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Analysis of critical–length data from Electromigration failure studies

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Abstract

An accurate estimation of the Blech length, the critical line length below which interconnect lines are immortal, is vital as it allows EDA tools to reduce their workload. In lines longer than the Blech length, either a void will inevitably nucleate and grow until the line fails, or the line will rupture. The majority of failure analyses reveal voiding as the failure mechanism however recent analysis suggest Blech length failures are characterised by simultaneous voiding and rupture, and a non-zero steady-state drift velocity. This paper provides an alternative interpretation of results.

1. Introduction

With the ongoing scaling of IC dimensions, copper interconnects become ever more susceptible to Electromigration (EM) failure. The more mobile metal atoms (typically those in the grain boundary network or at interfaces) are driven downstream by the high current density. In Dual Damascene (DD) copper, the line ends are terminated by a Ta–based barrier layer which prevents further progress. As a result the drifting copper is forced into the interconnect lattice, increasing compressive stresses close to the anode and tensile stresses close to the cathode. If sufficiently high, these stresses can lead to ruptures at the anode and voiding at the cathode, and either may cause interconnect failure.

A possible resource, in circuit design, is the critical length or Blech length effect. The stress gradient that builds up during copper migration leads to a back force which opposes the EM ‘wind’ force. In short lines a relatively small transfer of material is required to produce a gradient sufficient to offset the EM force, halt the metal migration, and so save the interconnect. Consequently all interconnect lines whose length L is shorter than some critical (Blech) length $L_{B}$ are immortal as far as Electromigration failure is concerned. Either such lines are unable to generate sufficient stress to nucleate a void or, if they are able to nucleate a void, then both the line is unable to generate sufficient stress to cause the line to rupture and the line is unable to grow the void to a size sufficient for failure to occur. Using standard EM theory, based on the Stress Evolution Model (SEM) of Korhonen et al., the two former cases (nucleation and rupture) lead to critical values of the current density–length product $jL_{B}$ [1], while the latter leads to a critical $jL^{2}$ [1, 2].

The word ‘unable’ in the present context means that, once the stress in the line reaches its steady-state, the tensile stress at the cathode ($x = L$) is too low for nucleation, $|\sigma(L, t \to \infty)| < |\sigma_{n}|$, or the compressive stress at the anode ($x = 0$) is too low to cause the line to rupture, $|\sigma(0, t \to \infty)| < |\sigma_{rip}|$, and the steady-state void volume is too small, $V(t \to \infty) < V_{c}$, to cause the (typically 10%) increase in line resistance that indicates failure. For a given current density $j$, it will be the smaller of these critical lengths, for growth and for rupture (rather than their sum as suggested in [3]) that is expected to be the measured value for $L_{B}$.

For a theoretical line of length equal to the critical value, i.e. one with $L = L_{B}$, failure will occur only as the steady–state is reached, leading to an asymptotic failure
time $t_0 \to \infty$. Similarly, all lines of length $L > L_a$ will fail in finite time and all lines of length $L < L_a$ will survive indefinitely. From this it is clear that the definition of $L_a$ is the longest interconnect that does not exceed either the void or rupture thresholds before the steady-state condition in the line is reached. In the case of most lines it is voiding, rather than rupture, which causes the final failure; which implies that in most cases the rupture threshold is relatively high.

The situation differs slightly between passivated and unpassivated lines. For unpassivated lines, such as those of Blech’s original gold on molybdenum experiments [4], there is no confinement to cause the compressive stress at the anode and the tensile stress at the cathode to rise with each transported atom. In such lines, the stress at the line ends builds up to steady-state levels, say $\sigma_c(\infty)$ and $\sigma_L(\infty)$, at the cathode and the anode respectively. If those stresses can generate a large enough gradient to balance the electron wind force, then EM will cease. If they are not, gold will continue to be displaced from cathode to anode. For an unpassivated line, in the steady–state, the gold ends will move at a steady velocity along the molybdenum. As the steady–state stress gradient, $(\sigma_c(\infty)–\sigma_L(\infty))/L$, is larger in shorter lines, a sufficiently short line can prevent electromigration, while longer lines cannot.

For the passivated lines used in ICs, the void front of a cathode void should not move in the steady–state, since that would imply atoms moving, stress redistribution, and a state not yet steady (the only exception to this is a steady rupture, considered later). Provided that this steady–state sets up before the various thresholds are reached, EM failure can be prevented. This is known as the short line effect, and can be vital in Electromigration–aware chip design as, by daisy chaining long interconnects, say in M1 and M2 sections, all lines can conceivably be made sufficiently short that EM ceases, this defines a critical or Blech length. In recent years a number of studies of the short line effect in DD copper have been reported [3, 5–14] some of which have indeed daisy chained interconnects of different lengths to increase the efficiency of the experiment. The purpose of this paper is to analyse that work using what might be described as standard theory for Electromigration [1].

Failure in copper interconnect begins with the nucleation of a void which is generally assumed to occur relatively quickly, although copper reservoirs and a variety of other techniques can slow this process down. For present purposes we shall assume that the voiding occurs at the cathode via [15]. Although there is much evidence that in a significant number of cases nucleation occurs several microns from the via, to which the void then drifts, such transient issues are unimportant here as it is asymptotic failure which is of interest.

Once the void is nucleated, the tensile stress at its free surface collapses, creating stress gradients close by which temporarily reinforce rather than oppose the EM force, sweeping neighbouring vacancies in the void [16]. After a period of initial relatively fast growth driven by this release of strain energy, the stress gradient force gradually dies out leaving only the EM wind force, which is independent of line length $L$ [16]. The void then undergoes a period of reasonably constant growth.

For a line of length just below $L_a$, the growth rate will gradually decrease, as the stress gradient is re-established, until a new steady–state obtained. At $L = L_a$, just as the steady–state is set up, either the void volume, or the compressive anode stress, will reach the critical void volume $V_c$, or the rupture threshold $\sigma_{rup}$, asymptotically [1,2].

The atomic drift velocity $v_{drift}$, from Blech [4], is

$$v_{drift}(x,t) = \frac{D_a \Omega}{kT} \left( \frac{Z^* q \rho}{\Omega} - \frac{\partial \sigma}{\partial x} \right)$$  \hspace{1cm} (1)$$

where $D_a$ is the atomic diffusivity, $Z^*$ the effective valence, $\rho$ the copper resistivity, $j$ the applied current density, $\Omega$ the atomic volume, $kT$ the thermal energy and $\sigma$ the tensile stress, (it will also be useful later to define the parameter $G = Z^* q \rho / \Omega$). Averaging over the line length $L$, and setting $\Delta \sigma(t) = \sigma_c(t) - \sigma_L(t)$ to be the stress drop along the line, then gives

$$\bar{v}_{drift}(t) = \frac{D_a \Omega}{kT} \left( \frac{Z^* q \rho}{\Omega} - j \frac{\Delta \sigma(t)}{L} \right)$$  \hspace{1cm} (2)$$

For an unpassivated line, the steady–state occurs when the cathode and anode reach their final values and, in general, $\bar{v}_{drift}(t \to \infty) \neq 0$.

This case, which is valid for unpassivated lines [4], has also been used consistently in the case of passivated lines [3, 5–14]. In passivated lines, unless the anode is steadily leaking copper into the surrounding dielectric stack, the steady–state occurs only when $\bar{v}_{drift} = 0$.

From eqn (1), this corresponds to $\sigma_{rup}(x) = \sigma_0 - Gx$ where the constant $\sigma_0$ depends upon the line boundary conditions, Fig (1).

In references [3,5–14] it is assumed that a rupture pins the anode stress at $\sigma_{rup}$. Should that happen the void will continue to grow until the flux leaking into the dielectric stack can be brought to a halt; this can only
happen when the line length from the anode edge of the void to the anode is \([\sigma_{\text{rup}}]/G\), as shown in Fig. (1). If the line is not to fail, the void must also be less that the critical length \(L_{\text{void}} = V_J/A\), where \(A\) is the line cross-sectional area, and consequently the Blech length would becomes \(L_B = |\sigma_{\text{rup}}|/G + L_{\text{void}} \approx |\sigma_{\text{rup}}|/G\), i.e. the rupture threshold. If lines are rupturing, this indicates that this should be used to define the Blech length.

In references [11, 13, 14] only void growth is considered, although a critical value of the \(jL\) product (implying nucleation or rupture) is sought rather than \(jL^2\), which is relevant to void growth [2]. References [5–8] define a probability of line failure, after the line ruptures and in the passivated case, as the ratio of two non–zero steady–state drift velocities,

\[
P(j, L) = C \frac{\bar{v}_{\text{drift}}(j, L)}{\bar{v}_{\text{drift}}(j, L_{\text{A}})}
\]

(3)

where the braces indicate the dependence of \(\bar{v}_{\text{drift}}\) on the current density \(j\) and line length \(L\), \(L_{\text{A}}\) is the longest line in the sample and \(C\) is a constant. Other authors [3, 9–14] associate the median time to failure \(MTTF\) with

\[
MTTF = \frac{L}{\bar{v}_{\text{drift}}(j, L)}
\]

(4)

The implications of eqns (3) or (4) are that the failure time is dominated by the time after a rupture, as it is only then when \(\bar{v}_{\text{drift}} \neq 0\) is possible at steady–state, and further that the rupture occurs in the manner of a controlled overflow of atoms into the dielectric stack, leading to \(\bar{v}_{\text{drift}} = \text{constant}\), rather than as an unpredictable breach. A line that ruptures with a non–zero steady–state velocity \(\bar{v}_{\text{drift}}\) must eventually fail, and for such lines the rupture condition must then determine the critical length. If the rupture pins the stress at the anode to a value lower than the rupture threshold \(|\sigma_A| \leq |\sigma_{\text{rup}}|\), then the void growth rate will simply decrease the failure time compared to a more robust line.

The motivation behind eqns (3) and (4) is the assumption that the steady–state stress is created very quickly (which would also include the rupture at the anode), and following which the void grows according to eqn (2). This seems difficult to justify as it is also eqn (2) that is responsible for the atomic transport which sets up that steady–state. The original experimental results, on which this assumption is based, come from the work of Hu et al. [18–20 and references therein]. That work, however, refers to Al(Cu) interconnect which is generally characterised rather differently: by a long nucleation period and a shorter growth period, \((n = 2\) in the Black equation). In addition the steady–state so described relates to the migration of the Cu solute [18], prior to aluminium migration, and on the impact of the resulting stress profile on the aluminium drift. The activation energy for Cu diffusion in the Al(Cu) grain boundary network is considerably smaller that for the Cu–nitride interface [21, 22], consequently the time for the steady–state Cu profile to develop in Al(Cu) cannot be assumed to be representative of events in DD Cu. The analysis given in refs [18–20] is also only relevant to long interconnects [20], and consequently is unsuitable for analysis of the short length effect.

Within the current picture, any variation between samples in the void growth rate just after their nucleation is determined not by the length, but rather by variations in the EM part of the drift velocity \(v_{\text{drift}}(x, t)\), i.e., essentially by variations between samples of the product \(Z^*D_e\). Thus potentially this variation is caused by the same mechanism that causes variations in interconnect failure times. For lines close to the Blech length, the anode stress affects the growth rate, which will eventually drop to zero if the line does not fail first. For very long lines, however, the anode will have little impact and the void will grow large enough to cause failure. For large \(L\), the growth rate is roughly constant, due to the roughly constant EM wind force, thus

\[
t_f = \frac{V_{cr}}{v_{\text{EM}}(L)hw} = \frac{kT}{Z \cdot D_e q \eta} h\]

(5)

The distribution of \(t_f\) is then dependent on the distributions of both the volume of copper moved \(V_{cr}\) and on the effective line diffusivity. In references [3, 5–14], and in most analysis \(V_{cr}\) is assumed fixed which for

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**Fig. 1.** The steady–state stress distribution for a line with a rupture, if the anode stress is pinned at \(\sigma_{\text{rup}}\).
now we do also. But in contrast in lines close to \( L_e \), it is clearly vital to also include the effects of the anode stress, which we do now.

2. Interpreting Blech length data

2.1. Nucleation/rupture experiments \(^{2,8}\) \((jL)_{cr}\)

Using a simple, one-dimensional linearised version of the stress evolution model (SEM) of Korhonen et al. [1], failure occurs when \([e.g. 17]\)

\[
\frac{(jL)_{cr}}{jL} = 1 - \frac{8}{\pi^2} \sum_{n=0}^{\infty} \exp\left(-\frac{(2n+1)^2\pi^2\kappa f}{4L^2}\right) = g\left(\frac{\kappa f L}{L^2}\right) \tag{6}
\]

which also defines the function \(g(\eta)\) in an obvious manner. \(\kappa\) is an effective diffusivity given by \(\kappa = BOD_\delta h/kT\) for bulk modulus \(B\), interface thickness \(\delta\), and line height \(h\). The critical value \((jL)_{cr}\) is given by \(\Omega\Delta\sigma_0 Z^* q_p\rho\) and independent of \(\kappa\). When \(jL\to(jL)_{cr}\), it is clear that \(t_f\to\infty\), as expected. In terms of the dimensionless parameter \(r = (jL)_{cr}/jL\), the failure time is

\[
t_f = \left(\frac{L^2 jL_{cr}^2}{\pi^2 \kappa f^2 r^2}\right) \tag{7}
\]

where \(\eta = g^{-1}(\eta)\) is the inverse function of \(r = g(\eta)\). Note as, for fixed \(L\), \(g^{-1}(\eta)\) depends on \(j\) this is more complex than Black’s equation. Since some of the rupture times are expected to be very long, some will be scheduled after the experiment has finished (at \(t = t_{cr}\), whatever the value of \(t_{cr}\)). Such line lengths \(L\) will appear to be in a grey area; some mortal, some appearing immortal. The probability of immortal, within the lifetime of the experiment, which is sought by eqn (3), is then simply \(P(j, L) = \text{Pr}\{t_f > t_{cr}\}\) or equivalently \(\text{Pr}\{\kappa < (jL)_{cr}\} = g^{-1}(\eta)\), from eqn (7). If the effective diffusivity values \(\kappa\) are distributed with a Cumulative Distribution Function (cdf) \(F(\kappa)\) we obtain

\[
P(j, L) = \int F\left(\frac{L^2 jL_{cr}^2}{\pi^2 \kappa f^2 r^2}\right) \tag{8}
\]

\(P(j, L)\) now gives an important measure of the diffusivity cdf, as in Fig. 2. For lognormal \(D_\kappa\), and hence \(\kappa\) values (consistent with lognormal failure times in eqns (5) and (7)), with a median value of \(\kappa_0\) and lognormal standard deviation \(\sigma_\kappa\), eqn (8) becomes

\[
P(j, L) = 1 + \frac{1}{2} \text{erf}\left(\sqrt{2}\sigma_\kappa^2 \right) \tag{9}
\]

2.2. Growth time experiments \(^{9\text{-}14}\) \((jL)^2\)

The growth of a void, again using the SEM equation of Korhonen et al. [1], follows the expression of He et al. [2], and failure occurs under the condition

\[
\frac{(jL)^2_{cr}}{jL^2} = 1 - \frac{32}{\pi^2} \sum_{n=0}^{\infty} \exp\left(-\frac{(2n+1)^2\pi^2\kappa f}{4L^2}\right) = h\left(\frac{\kappa f L}{L^2}\right) \tag{10}
\]

where \((jL)^2_{cr} = 2\Omega BV_{cr}/Z^* q_p\alpha\) is also independent of \(\kappa\). This leads to failure time (again more complex than Black’s) of

\[
t_f = \left(\frac{(jL)^2_{cr} s}{jL_{ex}}\right) h^{-1}(s) \tag{11}
\]

where \(s\) is the dimensionless parameter \((jL)^2_{cr}/jL^2\), and \(\xi = h^{-1}(s)\) is the inverse function of \(s = h(\xi)\). If rupture is unlikely then, eqn (11) rather than eqn (7) should be used to fit the data in Fig. 2. In this case \(P(j, L)\) is

\[
P(j, L) = F\left(\frac{(jL)^2_{cr} h^{-1}(s)}{jL_{ex}}\right) \tag{12}
\]

References [3,9–14] also consider the dependence of \(L/MTTF\) on \(jL\). If \(D_\kappa\) is lognormally distributed, eqns (7) and (11) imply that both \(t_f\) and \(L/MTTF\) will also be so. Then from eqn (11) the median time to failure \(MTTF\) is

\[
\frac{L}{MTTF} = jL \frac{\kappa_{50}}{\kappa_{50}} \frac{s}{(jL)^2_{cr} h^{-1}(s)} \tag{13}
\]

since \(s\) is independent of \(\kappa\). These authors also find an increasing value of the lognormal standard deviation for shorter lines. However, from say eqn (11),

\[
\log(t_f) = \log\left(\frac{1}{jD_\alpha}\right) + \log\left(\frac{(jL)^2_{cr} h^{-1}(s)/s}{\delta B\Omega/kTh}\right) \tag{14}
\]
Clearly, from eqn (14), the effect of changing either \( j \) or \( L \) does not change \( \sigma_{SD} \). A growing number of recent results, relating to in-line nucleation, void drift and extrusion occurrence, appear to show that accounting for variations in \( D_e \) with individual grain orientations, is necessary to interpret EM effects [17]. Consequently, short lines with fewer grains will have a wider variation. In other words, the analysis above should probably include intra-grain variations in \( D_e \). This may then explain the increase in the variation \( \sigma_{SD} \) as \( L \) decreases.

3. Results

Using eqns (8) and (12), it is now a simple matter to reinterpret the results of references [3, 5–14].

3.1. Nucleation/Rupture time experiments \(^{5–8} \) (jL)

Fig. (2) shows a comparison of results taken from references [7, 8] with theoretical results from eqn (9). The distribution of \( D_e \) values is assumed to be lognormal with a median value \( D_{e50} \) and a lognormal deviation \( \sigma_{SD} \). The fit corresponds to \( \sigma_{SD} = 0.7 \) and \( \kappa_{SD} f_{cr}/L_{cr}^2 = 0.2 \). As \( t_x \) was 45 days in the experiment, and \( L_{cr} \sim 110 \) \( \mu \)m [7,8], i.e. \( \kappa_{SD} \sim 9.3 \times 10^{-16} \) m\(^2\)/s. If \( B \Omega/kT \sim 40 \) [17] this gives a median effective atomic diffusivity of \( D_{eff,50} = \delta D_{eff}/n = 2.33 \times 10^{-14} \) m\(^3\)/s. The log-deviation \( \sigma_{eff} \) of \( D_{eff} \) values is rather large compared to that quoted (0.45) for the failure time of the multi-interconnect structures in [7,8]; however the median Diffusivity value \( D_{eff,50} \) itself is quite reasonable [e.g. 23]. In addition a second failure mode is quoted in [7,8] with a \( \sigma_{SD} \) value of 0.2 which acts to broaden the distribution, while here a single mode is assumed.

3.1. Growth time experiments \(^{10–14} \) (jL\(^2\))

The relationship between \( LMTTTF \) and \( jL \) indicated by eqn (13) is now compared with the fixed length experimental observations of [11], Fig. (3). Close to \( jL \), only one term in the sum in eqn (11) is required so,

\[
\frac{L}{T_f} = \frac{\pi^2 D}{4L \log \left( \frac{32}{\pi^2} j/j_{cr} \right)}
\]

With \( L = 50 \) \( \mu \)m and \( T = 300 \) K, as in [11], eqn (15) estimates a critical current density of 1.58\( \times 10^9 \) Acm\(^{-2}\), while fitting eqn (4) produces a value of \( j_{cr}L = 6319 \) Acm\(^{-1}\) (or \( j_{cr} = 1.26 \times 10^9 \) Acm\(^{-2}\)) thus underestimating \( j_{cr} \) by 25%. The result in [11] should probably, in any case, be presented as a critical jL\(^2\) rather than critical jL.

Fig. (4) compares \( L^2/T_f \) from eqn (15) (solid curve and squares to provide ‘data’ points) as a function of \( j/j_{cr} \) together with 0.85\( (j/j_{cr} - 0.3) \) (dashed curve) and 1.05\( (j/j_{cr} - 2/3) \) (dot–dashed curve). Fitting to large currents, underestimates the critical current by 70% while fitting to currents close to \( j_{cr} \) still underestimates \( j_{cr} \) by around 33%. This gives a useful comparison of the analysis in ref [12] which uses eqn (4) with \( \bar{v}_{drift} \) from eqn (2) to obtain a plot of \( 1/T_f \) against j. Fig. 4 suggests such fits of 1/failure-time to the current may lead to a critical current in error by 25% or over.

The lognormal standard \( \sigma_{SD} \) deviation should not depend on \( (j–j_{cr}) \), eqn (14) as \( L \) decreases towards \( L_B \). An increase in \( \sigma_{SD} \) as \( j \) approaches \( j_{cr} \) can be argued, but requires the development of the model with intra-line diffusivities – a shorter line averages over a smaller number of grains.

4. Conclusions

The purpose of this paper has been two fold. The
The experimental support on which it is based relates to a rather different situation in Al(Cu) in which copper diffusion reaches a steady–state before the aluminium migration begins [18, 19].

The second purpose is to provide some analysis of short length data in DD Cu interconnect. The definition of $L_B$ pivots on the approach to the steady–state stress within the interconnect. If the critical void size/rupture stress is reached before the steady–state is able to stop the atomic migration, the line will fail. Any line that ruptures will eventually fail as the stress gradient which would prevent void growth is released during the rupture. In copper it is generally believed that voids nucleate relatively quickly ($n = 1$ in the Black equation and this is borne out by most simulations e.g. [17 and references therein]. Close to $L_B$, the steady–state is reached exponentially slowly. It is the approach to the critical rupture stress/void size that is important in defining an immortal line, and hence $L_B$, and not the steady–state velocity of the void front afterwards (as in [5–8]). In addition an alternative analysis of the existing short length data can bring important information about failures and this may be used to corroborate EM models. For example, in this case, the probability of mortality within the time limit of the experiment is used to extract information on the cdf of the atomic diffusivity values. Finally, this work supports recent analysis which suggests that the variation of $D_v$ values between grains is important to all EM analysis [e.g. 17].

References

[22] The Cu$_2$SiN$_x$ diffusion activation energy Q=0.9eV (ref. [19]) while in Al(Cu) Q=0.7eV for Al, slowed down by the Al$_2$Cu precipitates. For the copper in the Al(Cu) grain boundary network Q should be considerably smaller [18].
[23] L Arnaud et al., Electromigration induced void kinetics in Cu interconnects for advanced CMOS nodes, Inter Rel Phys Sym (2011), 3E.1.1-3E.1.10, Monterey, CA, USA.