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Influence of threshold variation on determining the properties of a polymer electrolyte fuel cell
gas diffusion layer in X-ray nano-tomography

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Abstract

Morphological parameters of a 3D binary image of a porous carbon gas diffusion layer (GDL) for
polymer electrolyte fuel cells (PEFC) reconstructed using X-ray nano-tomography scanning have
been obtained, and influence of small alterations in the threshold value on the simulated flow
properties of the reconstructed GDL has been determined. A range of threshold values with 0.4%
increments on the greyscale map have been applied and the gas permeability of the binary images
have been calculated using a single-phase lattice Boltzmann model (LBM), which is based on the
treatment of nineteen velocities in the three dimensional domain (D3Q19). The porosity, degrees of
anisotropy and the mean pore radius have been calculated directly from segmented voxel
representation. A strong relationship between these parameters and threshold variation has been
established. These findings suggest that threshold selection can significantly affect some of the flow
properties and may strongly influence the computational simulation of micro and nano-scale flows in a
porous structure.
Keywords: X-ray nano-tomography; Three-dimensional reconstruction; Threshold; Lattice Boltzmann modelling; Gas diffusion layer; Micro-structure porous materials
1. Introduction

X-ray nano-computed tomography (nano-CT) enables non-invasive 3D visualisation and characterisation of both external and internal structures of samples, for example integrated circuit (IC) chips or porous materials such as the fuel cell GDL. In nano-CT several hundred 2D images of a physical sample over a range of angles are taken and the level of X-ray attenuation in the images according to the density of the sample is mapped. These shadow images are in 256 shades of grey and can be compiled to a stack and another stack of 2D images are created corresponding to what would be seen if the sample is cut through the scanning plane. The slices can then be assembled to reconstruct a 3D digital model (Imbaby et al.; Carmignato et al., 2009; Zschech et al., 2008).

The two types of high resolution X-ray tomography scanners currently available are micro-tomography and nano-tomography systems. The former provides a resolution of 1–10 $\mu$m, while the latter can produce a resolution of less than 100 nm. In addition, scanning transmission X-ray microscopes (STXMs) operating at the National Synchrotron Light Source and Advanced Photon Source have been used for nano-tomography. The latest laboratory-based X-ray nano-tomography can achieve a resolution of 400 nm with detectability of 100–200 nm (McNulty et al., 1995; Warwick et al., 1998; Cai et al., 2000; Parkinson and Sasov, 2008). Recently, X-ray micro-tomography has been used to quantify liquid water saturation distribution in porous GDLs and determining the Q1 two-phase material parameters with a sub 10 mm resolution (Becker et al., 2008; Sinha et al., 2006). The latest report suggests that nano-tomography (Nano XCT, US: Xradia Corp.) can be used to reconstruct the porous catalyst layer (CL) of fuel cells at sub-micron resolution in order to study the changes in membranes after transient operation (Garzon et al., 2007). Nano-tomography has also been successfully employed to scan porous human dentin tubules at 295 nm resolution and to reconstruct the 3D cylindrical structure of the porous tubules, which are between 1 and 3 $\mu$m in diameter using the SkyScan desktop nano-tomography system (SkyScan 2011, Belgium: SkyScan) (Parkinson and Sasov, 2008).

Computer modelling of porous materials such as GDL is used extensively in flow simulation and characterisation. These porous materials have to be purposefully designed to allow reactant gases to pass through to the CL while removing excess product water (Parkinson and Sasov, 2008; Becker et al., 2008; Sinha et al., 2006; Garzon et al., 2007; Barbir, 2005; Sinha and Wang, 2007; Sinha et al.,
The transport phenomena inside a GDL are dependent on the local micro-structural characteristics of the pore network (Thiedmann et al., 2009; Thiedmann, C. Hartnig, I. Manke, V. Schmidt and W. Lehnert, Local structural characteristics of pore space in GDLs of PEM fuel cells based on geometric 3D graphs, J. Electrochem. Soc. 156 (11) (2009), pp. B1339–B1347. Full Text via CrossRef | View Record in Scopus | Cited By in Scopus (11) Thiedmann et al., 2009). For fuel cell flow simulation in a porous layer and pore analysis, representative binary models are required which define the internal solid-void boundaries in a GDL structure. Therefore, it is necessary to threshold the greyscale images acquired from X-ray tomography in order to produce binary images (Manke et al., 2007; Feser et al., 2006; Hung et al., 2008).

One of the crucial steps in the X-ray tomography based digital reconstruction process is thresholding, in which structures are evaluated in voxels with grey level values and segmented to distinguish solids from pores using a threshold value. At present, a threshold is often determined visually or by an algorithm supplied by the manufacturer of the scanning system. However, it has been shown that the selection of threshold is crucial and can have a significant effect on the volume fractions, pore sizes, trabecular thickness, morphological parameters and mechanical properties of various structures (Imbaby et al.; Ostadi et al., 2008; Ding et al., 1999; Hara et al., 2002; Thiedmann et al., 2008). As such, further research is needed to improve the understanding of how optimal threshold levels can be determined to enhance the accuracy and practical applicability of X-ray tomography based structural modelling and porous flow simulation.

The purpose of this study is to understand the effect of threshold variation on the properties of reconstructed porous materials. A GDL sample of 5–10 µm filament size has been scanned in a SkyScan nano-tomography scanner (SkyScan 2011, Belgium: SkyScan) with a pixel resolution of 680 nm. Next, a set of 2D greyscale image slices were produced in 256 greyscales and thresholded in 7 grey levels with a step of 0.4% variation, such that each step equates to 1 grey level. This process results in a seven sets of thresholded 2D image slices. The key structural parameters were calculated directly from seven 3D digital models, which were constructed with the seven corresponding sets of image slices. Afterwards, well-tested LB model (Bals et al., 2007; Zhang et al., 2002; Zhang and Ren, 2003; Wang et al., 2005) was applied to simulate single-phase flows through each of these 3D digital models. Finally, the resulting permeability and its sensitivity to the threshold variation were analysed.
2. Experimental

In this investigation, a 1×1×0.3 mm carbon paper GDL sample without a microporous layer (Technical Fibre Products Ltd., UK) was scanned in front of an X-ray source of SkyScan 2011 with 25 kV, 200 µA without filter, 2 s exposure time, 3 frames in average and a rotation step of 0.5 degrees. 371 shadow images with 680 nm pixel resolution were acquired within 40 min. The shadow images were then processed using modified Feldkamp filtered back projection method to reconstruct the 2D greyscale slices (SkyScan Microtomography, 2007). CTAN software (CT-analyzer, Belgium) was then employed to reconstruct a 3D digital model of the sample, as shown in Figs. 1a (SkyScan Microtomography, 2007). Figs. 1b and c show a typical shadow and a reconstructed cross-section image of a carbon paper GDL. Fig. 1d is a typical binary image of Fig. 1c that is used for calculations.

3D and 2D images of a GDL carbon paper sample. (a) An isometric view of the reconstructed image of GDL sample with 680 nm pixel resolution using CTAN, (b) a shadow X-ray tomographic image, (c) a 2D reconstructed slice image, and (d) a binary image of the cross-section shown in Fig. 1d.

3. Calculations of structural parameters

A key parameter to determine the capacity of gas and water transport in GDL is its porosity ε defined by the ratio of pore volume over total volume. A GDL should be sufficiently porous to allow the flow of reactant gas and water, be electrically and thermally conductive, and have adequate rigidity in order to support the membrane electrolyte assembly. The calculation of porosity can be summarised in two steps. (1) A threshold is applied to the reconstructed grey scale images and the binary images are thus obtained. In each binary image 0 and 1 represent void space and solid space, respectively. (2) A cubic matrix of these images is built and the ratio between the number of zeros and the total number of elements in the matrix is obtained as the porosity of the GDL layer.

The anisotropy in porous media properties was found to be the most important factor of mechanical strength (Odgaard, 1997). Isotropy (or anisotropy) is a measure of 3D symmetry or the presence (or absence) of preferential alignment of structures along a particular directional axis. In a complexly structured volume containing void and solid, if the volume is isotropic, then a straight line passing through the volume at any orientation will make a similar number of intercepts through the solid phase. A GDL could be anisotropic, since lines going along the direction of filaments would make few
intercepts while lines crossing at right angle to the direction of the majority of the filaments would make many intercepts (Fig. 1a). The mean intercept length (MIL) measures isotropy by sending a line through a 3D image containing binary objects and then by dividing the length of the test line through the analysed volume by the number of intercepts between the lines and the solids. A large number of test lines are drawn passing through each point of the volume and anisotropy tensor analysis is used. Finally, one can derive a single parameter from the tensor eigenanalysis measuring anisotropy and express it as the minimum eigenvalue divided by the maximum eigenvalue. Degrees of anisotropy calculated in this way vary from 0 (fully isotropic) to 1 (fully anisotropic) (SkyScan Microtomography., 2007).

The mean pore radius is an important parameter in GDL characterisation as Knudson diffusion coefficient is a linear function of mean pore radius (Weber and Newman, 2004). In the analysis of 3D images produced using nano-CT, a 3D spherical local radius can be measured (Ulrich et al., 1999). The local radius for a point in a solid/pore is defined as the radius of a sphere with two conditions (Hildebrand and Ruegsegger, 1997): (1) the sphere encloses the point and (2) the sphere is entirely bounded within the solid/pore surfaces.

The above parameters have been calculated directly from the voxel representation through CTAN software based on a sample volume of 300×700×900 µm with 680 nm pixel resolution.

4. Calculations of fluid transport parameter

Permeability is one of the most important transport parameters of a porous material, describing the ability of the medium to conduct viscous fluids. The permeability of a medium depends on its pore geometry. Simulating gas flow through the void space in the 3D X-ray image can reveal the velocity field in detail and help estimate the permeability. However, the complexity of the 3D pore geometry in the GDL makes a direct simulation of fluid flow through it difficult. In this research the LB model was used to simulate the microscopic velocity field and thus the absolute permeability as a macroscopic property.

Unlike the traditional computational fluid dynamics (CFD) the LB method does not solve a group of partial differential equations, but simulates fluid flow by tracking the movement and collisions of a number of fictitious fluid particles in lattice (Chen et al., 1992; McNamara and Zanetti, 1988; Frisch et
The following equation describes the movement and collisions of the fluid particles:

\[ f_i(x + e_i \delta t, t + \delta t) = f_i(x, t) + \left[f_i^{eq}(x, t) - f_i(x, t)\right]/\tau \]  \hspace{1cm} (1)

where \( f_i(x, t) \) is the distribution function of the particle at location \( x \) and time \( t \); \( e_i \) the velocity, \( f_i^{eq}(x, t) \) the value of \( f_i(x, t) \) at equilibrium, and \( \tau \) is a dimensionless relaxation parameter that controls the rate at which \( f_i(x, t) \) approaches \( f_i^{eq}(x, t) \). The particles in each void voxel are allowed to move in 19 directions from the origin, as shown in Fig. 2, which includes stagnation at the origin, \( e_0 \).

The equilibrium distribution of particles moving in each of the 19 direction is given by

\[ f_i^{eq}(x, t) = w_i \left\{ \rho + \rho_0 \left[ \frac{1}{c_i^2} (e_i \cdot u) + \frac{1}{2c_i^2} (e_i \cdot u)^2 - \frac{1}{2c_i^2} (uu) \right] \right\} \]  \hspace{1cm} (2)

where \( w_i \) is a weighting factor in which \( w_i = 1/3 \) for \( |e_i| = 0 \), \( w_i = 1/18 \) for \( |e_i| = \delta x/\delta t \) and \( w_i = 1/36 \) for \( |e_i| = \sqrt{2} \delta x/\delta t \), \( \rho \) is fluid density, \( \rho_0 \) is a reference fluid density, \( u \) is the bulk fluid velocity, \( \delta x \) is the side length of the voxel and \( \delta t \) is a time step. The density and the bulk fluid velocity in each void voxel are calculated from

\[ \rho(x, t) = \sum_{i=1}^{9} f_i(x, t) = \sum_{i=1}^{9} f_i^{eq}(x, t) \]  \hspace{1cm} (3)

\[ \rho_0 u(x, t) = \sum_{i=1}^{9} e_i f_i(x, t) = \sum_{i=1}^{9} e_i f_i^{eq}(x, t) \]  \hspace{1cm} (4)

The above LB framework simulates the dynamics of a fluid with kinematic viscosity \( \nu \) given by

\[ \nu = \delta x^2 (\tau - 0.5)/3 \delta t \] and pressure by \( P = c_i^2 \rho \). Implementation of the LB model involves a collision step and a streaming step during each time step \( \delta t \). The collision step calculates the term on the left-hand side of Eq. (1) as \( f_i^c(x, t) = f_i(x, t) + \left[f_i^{eq}(x, t) - f_i(x, t) - f_i(x, t)\right]/\tau \), and the streaming step moves the pre-collision result from the voxel at \( x \) to its adjacent voxel at \( x + e_i \delta t \); the time for the particle to complete such a movement is \( \delta t \); that is \( f_i^c(x + e_i \delta t, t + \delta t) = f_i^c(x, t) \).

To simulate gas flow, a pressure gradient is imposed in one direction (the \( x \) direction). The four sides of the image in other two directions are treated as periodic boundaries such that any particle coming out of the image from any side re-enters the image through its opposite side without changing its momentum. All simulations start from a zero velocity field and are terminated once the flow in the void...
space is deemed to have reached steady state. If the size of the image in the $x$, $y$ and $z$ directions are denoted by $L_x$, $L_y$ and $L_z$, respectively, when flow reached steady state, the average flow rates over the image in the three directions are

$$q_x = \frac{\sum u_x(x_i + y_i + z_i)}{L_xL_yL_z}, \quad q_y = \frac{\sum u_y(x_i + y_i + z_i)}{L_xL_yL_z}, \quad q_z = \frac{\sum u_z(x_i + y_i + z_i)}{L_xL_yL_z}$$  \quad (5)

where $u_x(x_i + y_i + z_i)$, $u_y(x_i + y_i + z_i)$, and $u_z(x_i + y_i + z_i)$ are the three velocity components of fluid in the void the voxel located at $(x_i + y_i + z_i)$. Once the average flow rates are known, the absolute permeability of the image along and off the flow direction is calculated from the Darcy's law as follows:

$$k_{xx} = \frac{\rho_0 v q_x}{(\Delta P/L_x)}, \quad k_{xy} = \frac{\rho_0 v q_y}{(\Delta P/L_x)}, \quad k_{xz} = \frac{\rho_0 v q_z}{(\Delta P/L_x)}$$  \quad (6)

where $\Delta P$ is the pressure drop applied at the two opposite sides of the images in the $x$ direction. Applying the pressure drop in the $y$ and $z$ directions allows obtaining the permeability in other two directions.

The LBE model was applied to a sample of $100 \times 300 \times 100 \mu m^3$ (where the $300 \mu m$ length corresponds to the principal flow direction) to simulate the gas flow through the void space in the GDL.

5. Image processing and results

Images from SkyScan 2011 nano-tomography scanner are in 256 greyscales. Thresholding process defines a partition on the greyscale, where darker regions in the 2D image slices represent solid space, while lighter regions represent void space. For instance, if an operator chooses 100 to be the threshold value, then pixels with grey levels less than 100 will be taken as void while pixels with grey value greater than 100 will be taken as solid.

In this research, a reference threshold value was chosen for processing greyscale images and creating binary images. Six more threshold values in increments of 1 on the greyscale were subsequently used as test threshold values and the corresponding binary images were generated.

5.1. Threshold variation and structural parameter
The first important parameter that can be calculated directly from a reconstructed model is porosity using the method described in Section 3. Fig. 3a shows that the porosity of a 300×700×900 µm³ region, which is the full area of tomography image and shows that the porosity changes linearly over the range of thresholds for the seven samples.

Since the calculation of degrees of anisotropy is time consuming, a cubic sample of 300 µm in length (equalling the thickness of the carbon paper) was selected for calculation purposes. Dimensionless degrees of anisotropy of the sample over the threshold variation is summarised in Fig. 3b for both pore and solid networks. It can be seen that threshold variation has a little effect on the degree of anisotropy for both solid and pore network in the GDL. A 3% variation in threshold results in a 2% change in the degree of anisotropy.

The average pore size of the 7 samples measuring 300×700×900 µm has been calculated and was found to change with the threshold value by 0.5 while the average pore diameter increased by 25% from 13.5 to 16.9 µm over a 3% threshold variation span linearly. This means that Knudson diffusion coefficient may also change about 25% over only 3% of threshold variation. The variation of the average pore diameter over threshold is shown in Fig. 4.

5.2. Threshold variation and fluid transport parameter

The reconstructed 3D model of the GDL is stored in a 3D binary array and uploaded to the LB model for porous flow simulation. In general modelling terms, the spatial resolution of the LB model has to match the pixel resolution of the 3D image. In the current study the GDL has a porosity of greater than 80%, which thereby eases the computational demand of the LB flow simulation. This therefore allows each voxel of the 3D binary image to be used directly as the lattices of the LB model. In this case, the spatial resolution of the LB model is set equal to the pixel resolution of the X-ray images. The application of the LB model to simulate the permeability of the carbon paper GDL was validated by the authors in previous work (Rama et al., in press).

The LB model was applied to four differently thresholded samples of 100×300×100 µm flowing along 300 µm length direction to simulate the detailed gas velocity field in the void space of the GDL, with the assumption that the void spaces were filled with air. The simulated velocity was then used to obtain the absolute permeability of the region. Because absolute permeability represents linear
dependence of gas flow rate on pressure gradient, it should be ensured that the flow rate in the simulations is also in this linear range. As such, the pressure difference applied to each region was set to 20 Pa. The simulations were carried out on a dual-core 2.01 GHz workstation with 3.25 GB RAM. A single-phase simulation for the region took 500 min. Fig. 5 illustrates that the through-plane permeability ($k_{xx}$) is a strong function of threshold variation.

6. Conclusions

In reconstruction of a digital model of a porous material from X-ray nano-tomography scans, a small variation in threshold may have a significant influence on structural properties of the structural model and on its simulated flow parameters. The aim of this study was to quantify the significance of the influence of the threshold variation to the key parameters of porous materials for the first time. The outcomes of this research provide a useful guidance to researchers in the selection of adequate threshold levels in a variety of tomography-based techniques.

In this research, the influence of a small threshold variation on the mechanical and fluidic flow properties of a carbon fibre GDL layer was studied. The results show that porosity increases linearly with reducing threshold. The linearity implies that the GDL structure can be assumed to be generally homogeneous in terms of material density distribution. The sensitivity of the degree of anisotropy for the solid/pore network to a 3% threshold variation is only about 2%.

The analysis on average pore diameter finds that it increases from 13.5 to 16.9 µm and can potentially therefore have an influence of 25% on Knudson diffusion coefficient of the GDL. Hence diffusion is a parameter sensitive to threshold.

Permeability is found very sensitive to the threshold and changes about 85% with only 3% threshold variation since increasing the porosity helps fluidic flow in the pore network. One way to reduce the effect of threshold on permeability is using a higher resolution scanner.

In conclusion, a small variation in the selection of threshold has a great effect on permeability, porosity and Knudson diffusion coefficient and negligible effect on degree of anisotropy. Researchers should be aware of the significance of selecting a threshold value towards the final simulation results when they process reconstructed images obtained from X-ray nano-tomography on porous materials.
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Fig. 1. 3D and 2D images of a GDL carbon paper sample. (a) An isometric view of the reconstructed image of GDL sample with 680 nm pixel resolution using CTAN, (b) a shadow X-ray tomographic image, (c) a 2D reconstructed slice image, and (d) a binary image of the cross-section shown in Fig. 1d.

Fig. 2. The 19 directions along which the particles in each void voxel move.
Fig. 3. Influence of threshold values on porosity and degrees of anisotropy of the GDL. (a) Porosity variation over threshold values and (b) degrees of anisotropy of both pore and solid network over threshold values.

Fig. 4. The relationship between the average pore diameter of the GDL and threshold values.
Fig. 5. Through plane permeability ($K_{zz}$) sensitivity over threshold variation. With only 3% variation of threshold the permeability is almost doubled from $2.38 \times 10^{-7}$ to $4.02 \times 10^{-7}$ mm$^2$ which is a significant change and is likely to affect the simulation results of the fuel cell.