrow \) r do
12: \( m_i(H) = m_i(H)/\sum H \subseteq \Theta m_i(H) \)
13: end for
14: Output: \( m_i(N)^t, m_i(A)^t, m_i(U)^t \)
15: 3) Beliefs Fusion
16: Input: Adjusted beliefs set assigned to ith frame
17: \( m_i(N)^t, m_i(A)^t, m_i(U)^t \)
18: for metric = 1 \( \rightarrow \) r do
19: Apply Dempster’s rule of combination (2)
20: \( m(H) = m_i(H) \oplus m_{i+1}(H) \ \forall \ H \subseteq \Theta \)
21: end for
22: Output: \( m(N), m(A), m(U) \)
23: 4) Network Traffic Classification
24: Input: Fused beliefs set
25: \( m(N), m(A), m(U) \)
26: if \( m(N) \geq m(A) \) then
27: Currently analysed frame classified as normal
28: else
29: Classified as malicious
30: end if
31: Output: Network frame classification

**FIGURE 5.** Logical topology of the IEEE 802.11 network testbed; one wireless client machine connecting to the Internet, one legitimate AP, and one attacker implementing the wireless injection attacks.

1) MAN-IN-THE-MIDDLE ATTACK AT THE PHYSICAL LAYER
To implement the MitM attack, the Airpwn tool [29] was used by the attacker to launch the attack. This software can be found as part of the suite of penetration testing tools Aircrack. Airpwn eavesdrops the transmitted frames in a WiFi network, analyses this information and injects malicious frames into the wireless channel. If Airpwn identifies an HTTP request from a legitimate wireless node, it injects its own crafted HTML code, spoofing the TCP sequence number and the MAC address of the legitimate AP.

This tool takes advantage of the time required by the server to respond to legitimate website requests. The nature of this MitM attack requires the victim to be located within the wireless coverage area of the attacks. Since there are no hops between the attacker and the victim, it takes the attacker much less time to respond to legitimate website requests than the web server. When the client receives the response from the attacker, it assumes the response as legitimate and processes the injected code. The future response from the legitimate web server would be discarded by the victim as it assumes the original request has already been received.

2) DEAUTHENTICATION ATTACK
The deauthentication attack has also been investigated in this work. To implement this attack, the Aircrack tool [28] was used by the attacker to inject deauthentication frames to the wireless network traffic. The attacker injects spoofed deauthentication frames with the purpose of forcing the client to re-establish a connection with the AP. The attacker spoofs its MAC address to deceive the victim that the frames are coming from the authorized AP.

This type of attack is commonly utilized in DoS attacks but also constitutes the first step of breaking into WPA2 encrypted wireless networks. In the latter case, the attacker injects a few spoofed deauthentication frames with the purpose of forcing the client to re-establish a connection with the AP. At a later stage and offline, the attacker could succeed in cracking WPA2 by applying brute force or dictionary attack techniques.

**C. NETWORK TRAFFIC FEATURES**
The relevant network traffic has been monitored and gathered by the client machine using the network packets analyzer tcpdump [30] in pcap format. Two datasets have been gathered from a real IEEE 802.11 network testbed shown in Fig. 5. The first dataset contains traces of the MitM attack at the physical layer, whereas the second dataset contains traces of the deauthentication attack. The MitM dataset comprises 14493 instances of which 93.1% (13498 frames) is normal and 6.9% (995 frames) is malicious. The Deauthentication dataset comprises 228 instances of which 71.93% (164 frames) is normal and 28.07% (64 frames) is malicious. It is worth noting that in our experimental evaluation, the ground truth was used only for evaluation purposes and was not used during the detection process.
The network analyzer TShark [31] was used to extract different metrics from the frame in the captured pcap files. These metrics are *Rate*, *NAV*, *Seq* and *IAT*. Since the implemented MitM attack affects only the data frames, management and control frames were not considered in the MitM attack detection process. On the other hand, only management frames were used during the detection of deauthentication attack, which are the type of frames used to conduct this attack.

The metrics *RSSI*, *Seq* and *IAT* for the MitM dataset are represented in Figs. 6-8. The section in blue corresponds to the non-malicious traffic, whereas the section in red corresponds to the traces of MitM attack. The Y-axis of the figures represents the respective metric, whereas the X-axis of the figures represents the number of captured network frames. As seen in Fig. 6, even though both the attacker and the authorized AP manifest themselves in their own range of *RSSI* values, we cannot clearly define a threshold to differentiate between normal and malicious traffic. This is because in some network frames, such as the ones around the 5000th frame, there is an overlap of *RSSI* values between the normal and attack traffic. For the metrics *Seq* and *IAT*, as shown in Figs. 7-8 respectively, the nature of both metrics does not allow us to define what values correspond either to normal or malicious traffic, as there are spikes in both types of traffic.

**VI. EVALUATION OF RESULTS**

This section describes the off-line detection results, and compares the results generated by the proposed methodology using all the possible combinations of metrics. There are two main purposes of these results. First, to evaluate the efficiency of the proposed methodology in identifying the presence of attacks, and producing reduced number of false alarms. Second, to identify which of the possible combinations of metrics produces the best detection results.

The effectiveness of the proposed methodology has been evaluated using the following performance metrics, which provide evidence of how effective an IDS is at making correct detections:

- **True Positive Rate (TPR) or Detection Rate** - Proportion of malicious frames correctly classified among all the malicious data:
  \[
  TPR = \frac{TP}{TP + FN}
  \]  

- **False Positive Rate (FPR)** - Proportion of normal data misclassified as malicious among all the normal data:
  \[
  FPR = \frac{FP}{TN + FP}
  \]  

- **Overall Success Rate (OSR) or Accuracy** - Proportion of frames correctly classified among all the data:
  \[
  OSR = \frac{TP + TN}{TP + FP + TN + FN}
  \]  

- **Precision** - Proportion of malicious frames correctly classified among all the alarms generated:
  \[
  Precision = \frac{TP}{TP + FP}
  \]  

- **F-score** - Tradeoff between *Precision* and TPR, used to compare two distinctive classification methodologies:
  \[
  F\text{-score} = \frac{2 \cdot Precision \cdot TPR}{Precision + TPR}
  \]
where True Positive (TP) represents attacks classified as attacks; True Negative (TN) represents normal instances classified as normal; False Positive (FP) represents normal instances misclassified as attack; and False Negative (FN) represents attacks misclassified as normal.

We have divided the datasets in 80% for training (i.e. train data) and 20% for testing (i.e. test data). The training dataset was used to build the normality and attack baselines (i.e. baseline data), whereas the remaining data were used to generate the beliefs and evaluate the proposed methodology.

### A. SINGLE METRIC DETECTION PERFORMANCE

This section presents the initial performance evaluation of the proposed methodology, which focuses on the assessment of the single metric based attack detection, as described in Section IV-E. For all the five considered features, the proposed approach could classify the network frames as normal or malicious, based on the belief values generated for each single metric.

#### 1) DETECTION OF MAN-IN-THE-MIDDLE ATTACK

The detection results for the MitM attack, based on individual metric, are presented in Table 1. As can be seen, there are two metrics that provide outstanding performance. These are Rate and NAV. The single metric NAV generates perfect detection results, 100% TPR and 0% FPR. Regarding the metric Rate, it produces perfect TPR (i.e. 100%) and only 0.18% FPR. Regarding the remaining three metrics, despite generating relatively low FPR (i.e. reaching 8.24%), none of the metrics produce acceptable results in terms of TPR. The TPR for metrics RSSI and IAT are 49.01% and 79.72% respectively, whereas the TPR for Seq reaches only 34.93%. In terms of Precision, the metrics RSSI, IAT and Seq produce 57.62%, 60.99% and 50.2%, respectively.

<table>
<thead>
<tr>
<th>Metric</th>
<th>TPR (%)</th>
<th>FPR (%)</th>
<th>OSR (%)</th>
<th>Precision (%)</th>
<th>F-score</th>
</tr>
</thead>
<tbody>
<tr>
<td>RSSI</td>
<td>49.01</td>
<td>5.83</td>
<td>87.89</td>
<td>57.62</td>
<td>0.53</td>
</tr>
<tr>
<td>Rate</td>
<td>100</td>
<td>0.18</td>
<td>99.84</td>
<td>98.89</td>
<td>0.99</td>
</tr>
<tr>
<td>NAV</td>
<td>100</td>
<td>0</td>
<td>100</td>
<td>50.2</td>
<td>0.41</td>
</tr>
<tr>
<td>Seq</td>
<td>34.93</td>
<td>5.6</td>
<td>86.13</td>
<td>50.2</td>
<td>0.41</td>
</tr>
<tr>
<td>IAT</td>
<td>79.72</td>
<td>8.24</td>
<td>90.09</td>
<td>60.99</td>
<td>0.69</td>
</tr>
</tbody>
</table>

The reasons that justify the good performance of these two metrics are related to the implementation of the MitM attack by the Airpwn tool. For instance, the attacker constantly transmits at a low transmission rate (i.e. 1 Mbps) to achieve a higher throughput in the wireless communication. This transmission rate would usually be different from the rate, used to transmit data frame, by the legitimate wireless devices. Similarly, the actual NAV value set by the transmitters in a wireless network is correlated with the used transmission rate.

Since the attacker would use a low transmission rate, the NAV value set by the attacker would equivalently be larger than the NAV value set by the legitimate wireless devices.

From the presented results, it would be expected to use the single metric methodology using either Rate or NAV to defend the wireless network against MitM attacks at the physical layer. Nonetheless, the detection system cannot assume the implementation parameters chosen by the attacker. More importantly, it is impossible to anticipate the particular type of attack implemented by the attacker. Hence, basing the wireless injection attack detection on the use of single metric may be prone to a high number of misclassification results.

#### 2) DETECTION OF DEAUTHENTICATION ATTACK

The detection results for the deauthentication attack, based on individual metric, is presented in Table 2. Regarding the deauthentication attack detection, one noticeable result is produced by the single metric Rate. In contrast to the case of MitM attack in which Rate produces 100% TPR, for the deauthentication attack detection, the same metric generates 0% TPR and 2.44% FPR. It is also remarkable the detection results for RSSI, which produces 0% FPR. This is the best FPR results of all the evaluated metrics for deauthentication attack. Apart from IAT, which reaches 19.51% FPR, all metrics generate low rate of false alarms, reaching 5% FPR. Nevertheless, these metrics have poor results in terms of TPR, except for NAV. Once again, the best overall detection results are produced by the single metric NAV, with 100% TPR and only 5% FPR. The OSR, Precision and F-score for this metric are 96.83%, 91.67% and 0.96, respectively.

<table>
<thead>
<tr>
<th>Metric</th>
<th>TPR (%)</th>
<th>FPR (%)</th>
<th>OSR (%)</th>
<th>Precision (%)</th>
<th>F-score</th>
</tr>
</thead>
<tbody>
<tr>
<td>RSSI</td>
<td>68.18</td>
<td>0</td>
<td>88.89</td>
<td>10</td>
<td>0.81</td>
</tr>
<tr>
<td>Rate</td>
<td>0</td>
<td>2.44</td>
<td>63.49</td>
<td>0</td>
<td>n/a</td>
</tr>
<tr>
<td>NAV</td>
<td>100</td>
<td>5</td>
<td>96.83</td>
<td>91.67</td>
<td>0.96</td>
</tr>
<tr>
<td>Seq</td>
<td>50</td>
<td>2.44</td>
<td>80.95</td>
<td>91.67</td>
<td>0.65</td>
</tr>
<tr>
<td>IAT</td>
<td>45.45</td>
<td>19.51</td>
<td>68.25</td>
<td>55.56</td>
<td>0.5</td>
</tr>
</tbody>
</table>

The good performance produced by the single metric NAV is explained by the large NAV value set by the attacker, as explained in the case of MitM attack. However, the performance drop in the case of Rate is justified by the fact that the AP also transmits at a very low transmission rate the control and management frames. Therefore, distinguishing between normal and malicious frames, based only on single metric Rate becomes extremely complicated in the case of deauthentication attack.

These results highlight the fact that the use of single metrics configuration to detect the presence of wireless injection attacks may be inefficient against different type of attacks. Therefore, we argue that a multi-metric approach would address such issues.
B. MULTI-METRIC DETECTION PERFORMANCE

This section presents the multi-metric attack detection evaluation of the proposed methodology for all the possible combinations of metrics. The best results overall are expected in the case where all the possible metrics are combined.

The detection results of the proposed methodology, for all possible metrics combinations, have been plotted in Figs. 9-10. These figures, in the form of bar chart, present the TPR, FPR and OSR results in three separate bars, for each metrics combination. The X-axis represents the particular metrics combination, whereas the Y-axis represents the detection result in percentage. The TPR is represented in green, the FPR in red, and the OSR is blue.
1) DETECTION OF MAN-IN-THE-MIDDLE ATTACK

The MitM attack detection results of the proposed methodology, for all possible metrics combinations, have been plotted in Fig. 9. For the case of two-metrics combination, the combination Rate & NAV generates the best detection results, with 100% TPR and 0.18% FPR. The two metrics that produce the best single metric results for MitM attack detection would also produce the best detection results when combined. Furthermore, the two-metric combinations RSSI & Rate, RSSI & NAV, Rate & IAT and NAV & IAT also provide considerably good detection results. All these metrics combinations produce 100% TPR. In terms of FPR, these two-metric combinations generate 5.33%, 5.83%, 7.69%, and 8.19%, respectively. A common factor to all these metrics combinations is the presence of either RSSI or NAV. This shows that the contributions of these two metrics dominate the detection and, in turn, improve the results.

On the other hand, metrics combinations such as RSSI & Seq produce poor detection results in terms of TPR (i.e. 36.06%). Because these two metrics generate low TPR during the single metric detection, it is expected that this metrics combination would also perform poorly. All the detection results for the two-metrics combinations have been tabulated in Table 3.

<table>
<thead>
<tr>
<th>TABLE 3. Man-in-the-Middle attack detection results generated by the proposed methodology, using two-metrics combination detection configuration.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Metric</td>
</tr>
<tr>
<td>RSSI, Rate</td>
</tr>
<tr>
<td>RSSI, NAV</td>
</tr>
<tr>
<td>RSSI, Seq</td>
</tr>
<tr>
<td>RSSI, IAT</td>
</tr>
<tr>
<td>Rate, NAV</td>
</tr>
<tr>
<td>Rate, Seq</td>
</tr>
<tr>
<td>Rate, IAT</td>
</tr>
<tr>
<td>NAV, Seq</td>
</tr>
<tr>
<td>NAV, IAT</td>
</tr>
<tr>
<td>Seq, IAT</td>
</tr>
</tbody>
</table>

The detection results for all the three-metrics combinations have been tabulated in Table 4. For this number of metrics, the best detection results are produced by both RSSI, Rate & IAT and RSSI, NAV & IAT. Both metrics combinations produce 100% TPR, 3.96% FPR and 96.59% OSR. All the remaining combinations, except from RSSI, Rate & Seq, RSSI, NAV & Seq and RSSI, Seq & IAT, provide 100% TPR. However, these metrics combinations also generate slightly higher FPR results, reaching 10.29% FPR in the case of Rate, Seq & IAT.

These results show that, as more metrics are combined, the overall efficiency of the proposed detection methodology, in terms of TPR, improves among most of the metrics combinations. Nonetheless, there is also a slight overall increase in terms of FPR. This phenomenon can be interpreted as that the detection methodology becomes more sensitive as more metrics are used during the detection process. In other words, the BPA in Attack generally increases, and more malicious frames are correctly classified, but also more normal frames are misclassified as malicious.

For the case of four-metrics combination, all the combinations achieve perfect detection, in terms of TPR (i.e. 100%). The best detection results overall are obtained by the combination of RSSI, Rate, NAV & IAT, which produces 3.96% FPR and 96.59% OSR. Only the combination of Rate, NAV, Seq & IAT provides FPR results higher than 5.69%.

The detection results for the four-metrics and five-metrics combinations have been tabulated in Table 5. Similar to the analysis presented about the three-metrics combination, as more metrics are combined, the overall efficiency of the proposed detection methodology, in terms of TPR, improves among most of the metrics combinations.

<table>
<thead>
<tr>
<th>TABLE 4. Man-in-the-Middle attack detection results generated by the proposed methodology, using three-metrics combination detection configuration.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Metric</td>
</tr>
<tr>
<td>RSSI, Rate, NAV</td>
</tr>
<tr>
<td>RSSI, Rate, Seq</td>
</tr>
<tr>
<td>RSSI, Rate, IAT</td>
</tr>
<tr>
<td>RSSI, NAV, Seq</td>
</tr>
<tr>
<td>RSSI, NAV, IAT</td>
</tr>
<tr>
<td>RSSI, Seq, IAT</td>
</tr>
<tr>
<td>Rate, NAV, Seq</td>
</tr>
<tr>
<td>Rate, NAV, IAT</td>
</tr>
<tr>
<td>Rate, Seq, IAT</td>
</tr>
<tr>
<td>NAV, Seq, IAT</td>
</tr>
</tbody>
</table>

Finally, the combination of five metrics RSSI, Rate, NAV, Seq & IAT provides 100% TPR, 4.23% FPR, 96.36% OSR and 0.88 F-score.

2) DETECTION OF DEAUTHENTICATION ATTACK

The deauthentication attack detection results of the proposed methodology, for all possible metrics combinations, have been plotted in Fig. 10. For the case of two-metrics combination, the combinations RSSI & Rate, Rate & NAV, and NAV & Seq generate the best detection results, with 100% TPR and 2.44% FPR. Once again, the metric that generated the best results in the single metric configuration (i.e. NAV), is present in all these two-metrics combinations. Although the metrics combination NAV & IAT also produces 100% TPR,
the detection results in terms of FPR reach 19.51%. It is notable that the combinations RSSI & Seq and RSSI & IAT do not generate any false alarm (i.e. 0% FPR). However, their F-score is less than 0.78 due to the low detection rate (i.e. 63.64% and 27.27% TPR, respectively). The detection results for the two-metric combinations have been tabulated in Table 6.

The detection results for all the three-metrics combinations have been tabulated in Table 7. In this case, the best detection results are produced by RSSI, Rate & NAV, RSSI, NAV & Seq and Rate, NAV & Seq, with 100% TPR and 98.41% OSR. Although both sets Rate, NAV & IAT and NAV, Seq & IAT also provide 100% TPR, they produce a high number of FPR, causing a low Precision of 73.33%. For all the different combinations, the metric NAV seems to generally improve the detection performance. In contrast to the case of MitM attack, the inclusion of the metric Rate drastically degrades the performance of the deauthentication attack detection.

The detection results for the four-metrics and five-metrics combinations have been tabulated in Table 8. For the case of four-metrics combination, apart from the set RSSI, Rate, Seq & IAT, all the combinations achieve detection rate larger than 90.91%. Two of these sets, RSSI, NAV, Seq & IAT and Rate, NAV, Seq & IAT, achieve 100% TPR. In particular, the combination RSSI, NAV, Seq & IAT generates the best detection results, with only 2.44% FPR and F-score of 0.85. Similar to what was discussed for the case of MitM attack detection, as more metrics are combined, the overall efficiency of the proposed detection methodology, in terms of TPR, improves among most of the metrics combinations. Additionally, in the case of deauthentication attack detection, the FPR remains generally low, with 2.44% for almost all the four-metric combinations.

Finally, the five-metric combination provides 100% TPR, 2.44% FPR, 98.41% OSR and F-score of 0.98. These results coincide with the best detection overall across all the possible metrics combinations, for the detection of the deauthentication attack.

### C. SINGLE AND MULTI-METRIC PERFORMANCE COMPARISON

This section provides a comparison analysis between the performance of the single-metric and multi-metric configurations for the detection methodology that we propose. Table 9 presents the detection results, of the single-metric and five-metric combination configurations, for the detection of MitM and deauthentication attack. In the case of single-metric, only the metrics that generate the best detection results are included, NAV and Rate.

The detection results for the four-metrics and five-metrics combinations have been tabulated in Table 8. For the case of four-metrics combination, apart from the set RSSI, Rate, Seq & IAT, all the combinations achieve detection rate larger than 90.91%. Two of these sets, RSSI, NAV, Seq & IAT and Rate, NAV, Seq & IAT, achieve 100% TPR. In particular, the combination RSSI, NAV, Seq & IAT generates the best detection results, with only 2.44% FPR and F-score of 0.85. Similar to what was discussed for the case of MitM attack detection, as more metrics are combined, the overall efficiency of the proposed detection methodology, in terms of TPR, improves among most of the metrics combinations. Additionally, in the case of deauthentication attack detection, the FPR remains generally low, with 2.44% for almost all the four-metric combinations.

Finally, the five-metric combination provides 100% TPR, 2.44% FPR, 98.41% OSR and F-score of 0.98. These results coincide with the best detection overall across all the possible metrics combinations, for the detection of the deauthentication attack.

### TABLE 6. Deauthentication attack detection results generated by the proposed methodology, using two-metrics combination detection configuration.

<table>
<thead>
<tr>
<th>Metric</th>
<th>TPR (%)</th>
<th>FPR (%)</th>
<th>OSR (%)</th>
<th>Precision (%)</th>
<th>F-score</th>
</tr>
</thead>
<tbody>
<tr>
<td>RSSI, Rate</td>
<td>13.64</td>
<td>2.44</td>
<td>68.25</td>
<td>75</td>
<td>0.23</td>
</tr>
<tr>
<td>RSSI, NAV</td>
<td>100</td>
<td>2.44</td>
<td>98.41</td>
<td>95.65</td>
<td>0.98</td>
</tr>
<tr>
<td>RSSI, Seq</td>
<td>63.64</td>
<td>0</td>
<td>87.30</td>
<td>100</td>
<td>0.78</td>
</tr>
<tr>
<td>RSSI, IAT</td>
<td>27.27</td>
<td>0</td>
<td>74.60</td>
<td>100</td>
<td>0.43</td>
</tr>
<tr>
<td>Rate, NAV</td>
<td>100</td>
<td>2.44</td>
<td>98.41</td>
<td>95.65</td>
<td>0.98</td>
</tr>
<tr>
<td>Rate, Seq</td>
<td>50</td>
<td>2.44</td>
<td>89.95</td>
<td>91.67</td>
<td>0.65</td>
</tr>
<tr>
<td>NAV, Seq</td>
<td>100</td>
<td>2.44</td>
<td>98.41</td>
<td>95.65</td>
<td>0.98</td>
</tr>
<tr>
<td>NAV, IAT</td>
<td>100</td>
<td>19.51</td>
<td>87.30</td>
<td>73.33</td>
<td>0.85</td>
</tr>
<tr>
<td>Seq, IAT</td>
<td>59.09</td>
<td>19.51</td>
<td>73.02</td>
<td>61.90</td>
<td>0.60</td>
</tr>
</tbody>
</table>

### TABLE 7. Deauthentication attack detection results generated by the proposed methodology, using three-metrics combination detection configuration.

<table>
<thead>
<tr>
<th>Metric</th>
<th>TPR (%)</th>
<th>FPR (%)</th>
<th>OSR (%)</th>
<th>Precision (%)</th>
<th>F-score</th>
</tr>
</thead>
<tbody>
<tr>
<td>RSSI, Rate, NAV</td>
<td>100</td>
<td>2.44</td>
<td>98.41</td>
<td>95.65</td>
<td>0.98</td>
</tr>
<tr>
<td>RSSI, Rate, Seq</td>
<td>31.82</td>
<td>2.44</td>
<td>74.6</td>
<td>87.5</td>
<td>0.47</td>
</tr>
<tr>
<td>RSSI, Rate, IAT</td>
<td>18.18</td>
<td>2.44</td>
<td>69.84</td>
<td>80</td>
<td>0.30</td>
</tr>
<tr>
<td>RSSI, NAV, Seq</td>
<td>100</td>
<td>2.44</td>
<td>98.41</td>
<td>95.65</td>
<td>0.98</td>
</tr>
<tr>
<td>RSSI, NAV, IAT</td>
<td>95.45</td>
<td>2.44</td>
<td>96.83</td>
<td>95.45</td>
<td>0.95</td>
</tr>
<tr>
<td>RSSI, Seq, IAT</td>
<td>31.82</td>
<td>0</td>
<td>76.19</td>
<td>100</td>
<td>0.48</td>
</tr>
<tr>
<td>Rate, NAV, Seq</td>
<td>100</td>
<td>2.44</td>
<td>98.41</td>
<td>95.65</td>
<td>0.98</td>
</tr>
<tr>
<td>Rate, NAV, IAT</td>
<td>100</td>
<td>19.51</td>
<td>87.3</td>
<td>73.33</td>
<td>0.85</td>
</tr>
<tr>
<td>Rate, Seq, IAT</td>
<td>59.09</td>
<td>19.51</td>
<td>73.02</td>
<td>61.90</td>
<td>0.60</td>
</tr>
<tr>
<td>NAV, Seq, IAT</td>
<td>100</td>
<td>19.51</td>
<td>87.3</td>
<td>73.33</td>
<td>0.85</td>
</tr>
</tbody>
</table>

### TABLE 8. Deauthentication attack detection results generated by the proposed methodology, using four-metric and five-metric combination detection configuration.

<table>
<thead>
<tr>
<th>Metric</th>
<th>TPR (%)</th>
<th>FPR (%)</th>
<th>OSR (%)</th>
<th>Precision (%)</th>
<th>F-score</th>
</tr>
</thead>
<tbody>
<tr>
<td>RSSI, Rate, NAV, Seq</td>
<td>90.91</td>
<td>2.44</td>
<td>95.24</td>
<td>95.24</td>
<td>0.93</td>
</tr>
<tr>
<td>RSSI, Rate, NAV, IAT</td>
<td>95.45</td>
<td>2.44</td>
<td>96.83</td>
<td>95.45</td>
<td>0.95</td>
</tr>
<tr>
<td>RSSI, Rate, Seq, IAT</td>
<td>31.82</td>
<td>2.44</td>
<td>74.6</td>
<td>87.5</td>
<td>0.47</td>
</tr>
<tr>
<td>RSSI, NAV, Seq, IAT</td>
<td>100</td>
<td>2.44</td>
<td>98.41</td>
<td>95.65</td>
<td>0.98</td>
</tr>
<tr>
<td>Rate, NAV, Seq, IAT</td>
<td>100</td>
<td>19.51</td>
<td>87.3</td>
<td>73.33</td>
<td>0.85</td>
</tr>
<tr>
<td>RSSI, Rate, NAV, Seq, IAT</td>
<td>100</td>
<td>2.44</td>
<td>98.41</td>
<td>95.65</td>
<td>0.98</td>
</tr>
</tbody>
</table>

### TABLE 9. A Performance comparison between single and multi-metric detection.

<table>
<thead>
<tr>
<th>Detection approach</th>
<th>MitM TPR (%)</th>
<th>MitM FPR (%)</th>
<th>MitM OSR (%)</th>
<th>Deauthentication TPR (%)</th>
<th>Deauthentication FPR (%)</th>
<th>Deauthentication OSR (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Single-metric</td>
<td>100</td>
<td>0</td>
<td>100</td>
<td>5</td>
<td>96.83</td>
<td></td>
</tr>
<tr>
<td>Rate</td>
<td>100</td>
<td>0.18</td>
<td>99.84</td>
<td>0</td>
<td>2.44</td>
<td>63.49</td>
</tr>
<tr>
<td>Multi-metric</td>
<td>100</td>
<td>4.23</td>
<td>96.36</td>
<td>100</td>
<td>2.44</td>
<td>98.41</td>
</tr>
</tbody>
</table>

If we focus only on the detection of the MitM attack with single metric, these results may lead to the conclusion that the use of single metric is enough for the detection of wireless injection attacks. This is true for this particular attack and the metrics NAV and Rate. Nonetheless, these results are not always consistent when detecting other types of injection...
attacks. For instance, the use of the single metric Rate to
detect deauthentication attack leads to 0% TPR. On the other
hand, for these types of attack, the use of single metric NAV
provides high detection results.

It can be argued that the configuration of the detection
methodology can be adapted to the particular type of attack
being detected. However, it is impossible to know beforehand
the type of attack that the protected environment is going
to face. Therefore, as we argue in this work, the solution
would be the combined use of multiple metrics during the
attack detection. As we can see in Table 9, the performance
of the five-metric combination provides highly accurate results,
regardless of the type of attack being detected (both MitM and
deauthentication attack). In both cases, the multi-metric
configuration produces 100% TPR and less than 5% FPR. These
results highlight the benefit of using a multi-metric approach
in comparison with the single-metric approach. Hence, there
is an advantage of fusing beliefs from all possible metrics
as this provides robustness against uncertainty, for example
if the type of attack is unknown or if the attacker employs
sophisticated tools to manipulate certain metrics associated
with attacks.

VII. CONCLUSION
We have presented a novel unsupervised methodology to
dynamically generate the BPA values, based on the use of
Gaussian and exponential pdf, the categorical pmf, and the
lrd. This novel methodology dynamically assigns BPA val-
ues for each metric extracted from Wi-Fi frames, which
appropriately represent the real nature of the analyzed data.
The methodology is employed by an IDS that defends
Wi-Fi networks against different types of injection attacks.
In particular, we have evaluated the proposed methodology
against MitM and deauthentication attacks, using real net-
work traffic data generated using a Wi-Fi network.

Although the use of single metric detection can provide
very accurate detection results, there is not a single metric that
is efficient for all types of attacks. The configuration of the
detection methodology ought to be adapted to the particular

type of attack being detected. However, it is impossible to
know beforehand the type of attack that the monitored envi-
ronment may have to face. On the other hand, the combined
use of multiple metrics during the attack detection provides
accurate results, without the need to select beforehand a
specific set of metrics. In the presented results, the multi-
metric configuration produces 100% TPR and less than 5% FPR
for both the MitM and deauthentication attacks. These
results highlight the benefit of using a multi-metric approach
in comparison to the single-metric approach.

REFERENCES
storage service selection based on fuzzy logic, theory of evidence and game
detection system for 802.11 networks,” in Proc. Int. Conf. Wireless Com-
2014.
[25] S. Ando, “Introduction to k nearest neighbour classification and con-
densed nearest neighbour data reduction,” Dept. Math., Univ. Leicester,
[26] D. Taniar and W. Rahayu, “A taxonomy for nearest neighbour queries in
[27] W. C. Gorder and D. I. Foreman, Nonparametric Statistics for Non-
IBRAHIM GHAFIR is currently a Research Associate with the Wolfson School Mechanical, Electrical and Manufacturing Engineering, Loughborough University, U.K. His research interests cover several areas in computer science, including network security, wireless communication, and performance optimization.

KONSTANTINOS G. KYRIAKOPOULOS received the B.Sc. degree in electrical engineering from the Technological Education Institute of Larisa, Greece, in 2003, and the M.Sc. degree in digital communication systems and the Ph.D. degree in computer networks from Loughborough University, Loughborough, U.K., in 2004 and 2008, respectively.

From 2008 to 2016, he was a Research Associate with the School of Electronic, Electrical, and Systems Engineering, Loughborough University, where he was mainly involved in EPSRC projects and successfully licensing research output from his work. Since 2016, he has been an Academic Member with the Wolfson School of Mechanical, Electronic and Manufacturing Engineering, Loughborough University, and the Institute of Digital Technologies, Loughborough University London, London, U.K. His research interests are in the areas of computer networks, including network security, intrusion detection, vehicular communications, intelligent decision making based on network situational awareness, and network performance measurements in emerging network paradigms and their applications.

FRANCISCO J. APARICIO-NAVARRO received the B.Eng. degree in telecommunications engineering, specialized in computer networks, from the Technical University of Cartagena, Spain, in 2009, and the Ph.D. degree in computer networks from Loughborough University, Loughborough, U.K., in 2014.

From 2013 to 2018, he was a Research Associate with the School of Electronic, Electrical, and Systems Engineering, Loughborough University, and the School of Engineering, Newcastle University, Newcastle upon Tyne, U.K., where he was involved in the project University Defence Research Collaboration in Signal Processing, funded by Dstl/MoD and EPSRC. Since 2018, he has been a Lecturer (Assistant Professor) in cyber security at the Faculty of Technology, De Montfort University, Leicester, U.K. His research interests are in the areas of computer networks, cybersecurity, network security, intrusion detection, and network traffic analysis.

SANGARAPILLAI LAMBOTHRAN is currently a Professor of digital communications and the Head of the Signal Processing and Networks Research Group, Wolfson School Mechanical, Electrical and Manufacturing Engineering, Loughborough University, U.K.

He received the Ph.D. degree in signal processing from Imperial College London, U.K., in 1997. He was a Post-Doctoral Research Associate with Imperial College London until 1999. He was a Visiting Scientist with the Engineering and Theory Centre, Cornell University, USA, in 1996. From 1999 to 2002, he was with the Motorola Applied Research Group, U.K., and was investigated various projects, including physical link layer modeling and performance characterization of GPRS, EGPRS, and UTRAN. He was with King’s College London and Cardiff University as a Lecturer and a Senior Lecturer, respectively, from 2002 to 2007. His current research interests include 5G networks, MIMO, radars, smart grids, machine learning, network security and convex optimizations, and game theory. He has published approximately 200 technical journal and conference articles in these areas.

BASIL ASSADHAN received the M.S. degree in electrical and computer engineering from the University of Wisconsin and the Ph.D. degree in electrical and computer engineering from Carnegie Mellon University. He is currently an Assistant Professor with the Electrical Engineering Department, King Saud University. His research interests are in the areas of cybersecurity, network security, network traffic analysis, and anomaly detection.

HAMAD BINSALLEEH received the master’s degree in information systems security and the Ph.D. degree in computer science from Concordia University, Canada. He is currently an Assistant Professor with Al-Imam Muhammad Ibn Saud Islamic University. He has published several research papers in journals and conferences. His current research interests include cybersecurity, network security, network traffic analysis, anomaly detection, passive DNS traffic analysis, malware analysis, and malware reverse engineering. He received many honors, including international recognition and best papers.

* * *